Economics

# WORKSHOP IN <br> THE PRACTICAL ASPECTS OF <br> SOLAR SPACE AND DOMESTIC WATER HEATING SYSTEMS FOR <br> RESIDENTIAL BUILDINGS 

MODULE 12

## ECONOMIC CONSIDERATIONS

## TABLE OF CONTENTS

Page
LIST OF FIGURES ..... 12-iii
LIST OF TABLES ..... 12-iii
INTRODUCTION ..... 12-1
OBJECTIVES ..... 12-1
FACTORS IN ANALYSIS ..... 12-2
EXAMPLE 12-1 ..... 12-12
EXAMPLE 12-2 ..... 12-12
EXAMPLE 12-3 ..... 12-13
ENERGY COSTS ..... 12-15
INFLATION RATES ..... 12-19
SOLAR SYSTEM COSTS ..... 12-20
EQUIPMENT AND INSTALLATION TIME ESTIMATES ..... 12-21
Liquid-Heating Systems ..... 12-21
Air-Heating Systems ..... 12-22
TYPICPL INSTALLED COSTS ..... 12-23
Liquid-Heating System ..... 12-23
Air-Heating System ..... 12-24
MORTGAGE PAYMENTS ..... 12-25
PROPERTY TAX, INSURANCE, AND CREDIT ON INCOME TAXES ..... 12-25
OPERATING COSTS ..... 12-30
MAINTENANCE COSTS ..... 12-31
ECONOMIC ANALYSIS WORKSHEETS ..... 12-31
WORKSHEET LCA-1 ..... 12-32

## TABLE OF CONTENTS

|  |  |  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| WORKSHEET LCA-2 |  |  |  |  |  |  |  |  |  |  |

## LIST OF FIGURES

Figure Page
12-1 Energy Cost per Million Btu for Natural Gas Propane and No. 2 Fuel Oil ..... 12-17
12-2 Energy Cost per Million Btu for Electricity ..... 12-18
12-3 Inflation Factors ..... 12-19
12-4 Repayment on Loan ..... 12-26
12-5 Fraction of Mortgage Payment which is Interest ..... 12-29
LIST OF TABLES
Table Page
12-1 Values of $P / X(d, r, n)$ for Discount Rate of 0 Percent ..... 12-6
12-2 Values of $P / X(d, r, n)$ for Discount Rate of 4 Percent . ..... 12-7
12-3 Values of $P / X(d, r, n)$ for Discount Rate of 6 Percent ..... 12-8
12-4 Values of $P / X(d, r, n)$ for Discount Rate of 8 Percent ..... 12-9
12-5 Values of $P / X(d, r, n)$ for Discount Rate of 10 Percent ..... 12-10
12-6 Values of $P / X(d, r, n)$ for Discount Rate of 12 Percent ..... 12-11
12-7 Present Worth Factors (P) ..... 12-16

Solar heating systems involve higher capital costs than conventional systems and economic evaluations invariably involve cost comparisons between the two systems. Comparisons which do not account for future fuel cost savings for heating are both misleading and unfavorable to solar systems. By accounting for capital and operating costs of heating alternatives over a period of time, deemed to be the "life" of the systems, the relative economic merits of "paying for hardware" or "paying for energy" can be determined. Thus life-cycle costing methods have generally been used to make economic comparisons although speculative assumptions for the rate of increases in the energy prices, discount rates, costs for goods and services, property tax, insurance and income tax deductions are used in the analysis. While life-cycle cost analysis is a fair method for comparing solar and non-solar systems, homeowners may also consider annual cash flow differences between the two types of heating systems. Explanations for both methods are included in this module.

## OBJECTIVES

The objectives of this module are to describe methods for lifecycle cost and cash flow analyses to compare solar and non-solar systems. The participant of this workshop should be able to:

1. Estimate the installed cost of a solar system,
2. Establish the economic feasibility of a solar system.

## FACTORS IN ANALYSES

The total cost of a solar heating system, over the life of the system, includes (1) capital and installation costs or mortgage payments for money borrcwed to pay for the installed system, (2) fuel cost for the auxiliary unit, and (3) operating and maintenance ( 0 and M) costs. With a non-solar heating system the capital and 0 and $M$ costs are small but fuel costs are high (and rising steadily). A solar system has large capital costs, lower fuel costs, and non-negligible 0 and $M$ costs. A comparison is necessary to determine whether a solar system is economical compared to a non-solar system and the comparison is usually made for a selected number of years which is estimated to be the "life" of a system. A life-cycle cost analysis is first explained followed by an annual cash flow analysis.

The yearly cash flow for a residential solar heating system is:
$\underset{\text { With solar }}{\text { Yearly cost }}=\underset{\text { payment }}{\text { Mortgage }}+\underset{\text { Auxiliary }}{\text { fuel cost }}+\underset{\text { Property }}{\text { Pax increase }}+\underset{\text { premium }}{\text { Insurance }}$

$$
\begin{equation*}
+\underset{\text { Operating }}{\text { costs }}+\underset{\text { cost }}{\text { Maintenance }} \text { - Income tax savings for } \tag{12-1}
\end{equation*}
$$

whereas for a non-solar system,

$$
\begin{align*}
& \text { Yearly cost }  \tag{12-2}\\
& \text { for non-solar }
\end{aligned}=\begin{aligned}
& \text { Fuel } \\
& \text { cost }
\end{align*}+\begin{gathered}
\text { Operating and } \\
\text { maintenance costs }
\end{gathered}
$$

In commercial buildings there are other factors such as depreciation of equipment and salvage value to be considered.

The sum of the yearly cash flows over the "life" of the system can be construed as the life-cycle cost of the system, and the costs of the solar and non-solar systems can be compared over an equal lifetime of $n$ years, to determine which system would be more expensive.

Cash flow calculations should include inflation, with fuel costs perhaps increasing more rapidly than costs of general goods and services (at least in the near term). The use of different inflation factors for the items in Equation (12-1) or (12-2) in effect gives more weight to some cost items over others, say fuel costs over mortgage payments as an example, particularly if mortgage payment is fixed and fuel cost rises.

Because the sum of annual cash flows for both solar and non-solar systems would in effect add different value dollars each year as a consequence of inflation, a more appropriate economic comparison is made on the basis of present worth which discounts future expenditures to the value of first year dollars. Hence, when the present worth of future annual expenditures are added, equivalent value dollars are being added. When the inflation and discount factors are taken into consideration in a life-cycle cost analysis, Equations (12-1) and (12-2) may be rewritten as follows:

$$
\begin{equation*}
C_{T}(\text { solar })=\left(A C_{a}\right) E_{1}+C_{0} E_{0}+C_{m} E_{m}+(1-F) L c_{f} E_{f} \tag{12-3}
\end{equation*}
$$

and

$$
\begin{equation*}
C_{T C} \text { (non-solar) }=C_{o c} E_{0}+C_{m c} E_{m}+L c_{f} E_{f} \tag{12-4}
\end{equation*}
$$

where $A$ is the collector area, $\mathrm{ft}^{2}$
$C_{T}$ is the total life-cycle cost of the solar system, \$
${ }^{C_{T C}}$ is the total life-cycle cost of the rion-solar system, $\$$
$C_{a}$ is the installed cost of the solar system per unit collector area, $\$ / \mathrm{ft}^{2}$
$C_{0}$ is the first year operating cost for the solar system, \$/yr
$C_{\text {oc }} \begin{aligned} & \text { is the first year operating cost for the non-solar system, } \\ & \$ / y r\end{aligned}$
$C_{m}$ is the first year maintenance cost for the solar system, $\$ / y r$
$c_{\text {mc }}$ is the first year maintenance cost for the non-solar system, \$/yr
$c_{f}$ is the first year fuel cost per unit of delivered heat, $\$ /$ MMBtu
$\mathrm{E}_{1}$ is an economic factor which accounts for downpayment, mortgage interest rate, insurance rate, property tax rate, income tax saving, inflation rate, and market discount rate
$\mathrm{E}_{\mathrm{o}}$ is an economic factor which accounts for inflation rate of operating cost and market discount rate
$E_{m}$ is an economic factor which accounts for inflation rate of maintenance cost and market discount rate
$E_{f}$ is an economic factor which accounts for fuel inflation rate and market discount rate
$F$ is the fraction of annual heat provided by the solar system
$L$ is arı annual heating load for the building, MMBtu
The economic factors, $E_{0}, E_{m}$, and $E_{f}$ are the sums of annual compounded inflation factors discounted annually to present worth. The present worth of the sum of an annuity over a life time of $n$ years inflated at a constant rate and discounted at a constant rate can be written as:

$$
\begin{equation*}
P / X(d, r, n)=\frac{(1+d)^{n}-(1+r)^{n}}{(1+d)^{n}(d-r)} \text { for } d \neq r \tag{12-5}
\end{equation*}
$$

and

$$
\begin{equation*}
P / X(d, r, n)=n /(1+r) \text { for } d=r \tag{12-6}
\end{equation*}
$$

where $\quad P$ is the present value of an annuity over $n$ years
$X$ is the first year cost
d is the discount rate
$r$ is the inflation rate
n is the years of analysis or life of the system
The notation ( $d, r, n$ ) after $P / X$ indicates that the value of $P / X$ refers to values of $d, r$, and $n$, placed in the appropriate terms in

Equations (12-5) and (12-6). Tables of $P / X$ values are provided in this module for an appropriate range of $\mathrm{d}, \mathrm{r}$, and n in Tables 12-1 through 12-6.

The economic factors can now be expressed as:

$$
\begin{align*}
& E_{0}=P / X\left(d, r_{0}, n\right) \text { years }  \tag{12-7}\\
& E_{m}=P / X\left(d, r_{m}, n\right) \text { years }  \tag{12-8}\\
& E_{f}=P / X\left(d, r_{f}, n\right) \text { years } \tag{12-9}
\end{align*}
$$

The economic factor $\mathrm{E}_{1}$ is slightly more involved and is expressed as:

$$
\begin{align*}
&\left.E_{1}=\alpha+[(1-t) p+h)\right] P / X(d, g, n)+ \\
&(1-\alpha)\left[(1-t) \frac{P / X(d, 0, m)}{P / X(i, 0, m)}+(t) \frac{P / X(d, i, i n)}{P / X(0, i, m)}\right] \tag{12-10}
\end{align*}
$$

where
$\alpha$ is the downpayment rate in the terms of the loan and fixed mortgage payment is assumed
$t$ is the effective income tax rate of the owner,
$p$ is the property tax rate based on initial capital cost (first year market value),
$h$ is the insurance premium rate,
$g$ is the inflation rate for general cost of goods and services (general inflation rate),
$\mathfrak{i}$ is the interest rate of the loan,
$m$ is the term (years) of the loan
Values of $\mathrm{P} / \mathrm{X}(\mathrm{a}, \mathrm{b}, \mathrm{c})$ may be determined from Tables 12-1 through 12-6 by referring to the appropriate values in the tables as indicated by the terms in the parentheses following $P / X$. For example, $P / X(d, 0, m)$ may be determined by consulting the appropriate discount rate d , rate of annual increase 0 , (zero), and years $m$.

Table 12-1
Values of $P / X(d, r, n)$ for Discount Rate of 0 Percent

| Years | Annual Rate of Increase |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0 | 3 | 6 | 8 | 10 | 12 |
| 10 | 10.0 | 11.464 | 13.181 | 14.487 | 15.937 | 17.549 |
| 11 | 11.0 | 12.808 | 14.972 | 16.645 | 18.531 | 20.655 |
| 12 | 12.0 | 14.192 | 16.870 | 18.977 | 21.384 | 24.133 |
| 13 | 13.0 | 15.618 | 18.882 | 21.495 | 24.523 | 28.029 |
| 14 | 14.0 | 17.086 | 21.015 | 24.215 | 27.975 | 32.393 |
| 15 | 15.0 | 18.599 | 23.276 | $27.15 ?$ | 31.772 | 37.280 |
| 16 | 16.0 | 20.157 | 25.673 | 30.324 | 35.950 | 42.753 |
| 17 | 17.0 | 21.762 | 28.213 | 33.750 | 40.545 | 48.884 |
| 18 | 18.0 | 23.414 | 30.906 | 37.450 | 45.599 | 55.750 |
| 19 | 19.0 | 25.117 | 33.760 | 41.446 | 51.159 | 63.440 |
| 20 | 20.0 | 26.870 | 36.786 | 45.762 | 57.275 | 72.052 |
| 21 | 21.0 | 28.676 | 39.993 | 50.423 | 64.002 | 81.669 |
| 22 | 22.0 | 30.537 | 43.392 | 55.457 | 71.403 | 92.503 |
| 23 | 23.0 | 32.453 | 46.996 | 60.893 | 79.543 | 104.603 |
| 24 | 24.0 | 34.426 | 50.816 | 66.765 | 88.497 | 188.155 |
| 25 | 25.0 | 36.459 | 54.865 | 73.106 | 98.347 | 133.334 |
| 26 | 26.0 | 38.553 | 59.156 | 79.954 | 109.182 | 150.334 |
| 27 | 27.0 | 40.710 | 63.706 | 87.351 | 121.100 | 169.374 |
| 28 | 28.0 | 42.931 | 68.528 | 95.339 | 134.210 | 190.699 |
| 29 | 29.0 | 45.219 | 73.640 | 103.966 | 148.631 | 214.583 |
| 30 | 30.0 | 47.575 | 79.058 | 113.283 | 164.494 | 241.333 |

Table 12-2
Values of $P / X(d, r, n)$ for Discount Rate of 4 Percent

| Years | Annual Rate of Increase |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0 | 3 | 6 | 8 | 10 | 12 |
| 10 | 8.111 | 9.210 | 10.492 | 11.462 | 12.537 | 13.727 |
| 11 | 8.760 | 10.083 | 11.655 | 12.865 | 14.222 | 15.845 |
| 12 | 9.385 | 10.947 | 12.841 | 14.321 | 16.004 | 17.918 |
| 13 | 9.986 | 11.804 | 14.049 | 15.833 | 17.889 | 20.258 |
| 14 | 10.563 | 12.652 | 15.281 | 17.404 | 19.883 | 22.777 |
| 15 | 11.118 | 13.492 | 16.536 | 19.035 | 27.997 | 25.491 |
| 16 | 11.652 | 14.323 | 17.816 | 20.728 | 24.222 | 28.413 |
| 17 | 12.166 | 15.147 | 19.120 | 22.487 | 26.580 | 31.561 |
| 18 | 12.659 | 15.963 | 20.449 | 24.374 | 29.076 | 34.950 |
| 19 | 13.134 | 16.771 | 21.804 | 26.210 | 31.714 | 38.600 |
| 20 | 13.590 | 17.571 | 23.185 | 28.180 | 34.506 | 42.531 |
| 21 | 14.029 | 18.364 | 24.592 | 30.225 | 37.458 | 46.764 |
| 22 | 14.451 | 19.149 | 26.027 | 32.349 | 40.581 | 51.322 |
| 23 | 14.857 | 19.926 | 27.489 | 34.555 | 43.883 | 56.232 |
| 24 | 15.247 | 20.696 | 28.979 | 36.846 | 47.377 | 61.519 |
| 25 | 15.622 | 21.459 | 30.498 | 39.224 | 51.071 | 67.213 |
| 26 | 15.983 | 22.214 | 32.046 | 41.695 | 54.979 | 73.344 |
| 27 | 16.330 | 22.962 | 33.623 | 44.260 | 59.113 | 79.448 |
| 28 | 16.663 | 23.703 | 35.232 | 46.924 | 63.485 | 87.059 |
| 29 | 16.984 | 24.436 | 36.871 | 49.690 | 69.109 | 94.718 |
| 30 | 17.292 | 25.163 | 38.541 | 52.563 | 73.000 | 102.965 |

## Table 12-3

Values of $P / X(d, r, n)$ for Discount Rate of 6 Percent

| Years | Annual Rate of Increase |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0 | 3 | 6 | 8 | 10 | 12 |
| 10 | 7.360 | 8.319 | 9.434 | 10.277 | 11.208 | 12.238 |
| 11 | 7.887 | 9.027 | 10.377 | 11.414 | 12.575 | 13.874 |
| 12 | 8.384 | 9.715 | 11.321 | 12.573 | 13.993 | 15.603 |
| 13 | 8.853 | 10.383 | 12.264 | 13.753 | 15.464 | 17.430 |
| 14 | 9.295 | 11.033 | 13.208 | 14.958 | 16.991 | 19.360 |
| 15 | 9.712 | 11.664 | 14.151 | 16.182 | 18.575 | 21.399 |
| 16 | 10.106 | 12.277 | 15.094 | 17.430 | 20.220 | 23.553 |
| 17 | 10.477 | 12.873 | 16.038 | 18.703 | 27.926 | 25.830 |
| 18 | 10.828 | 13.452 | 16.981 | 19.9¢9 | 23.697 | 28.236 |
| 19 | 11.158 | 14.015 | 17.925 | 21.320 | 25.535 | 30.777 |
| 20 | 11.470 | 14.562 | 18.868 | 22.665 | 27.442 | 33.463 |
| 21 | 11.764 | 15.093 | 19.811 | 24.036 | 29.421 | 36.300 |
| 22 | 12.042 | 15.609 | 20.755 | 25.433 | 31.474 | 39.298 |
| 23 | 12.303 | 16.111 | 21.698 | 26.857 | 33.605 | 42.466 |
| 24 | 12.550 | 16.598 | 22.642 | 28.307 | 35.817 | 45.813 |
| 25 | 12.783 | 17.072 | 23.585 | 29.784 | 38.112 | 49.350 |
| 26 | 13.003 | 17.532 | 24.528 | 37.290 | 40.493 | 53.087 |
| 27 | 13.211 | 17.979 | 25.472 | 32.823 | 42.965 | 57.035 |
| 28 | 13.406 | 18.414 | 26.415 | 34.386 | 45.530 | 61.207 |
| 29 | 13.591 | 18.836 | 27.358 | 35.978 | 48.191 | 65.615 |
| 30 | 13.765 | 19.246 | 28.302 | 37.601 | 50.953 | 70.272 |

Table 12-4
Values of P/X (d, r, n) for Discount Rate of 8 Percent

| Years | Annual Rate of Increase |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0 | 3 | 6 | 8 | 10 | 12 |
| 10 | 6.710 | 7.550 | 8.525 | 9.259 | 10.070 | 10.965 |
| 11 | 7.139 | 8.127 | 9.293 | 10.185 | 11.183 | 12.297 |
| 12 | 7.536 | 8.676 | 10.046 | 11.111 | 12.316 | 13.679 |
| 13 | 7.904 | 9.200 | 10.786 | 12.037 | 13.470 | 15.111 |
| 14 | 8.244 | 9.700 | 11.513 | 12.963 | 14.645 | 16.597 |
| 15 | 8.559 | 10.177 | 12.225 | 13.889 | 15.842 | 18.137 |
| 16 | 8.851 | 10.632 | 12.926 | 14.815 | 17.061 | $19.735^{\circ}$ |
| 17 | 9.122 | 11.066 | 13.611 | 15.741 | 18.303 | 21.392 |
| 18 | 9.372 | 11.479 | 14.285 | 16.667 | 19.568 | 23.110 |
| 19 | 9.604 | 11.874 | 14.947 | 17.593 | 20.856 | 24.892 |
| 20 | 9.818 | 12.250 | 15.596 | 18.519 | 22.169 | 26.740 |
| 21 | 10.017 | 12.609 | 16.233 | 19.444 | 23.505 | 28.656 |
| 22 | 10.201 | 12.951 | 16.858 | 20.370 | 24.866 | 30.643 |
| 23 | 10.371 | 13.277 | 17.472 | 21.296 | 26.253 | 32.704 |
| 24 | 10.529 | 13.589 | 18.074 | 22.222 | 27.665 | 34.841 |
| 25 | 10.675 | 13.885 | 18.666 | 23.148 | 29.103 | 37.058 |
| 26 | 10.870 | 14.169 | 19.246 | 24.074 | 30.568 | 39.356 |
| 27 | 10.935 | 14.438 | 19.815 | 25.000 | 32.060 | 47.740 |
| 28 | 11.051 | 14.696 | 20.374 | 35.926 | 33.580 | 44.212 |
| 29 | 11.158 | 14.942 | 20.923 | 26.852 | 35.127 | 46.775 |
| 30 | 17.258 | 15.176 | 21.461 | 27.778 | 36.704 | 49.433 |

Table 12-5
Values of $P / X(d, r, n)$ for Discount Rate of 10 Percent

| Years | Annual Rate of Increase |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0 | 3 | 6 | 8 | 10 | 12 |  |
| 10 | 6.145 | 6.884 | 7.739 | 8.382 | 9.091 | 9.872 |  |
| 11 | 6.495 | 7.355 | 8.366 | 9.139 | 10.000 | 10.961 |  |
| 12 | 6.814 | 7.796 | 8.971 | 9.882 | 10.909 | 12.069 |  |
| 13 | 7.103 | 8.209 | 9.554 | 10.611 | 11.818 | 13.197 |  |
| 14 | 7.367 | 8.596 | 10.116 | 11.377 | 12.727 | 14.346 |  |
| 15 | 7.606 | 8.958 | 10.657 | 12.030 | 13.636 | 15.516 |  |
| 16 | 7.824 | 9.297 | 11.179 | 12.721 | 14.545 | 16.708 |  |
| 17 | 8.022 | 9.614 | 11.681 | 13.399 | 15.455 | 17.920 |  |
| 18 | 8.201 | 9.911 | 12.166 | 14.064 | 16.365 | 19.155 |  |
| 19 | 8.365 | 10.190 | 12.632 | 14.717 | 17.273 | 20.413 |  |
| 20 | 8.514 | 10.450 | 13.082 | 15.359 | 18.182 | 21.693 |  |
| 21 | 8.649 | 10.695 | 13.515 | 15.989 | 19.091 | 22.997 |  |
| 22 | 8.772 | 10.923 | 13.933 | 16.607 | 20.000 | 24.324 |  |
| 23 | 8.883 | 11.137 | 14.335 | 17.214 | 20.909 | 25.675 |  |
| 24 | 8.985 | 11.337 | 14.723 | 17.810 | 21.818 | 27.051 |  |
| 25 | 9.077 | 11.525 | 15.097 | 18.396 | 22.727 | 28.452 |  |
| 26 | 9.161 | 11.701 | 15.457 | 18.970 | 23.636 | 29.878 |  |
| 27 | 9.237 | 11.865 | 15.804 | 19.534 | 24.545 | 31.331 |  |
| 28 | 9.307 | 12.019 | 16.138 | 20.088 | 25.455 | 32.809 |  |
| 29 | 9.370 | 12.673 | 16.461 | 20.632 | 26.364 | 34.315 |  |
| 30 | 9.427 | 12.299 | 16.771 | 21.166 | 27.273 | 35.848 |  |

Table 12-6
Values of $P / X(d, r, n)$ for Discount Rate of 12 Percent

| Years |  |  | nnual Rate of Increase |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0 | 3 | 6 | 8 | 10 | 12 |
| 10 | 5.650 | 6.303 | 7.057 | 7.822 | 8.244 | 8.929 |
| 11 | 5.938 | 6.690 | 7.571 | 8.243 | 8.990 | 9.821 |
| 12 | 5.194 | 7.045 | 8.059 | 8.841 | 9.722 | 10.714 |
| 13 | 6.424 | 7.372 | 8.520 | 9.418 | 10.441 | 11.607 |
| 14 | 6.628 | 7.672 | 8.956 | 9.975 | 11.148 | 12.500 |
| 15 | 6.811 | 7.949 | 9.369 | 10.517 | 11.842 | 13.393 |
| 16 | 6.974 | 8.203 | 9.760 | 11.029 | 12.523 | 14.286 |
| 17 | 7.120 | 8.436 | 10.130 | 11.528 | 13.192 | 15.179 |
| 18 | 7.250 | 8.651 | 10.480 | 12.009 | 13.850 | 16.071 |
| 19 | 7.366 | 8.849 | 10.812 | 12.473 | 14.495 | 16.964 |
| 20 | 7.469 | 9.031 | 11.125 | 12.920 | 15.129 | 17.857 |
| 21 | 7.562 | 9.198 | 11.422 | 13.352 | 15.752 | 18.758 |
| 22 | 7.645 | 9.352 | 11.703 | 13.768 | 16.363 | 19.643 |
| 23 | 7.718 | 9.493 | 11.969 | 14.169 | 16.964 | 20.536 |
| 24 | 7.784 | 9.623 | 12.221 | 14.556 | 17.554 | 21.429 |
| 25 | 7.843 | 9.743 | 12.459 | 14.929 | 18.133 | 22.321 |
| 26 | 7.896 | 9.853 | 12.684 | 15.288 | 18.702 | 23.214 |
| 27 | 7.943 | 9.954 | 12.898 | 15.635 | 19.261 | 24.107 |
| 28 | 7.984 | 10.047 | 13.100 | 15.970 | 19.810 | 25.00 |
| 29 | 8.022 | 10.132 | 13.291 | 16.292 | 20.349 | 25.893 |
| 30 | 8.055 | 10.211 | 13.472 | 16.603 | 20.879 | 26.786 |

EXAMPLE 12-1
Determine the economic factors $E_{o}, E_{m}$, and $E_{f}$ if the manual rate of increase for operating cost, $r_{0}$, is 10 percent, annual rate of increase for maintenance, $r_{m}$, is 6 percent, annual rate of increase for fue1, $r_{f}$, is 12 percent, and the discount rate is 8 percent for a life span of 20 years.

Solution:

$$
\begin{aligned}
& E_{0}=P / X(8,10,20)=22.169 \text { (from Table 12-4) } \\
& E_{m}=P / X(8,6,20)=15.596 \text { (from Table 12-4) } \\
& E_{f}=P / X(8,12,20)=26.740 \text { (from Table 12-4) }
\end{aligned}
$$

## EXAMPLE 12-2

Determine the economic factor $\mathrm{E}_{\boldsymbol{\gamma}}$ if the terms of the loan are $m=25$ years, $i=10$ percent, and $\alpha=20$ percent downpayment. The property tax rate, $p$, is 3 percent and insurance rate, $h$, is 0.3 percent of market value, general inflation, $g$, is 6 percent, and the effective income tax rate is 35 percent. The market discount rate, d, is 8 percent.

Solution:
For Equation (12-10), find appropriate $P / X$ values from the tables.

$$
\begin{aligned}
& P / X(d, g, n)=P / X(8,6,20)=15.596 \\
& P / X(d, 0, m)=P / X(8,0,25)=10.675 \\
& P / X(i, 0, m)=P / X(10,0,25)=9.077 \\
& P / X(d, i, m)=P / X(8,10,35)=29.103 \\
& P / X(0, i, m)=P / X(0,10,25)=98.347
\end{aligned}
$$

$$
\begin{aligned}
\alpha & =0.20 \\
t & =0.35 \\
p & =0.03 \\
h & =0.003
\end{aligned}
$$

Thus,

$$
\begin{align*}
E_{1}= & 0.20+[(1-.35)(0.03)+0.003](15.596) \\
& +(1-0.2)\left[(1-.35) \frac{10.675}{9.077}+(0.35) \frac{29.103}{98.347}\right] \\
E_{1}= & 1.245 \tag{ans}
\end{align*}
$$

## EXAMPLE 12-3

Determine the present values of life-cycle costs of a solar system, a non-solar system and the savings with a solar system, given the following information:

$$
\begin{array}{ll}
A=500 \mathrm{ft}^{2} & r_{m}=6 \% \\
C_{a}=26 \$ / \mathrm{ft}^{2} & r_{f}=12 \% \\
C_{0}=87 \$ / \mathrm{yr} & \mathrm{~m}=25 \text { years } \\
C_{o c}=20 \$ / \mathrm{yr} & i=10 \% \\
C_{m}=100 \$ / \mathrm{yr} & \alpha=20 \% \text { down } \\
C_{m c}=10 \$ / \mathrm{yr} & \mathrm{p}=3 \% \text { of market value } \\
F=0.68 & h=0.3 \% \text { of market value } \\
C_{f}=10.25 \mathrm{R} / \mathrm{MMBtu} & g=6 \% \\
L=130 \mathrm{MMBtu} & t=35 \% \\
r_{0}=10 \% & d=8 \%
\end{array}
$$

Solution:
The equation to apply for the solar system is Equation (12-13).
From Example 12-1, $E_{0}=22.169, E_{m}=15.596, E_{f}=26.740$.
From Example 12-2, $\mathrm{E}_{\boldsymbol{j}}=1.245$

Therefore,

$$
\begin{aligned}
& \mathrm{C}_{\mathrm{T}}=(500)(26)(1.245)+(87)(22.169)+(100)(15.596) \\
&+(1-.68)(130)(10.25)(26.740) \\
& \mathrm{C}_{\mathrm{T}}= \$ 31,075 \text { present value over } 20 \text { years of } 1 \text { ife } \\
& \text { The equation to apply to the non-solar system is }
\end{aligned}
$$

Equation (12-4).

$$
C_{T C}=(20)(22.169)+(20)(15.596)+(130)(10.25)(26.740)
$$

$$
C_{T C}=\$ 36,230 \text { present value over } 20 \text { years of life }
$$

The cost of the non-solar is clearly larger than the cost of the solar system. The difference, or savings realizable with the solar system, is:

$$
\begin{aligned}
& \text { Present value } \\
& \text { of savings }
\end{aligned}=C_{T C}-C_{T}=36,230-31,075=\$ 5155
$$

While in Example 12-3 the present values of the total costs for systems and life time savings are determinable, the calculations are restricted to fixed annual increases, fixed discount rates, fixed property tax and insurance rates, and fixed income tax rates for the owner. These rates are, of course, uncertain in future years and highly variable. If variable rates are to be applied, a detailed year by year analysis of cash flow and present worth discounting must be carried out, using the basic form of Equations (12-1) and (12-2).

Annual cash flows are calculated for a system and the annual cost may be discounted to present value. The cost in a future year may be discounted to present worth by multiplying the cost by the present worth factor, P , in:

$$
\begin{equation*}
P=\frac{1}{(1+d)^{q}} \tag{12-11}
\end{equation*}
$$

where
$q$ is any year in the analysis period from 1 to $n$ d is the market discount rate

Values of $P$ for practical ranges of $d$ an $q$ are tabulated in Table 12-7.

ENERGY COSTS

The conversion of unit costs of energy to dollars per million Btu (\$/MMBtu) with various furnace efficiencies are shown on Figure 12-1 for natural gas, propane, and No. 2 fuel oil. The conversion of electric energy costs to dollars per million Btu for resistance heating and heat pumps with various coefficients of performance are shown on Figure 12-2. To determine the cost per million Btu of heat generated from furnaces, electric resistance heaters, or heat pumps, follow the unit cost of energy, found on the horizontal axis of the graphs, vertically to the appropriate line on the graph and read the cost in dollars along the vertical axis. For example, if No. 2 fuel oil cost fifty cents per gallon, and the furnace efficiency is 60 percent, the energy cost is $\$ 6.00 / \mathrm{mBtu}$ or 60 cents per therm ( $\$ /$ therm). If the furnace is more efficient, say 70 percent, the energy cost is $\$ 5.10 / \mathrm{MMBtu}$ or 51 \$/therm. Similarly, if electricity costs three cents per kilowatt-hour (C/kWh), and resistance heating is used, the energy cost is $\$ 8.80 /$ MMBtu. If a heat pump is used, and the COP of the heat pump is 2, the energy cost is \$4.40/MMBtu.

The cost of energy will increase in future years and an estimate of the rate of increase is subject not only to inilation rates of goods and services, but also to economic and political decisions of the federal government and the governments of other nations. One expects, however, the rate of fuel cost increases to be different from "normal" inflation rates and higher by a few percent, at least for the immediate future.

Table 12-7
Present Worth Factors (P)
(use for Worksheet LCA-4)

| Year of <br> Analysis | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | .943 | .935 | .926 | .917 | .909 | .901 | .893 | .885 | .877 | .870 | .862 |
| 2 | .890 | .873 | .857 | .842 | .826 | .812 | .797 | .783 | .769 | .756 | .743 |
| 3 | .840 | .816 | .794 | .772 | .751 | .731 | .712 | .693 | .675 | .658 | .641 |
| 4 | .792 | .763 | .735 | .708 | .683 | .659 | .636 | .613 | .592 | .572 | .552 |
| 5 | .747 | .713 | .681 | .650 | .621 | .593 | .567 | .543 | .519 | .497 | .476 |
| 6 | .705 | .666 | .630 | .596 | .564 | .535 | .507 | .480 | .456 | .432 | .410 |
| 7 | .665 | .623 | .583 | .547 | .513 | .482 | .452 | .425 | .400 | .376 | .354 |
| 8 | .627 | .582 | .540 | .502 | .467 | .434 | .404 | .376 | .351 | .327 | .305 |
| 9 | .592 | .544 | .500 | .460 | .424 | .391 | .361 | .333 | .308 | .284 | .263 |
| 10 | .558 | .508 | .463 | .422 | .386 | .352 | .322 | .295 | .270 | .247 | .227 |
| 11 | .527 | .475 | .429 | .388 | .350 | .317 | .287 | .261 | .237 | .215 | .195 |
| 12 | .497 | .444 | .397 | .356 | .319 | .286 | .257 | .231 | .208 | .187 | .168 |
| 13 | .469 | .415 | .368 | .326 | .290 | .258 | .229 | .204 | .182 | .163 | .145 |
| 14 | .442 | .388 | .340 | .299 | .263 | .232 | .205 | .187 | .160 | .141 | .125 |
| 15 | .417 | .362 | .315 | .275 | .239 | .209 | .183 | .160 | .140 | .123 | .108 |
| 16 | .394 | .339 | .292 | .252 | .218 | .188 | .163 | .141 | .123 | .107 | .093 |
| 17 | .371 | .317 | .270 | .231 | .198 | .170 | .146 | .125 | .108 | .093 | .080 |
| 18 | .350 | .296 | .250 | .212 | .180 | .153 | .130 | .111 | .095 | .081 | .069 |
| 19 | .331 | .277 | .232 | .194 | .164 | .138 | .116 | .098 | .083 | .070 | .060 |
| 20 | .312 | .258 | .215 | .178 | .149 | .124 | .104 | .087 | .073 | .061 | .051 |
| 21 | .294 | .242 | .199 | .164 | .135 | .112 | .093 | .077 | .064 | .053 | .044 |
| 22 | .278 | .226 | .184 | .150 | .123 | .101 | .083 | .068 | .056 | .046 | .038 |
| 23 | .262 | .211 | .170 | .138 | .112 | .091 | .074 | .060 | .049 | .040 | .033 |
| 24 | .247 | .197 | .158 | .126 | .102 | .082 | .066 | .053 | .043 | .035 | .028 |
| 25 | .233 | .184 | .146 | .116 | .092 | .074 | .059 | .047 | .038 | .030 | .024 |


Natural Gas - Price/IOOft ${ }^{3}$ \# 2 Fuel Oil-Price /Gallon Propane - Price /Gallon

Figure 12-1. Energy Cost per Million Btu for Natural Gas, Propane and No. 2 Fuel $0 i 1$


Figure 12-2. Energy Cost per Million Btu for Electricity

The increases in costs per unit of energy, several years in the future in terms of cents per gallon, cents per kilowatt-hour, cents per hundred cubic feet of natural gas, or dollars per therm, can be estimated on the basis of annual percentage of increases over current costs. The multiplying factors for current energy costs to determine future costs is shown on Figure 12-3. The horizontal axis is the years beyond the current year. The vertical axis gives the multiplying factor over current costs, and is simply the interest compounded annually, $(1+i)^{n}$.


Figure 12-3. Inflation Factors

For example, if the current cost of electricity is expected to increase at a rate of 6 percent each year for the next 12 years, at the end of 12 years the electricity cost will double. If 3 cent per kilowatt-hour is the current cost and heating cost is $\$ 8.80$ per million Btu, at the end of 12 years the electricity will cost 6 cents per kilowatthour and $\$ 17.80$ per million Btu.

## SOLAR SYSTEM COSTS

There is much speculation about the installed costs of solar systems and there is little information available to substantiate published information on costs. System costs based on research projects and demonstration projects funded by the federal government are misleading because the total costs of such projects include considerable engineering design costs and research staff costs. In some instances instrument costs for monitoring the performance of experimental systems, and often development costs of several alternative components in the systems are also included. The costs reported in popular magazines and newspaper accounts are likewise misleading because often systems which are designed and assembled by the owner on a do-it-yourself basis are cited and costs for the owners's time is seldom included in the cost quotations.

Guidelines are provided below to estimate the installed cost of a solar system including equipment costs and the cost of labor to install the system. Of these two items equipment costs are the largest and easiest to estimate, largely by consulting manufacturer's literature and price lists. Estimating labor costs is more difficult because it
depends upon the type of installation, location of the house and experience of the installer. Some ranges in prices for equipment and estimates in terms of man-hours for installation of systems in new buildings are listed below to provide cost estimating guidelines.

## EQUIPMENT AND INSTALLATION TIME ESTIMATES

## Liquid-Heating Systems

Typical equipment and material prices (in 1978) are listed below.

Item Unit

|  |  | Low | Medium | High |
| :--- | :---: | ---: | ---: | ---: |
| Flat-plate collectors and <br> mounting hardware | $\mathrm{ft}^{2}$ | 10 | 15 | 24 |
| Storage tank | 750 -1200 gal <br> capacity | 1000 | 1500 | 2500 |
| Pumps and motor | $10-20$ gpm | 80 | 180 | 350 |
| Heat exchanger | each | 200 | 300 | 400 |
| Controls and sensors | each | 500 | 750 | 1500 |
| Piping (3/4 inch copper) | ft | .45 | .60 | $.80-.85$ |
| Valves | each | 20 | 30 | 45 |
| Misc. fittings | - | 200 | 250 | 350 |
| Expansion tank | - | 60 | 80 | 100 |
| Insulation | - | 500 | 750 | 1000 |
| DHW Preheat tank | each | 80 | 100 | 150 |

Installation time estimates for typical liquid-heating systems are listed below:

| Item | Unit | Time (man-hours) |  |  |
| :--- | :---: | ---: | :---: | :---: |
|  |  | Low | Medium | $\underline{\text { High }}$ |
| Collectors and flashing | $400-500 \mathrm{ft}^{2}$ | 40 | 60 | 80 |
| Storage tank | each | 8 | 10 | 12 |
| Piping loops | all | 40 | 60 | 80 |
| DHW preheat subsystem | - | 8 | 12 | 20 |
| Insulation | all | 16 | 20 | 30 |
| Controls | - | 8 | 12 | 16 |
| Testing and balancing |  | 10 | 15 | 20 |

## Air-Heating Systems

Typical equipment and material prices (in 1978) are listed below Item Unit Price Range (in dollars)

Low Medium High

| Flat plate collectors and |  | 10 | 15 | 24 |
| :--- | ---: | ---: | ---: | ---: |
| mounting hardware | $\mathrm{ft}^{2}$ | 10 | 1 | 1.5 |
| Storage containers | $\mathrm{ft}^{3}$ | 0.5 | 4 | 5 |
| Gravel | ton | 3 | 175 | 200 |
| Blower and motor | each | 150 | 750 | 1500 |
| Control and sensors | set | 500 | 125 | 150 |
| Motorized dampers | each | 115 | 60 | 80 |
| Heat Exchanger | each | 45 | 100 | 150 |
| DHW Preheat tank | each | 80 | 3500 |  |
| Ducts | bulk | 2000 | 2500 | 350 |
| Insulation | bulk | 500 | 750 | 1000 |
| Miscellaneous |  | 200 | 300 | 400 |

Installation time estimates of typical air-heating systems are listed below

| Item | Unit | Time (man-hours) |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | Low | Medium | High |
| Collectors | 400-500 $\mathrm{ft}^{2}$ | 40 | 60 | 80 |
| Storage unit | each | 20 | 25 | 30 |
| Ducting | a11 | 50 | 75 | 100 |
| Controls | - | 8 | 12 | 16 |
| DHW preheat subsystem | - | 8 | 12 | 20 |
| Insulation |  | 16 | 20 | 30 |
| Testing and balancing | - | 10 | 15 | 20 |

## TYPICAL INSTALLED COSTS

## Liquid-Heating System

An estimate for the installed cost of a typical liquid-heating system in a new building with $400 \mathrm{ft}^{2}$ of collectors is outlined below using the median values in the foregoing section.

| 1. Collectors | equipment $400 \mathrm{ft}^{2} / \$ 15 / \mathrm{ft}^{2}$ <br> installation $60 \mathrm{hrs} \times \$ 15 / \mathrm{hr}$ | $\$ 6,000$ |
| :--- | :--- | ---: |
|  | 900 |  |

2. Storage Tank equipment 1,500
installation $10 \mathrm{hrs} \times \$ 15 / \mathrm{hr} 150$
3. Pipe Loops equipment 2,070
installation $60 \mathrm{hrs} \times \$ 15 / \mathrm{hr} 900$
4. DHW Subsystem equipment 280
installation, 12 hrs x \$75/hr 180
5. Controls equipment 750
installation 12 hrs x \$15/hr 180
6. Insulation materials 750
installation $20 \mathrm{hrs} \times \$ 15 / \mathrm{hr} 300$
7. Testing and balancing 225

Total Estimated Costs $\quad \mathbf{1 4 , 1 8 5}$
Breakdown of costs:
Equipment \& materials 11,350
Labor $\underline{\underline{2,835}}$
Installed cost/unit collector area $\quad \$ 35.46 / \mathrm{ft}^{2}$

## Air-Heating System

An estimate of the installed cost of a typical air-heating system in a new building with $400 \mathrm{ft}^{2}$ of collectors is outlined below using the median values in the foregoing section.

| 1. Collectors | equipment <br> installation 60 <br>  $\mathrm{fts}^{2} \times \$ 15 / \mathrm{ft}^{2}$ | $\$ 6,000$ |
| :--- | :--- | :--- |
|  | 900 |  |

2. Pebble Bed Container $300 \mathrm{ft}^{3} \times \$ 1 / \mathrm{ft}^{3} \quad 300$ Grave1 15 tons $\times \$ 4 /$ ton 60 Assembly $25 \mathrm{hrs} \times \$ 15 / \mathrm{hr} 375$
3. Duct, Pumpers \& blowers

Equipment 3,175
installation $75 \times \$ 15 / \mathrm{hr} \quad 1,125$
4. DHW Subsystem equipment 385
installation $12 \times \$ 15 / \mathrm{hr} 180$
5. Controls equipment 750
installation $12 \mathrm{hrs} \times \$ 15 / \mathrm{hr} 180$
6. Insulation materials 750
installation $20 \mathrm{hrs} \times \$ 15 / \mathrm{hr} 300$
7. Testing and balancing
$15 \mathrm{hrs} \times \$ 15 / \mathrm{hr}$
225
Total Estimated Costs 14,705
Breakdown of costs:
Equipment \& materials 11,420
Labor 3,285
Installed cost/unit collector area $\$ 36.76 / \mathrm{ft}^{2}$

The largest portion of the annual cost of a solar system is the repayment of the loan obtained to install the system. The loan may be based on the total building costs or separately on the solar system alone. In either event, a downpayment ranging from 10 to 20 percent is required to secure the loan.

The annual mortgage payments can be calculated from the mortgage interest rate and term of the loan using the curves of Figure 12-4. To illustrate the use of Figure 12-4, suppose that a solar system with 400 square feet of collectors cost $\$ 12,500$. A 20-year loan is obtained to purchase and install the system with interest at 9 percent, which requires a 20 percent downpayment. The annual mortgage payment on the loan is calculated as follows:

Annua 1
Mortgage $=($ System cost - downpayment $) \times($ Annual repayment factor $)$ (from Figure 12-4)
or
$\$ 1100=(12,500-2500) \times(0.11)$

PROPERTY TAX, INSURANCE, AND CREDIT ON INCOME TAXES

The annual cost of a solar system includes all the items contributing to the cash flow to operate a solar heating system. The costs include the mortgage payment and fuel costs, operating and maintenance costs, property tax, insurance on the solar system, income tax credits and savings on federal and state income taxes for property tax and interest paid on the loan.


Figure 12-4. Repayment on Loan

A major item of income tax credit is the recently passed legislation by the federal government, which allows a maximum credit of $\$ 2200$ from the owner's federal income tax liability. The credit allowance is 30 percent of the first $\$ 2000$ and 20 percent of the next $\$ 8000$ of the cost of the installed system. In some states there are additional credits provided to state income taxes for owners of solar systems.

Property taxes are based on a fraction of the assessed value of the solar system. The method of assessment, and the tax rate, varies from state to state and sometimes from county to county within the state. The office of the county treasurer can provide detailed information on method of assessed valuation on property and the tax rate. Usually, the assessed value is a fraction of the market value of the property and the tax rate is applied to the assessed value. In Colorado, the maximum assessed value of a solar system is 5 percent of market value. The amount of property tax on the solar system can be calculated as follows:
$\underset{\text { Pax }}{\text { Property }}=($ System cost $) \times($ Fraction of assessed value) $\times$ (tax rate)
Insurance rates on houses with a solar system, at present, are the same as for houses without solar systems. The basic insurance rate depends upon the type of house construction and location of the building within or outside a city or town. The insurance rate for a comprehensive homeowners policy differs from that for a straight fire insurance policy and the insurance rates for earthquake and flood damage (which is federally subsidized) are the only special insurances available for owners of buildings. The information on various insurance rates are available from local insurance agents. However, very few insurance companies have established insurance rates for solar systems. Damage to the contents
of a building resulting from leaks in piping or storage tanks or damage to the solar system resulting from flooding by natural causes is based on comprehensive or flood insurance rates. Although there are many factors to be considered, the annual premium on insurance for houses with solar systems is less than one percent of the value of the house and contents, and ranges from 0.3 to about 0.6 percent.

The "savings" on state and federal income taxes for property tax and interest paid on the mortgage can be substantial, depending upon the "tax bracket" of the homeowner. The amount of interest paid annually on the mortgage decreases with the number of years remaining on the mortgage. The portion of annual mortgage which is paid as interest can be determined from the graphs on Figure 12-5. The use of curves in the figure is illustrated in the following example.

Let us assume that a loan of $\$ 10,000$ has been secured at a term of 20 years and 9 percent interest. The annual mortgage payment was computed in the previous section to be $\$ 1100$. Of that mortgage payment, 82 percent, or $\$ 900$, is for interest in the first year. As this is the first year of payment, 20 years remain on the mortgage at the beginning of the year. By following the vertical line corresponding to 20 years in Figure 12-5 to the 9 percent curve, it is seen that the fraction of mortgage payment, which is interest, during the first year is 0.82 . In the eleventh year, with ten years remaining on the mortgage at the beginning of the year, the interest paid during the year is $(0.575) \times(\$ 1100)$, or $\$ 632$. The income tax savings on a federal or state return for interest and taxes would be:

$$
\binom{\text { Income }}{\text { tax credit }}=\binom{\text { Interest and }}{\text { taxes }} \times\binom{\text { Tax rate based }}{\text { on net income }}
$$



Figure 12-5. Fraction of Mortgage Payment which is Interest

The federal income tax return provides credit for state income taxes paid and many states give credit for federal income taxes. Thus the full credit for tax savings resulting from payment of interest is not simply the sum of state and federal tax savings. The net effective rate for states giving credit is:
$\begin{gathered}\text { Net } \\ \binom{\text { Effective }}{\text { Rate }}\end{gathered}=\binom{$ Federal }{ tax rate }$+\binom{$ State }{ tax rate }$-2\binom{$ Federal }{ tax rate }$\times\binom{$ State }{ tax rate } For states which do not give credit, the net effective rate is:

Net
$\binom{$ Effective }{ Rate }$=\binom{$ Federal }{ tax rate }$+\binom{$ State }{ tax rate }$-1\binom{$ Federal }{ tax rate }$\times\binom{$ State }{ tax rate }
If the income tax rate on a federal tax return is 25 percent and on a state tax return is 10 percent, the net effective rate is $(0.25+0.10-2 \times 0.25 \times 0.10) 0.30$, or 30 percent. The net annual income tax savings realized on the federal and state taxes for interest alone is $(0.30) \times(\$ 900)$, or $\$ 270$ in the first year and $(0.30) \times(\$ 632)$ or $\$ 190$ in the eleventh year.

OPERATING COSTS

The cost of operating a solar heating system, including the cost for operating the auxiliary unit in the system, is the cost of electric energy required to operate the pumps, central heat distribution fan, valves, and controller in a hydronic system, and the blowers, motorized dampers, and controller in an air system. The amount of energy used to collect, store, and distribute solar energy varies from system to system in the range from 5 to 10 percent of the total solar energy collected. The lower values in the range apply to low-heat systems with small pressure drops, and air systems with single blowers with small pressure
drops. The higher values in the range apply to high-head systems with large pressure drops, small systems with large pumps, and air systems with two blowers.

The operating cost for a non-solar system is much less than for a solar system. Although the blower size for distributing air to the rooms is the same, the power requirement is less for a non-solar system because the pressure drop in the system is lower. As an approximation, the energy required to operate a non-solar system is two to three percent of the total annual heating load.

## MAINTENANCE COSTS

The maintenance costs for solar systems is unknown; there is insufficient long-term experience with various systems to indicate an appropriate maintenance cost. While there is one air system that has been operated continuously for 19 years, on which the maintenance cost was zero, it can be expected that all solar systems will require some amount of maintenance during the life of the system. For the purpose of economic analysis, maintenance costs can be included each year for a nominal amount, say one hundred dollars, escalated annually at a selected inflation rate.

## ECONOMIC ANALYSIS WORKSHEETS

There are included in this section "short" forms and a "long" forms for calculating annual cash flow and life cycle costs of a system. The short form enables calculation of the present worth
of cummulative system and heating costs over the life of the system. The long method provides a year-by-year analysis of system cost, either in terms of present worth or cash flow, where the annual rates of increase can be changed for any item for any year. The steps for the calculations are outlined and explained on the worksheets. Sheets 1 and 2 of Worksheet LCA-1 are data sheets common to both the short and long forms.

## WORKSHEET LCA-1

Worksheets LCA-1 (2 sheets) are data sheets to facilitate the computations. Technical, economic, and cost data are listed on the worksheets.

WORKSHEET LCA-2
Worksheet LCA-2 outlines step by step procedure for calculating life-cycle costs of both the solar and non-solar system. The economic factors, E values, are determined from Tables 12-1 through 12-6.

Project $\qquad$
Building Data (see Worksheet B)

1. Annual space heating load MMBtu/yr
2. Annual DHW heating load $\square$ MMBtu/yr
3. Total H and DHW load (add lines 1 \& 2) $\qquad$ MMBtu/yr

Solar System Data
4. Collector area $\qquad$
$\mathrm{ft}^{2}$
5. Fraction of annual heating load supplied from solar

## Energy Prices

6. $c_{e}$, current energy cost for electricity (use Figure 12-2)
\$/kWhr
\$/MMBtu
7. $c_{f}, c_{f c}$, current cost of fuel
(use Figure 12-1 or 12-2) $\qquad$
Terms of Loan
8. $m$, term of the loan for solar system $\qquad$
9. $\alpha$, downpayment $\qquad$ \% decimal
10. i, interest rate on loan $\qquad$ \% decima 1

## Economic Data

11. $C_{a}$, installed cost of solar system per $\$ / \mathrm{ft}^{2}$
12. $r_{f}$, estimated auxiliary fuel inflation
rate
\%
13. $r_{e}, r_{0}$, estimated electric energy
14. $g, r_{m}$, estimated general inflation rate $\qquad$
\%
15. p, property tax rate (based on
decimal
16. $h$, insurance premium rate

17. Federal income tax rate for owner

18. State income tax rate for owner

19. $t$, effective income tax rate
\{i.e., (line 17) + (line 18)

- $[2 \times(1$ ine 17$) \times($ line 18) $]\}$
decimal

20. d, market discount rate decimal

## Solar System Cost Items

21. Installed cost (line $4 \times$ line 11) $\qquad$
22. Federal tax credit for solar ( $30 \%$ of first $\$ 2000$ plus $20 \%$ of next $\$ 8000$ on to total cost of system)

23. Downpayment (line $21 \times$ line 9 )
24. Amount of loan (line 21 - line 23)\$
25. Annual mortgage payment (multiply line 24 by annual mortgage rate from Figure 12-4) ..... \$/yr
26. $C_{f}$, first year cost of auxiliary heating (line $3 \times(1-1$ ine 5$) \times$ line 7 ) ..... \$/yr
27. First year property tax (1ine $21 x$ line 15) ..... \$/yr
28. First year insurance premium (line $21 \times$ line 16) ..... \$/yr
29. $C_{0}$, first year cost of operating the solar system (line $3 \times$ (a value between . 05 and .10) x line 6 ..... \$/yr
30. $C_{m}$, first year maintenance cost ..... \$/yr
Non-Solar System Cost Items31. $C_{f c}$, first year cost of fuel for non-solar system (line $3 \times$ line 7 )\$/yr
31. $C_{O C}$, first year cost of operating non-solar system (line $3 x$ $.01 \times$ line 6) ..... \$/yr

## LIFE-CYCLE COST ANALYSIS

## Total Cost for Solar System

33. $n$, total years of analysis

34. A, collector area (line 4 of LCA-1)

35. L, annual heat load (line 3 of LCA-1)

36. F, fraction of annual heat provided by the solar system (line 5 of LCA-1)
37. $P / X(d, g, n)$ (See Tables 12-1 through 12-6)

38. $P / X(d, 0, m)$ (See Tables 12-1 through 12-6)
39. $P / X(i, 0, m)$ (See Tables $12-1$
through $12-6$ )
40. $P / X(d, i, m)$ (See Tables 12-1 through 12-6)

41. $P / X(0, i, m)$ (see Tables $12-1$ through 12-6) $\qquad$
42. $(t)\left[\frac{P / X(d, i, m)}{P / X(0, i, m)}\right]=\left(\frac{\text { ine } 12 \times \text { line } 40}{\text { line } 41}\right)$
43. $(1-t)\left[\frac{P / X}{P / X(i, 0, m)}\right]=\left[\frac{(1-1 \text { ine 19) } x(\text { line } 38)}{\text { line } 41}\right]$
44. Add line 42 and line 43
45. 1 - $\alpha$ (1-1ine 9)
46. Multiply: line $44 \times$ line 45
47. (1-t)(p) +h $\quad(1-$ line 19)(line 15) + (line 16)
48. Multiply: line $47 \times$ line 37
49. $E_{1}=($ line 9) + (line 48) + (line 46)
50. $E_{0}=P / X\left(d, r_{0}, n\right)=$ (see Tables

12-1 through 12-6)
51. $E_{m}=P / X\left(d, r_{m}, n\right)$ (see Tables 12-1
through 12-6)
52. $E_{f}=P / X\left(d, r_{f}, n\right)$ (See Tables $12-1$
through 12-6)
53. $(A)\left(C_{a}\right)\left(E_{\eta}\right)=(l i n e ~ 34 \times$ line $11 \times$ line 49) $\square$
54. $\quad\left(C_{0} E_{0}=\right.$ (line $29 \times$ line 50 )

55. $\quad C_{m} E_{m}=$ (line $30 \times$ line 51 )



(1-1ine 36 ) $\times$ line $35 \times$ line $7 \times$ line 52
57. $\mathrm{C}_{\mathrm{T}}=$ line $53+$ line $54+$ line $55+$ line $56-1$ ine 22


Total Cost for Non-Solar System
58. $C_{o c} E_{0}=$ line $32 \times$ line 50
59. $\quad L c_{f c} E_{f}=\begin{aligned} & \text { line } 35 \times \text { line } 7 \times \text { line } 52 \\ & \text { (maintenance cost neglected) }\end{aligned}$

60. $C_{T C}=$ line $58+$ line 59


Present Value of Life-Cycle Cost Savings With Solar System
61. Savings $=($ line $60-1$ ine 57)


## WORKSHEET LCA- 3

In Worksheet LCA-3, column [1] is the year into the future for which the analysis may be made. A reasonable economic analysis can be made for 15 to 20 years into the future.

Column [2] is the annual mortgage payment (see Worksheet LCA-1, line 25). If the mortgage payment is a fixed annual amount, the payment for all future years would be the same as the first year,

Column [3] is the years remaining on the mortgage at the beginning of the year. The worksheet is for a 20 -year mortgage.

Column [4] is the fraction of the mortgage payment which is paid as interest. The fraction decreases with increasing years and may be determined from Figure 12-5 for the particular interest rate of the mortgage.

Column [5] is the portion of the mortgage which is paid as interest and is the product of column [2] times column [4].

Column [6] is auxiliary fuel cost. Because fuel cost is expected to increase, the first year fuel cost should be increased in subsequent years. The first year fuel cost is the amount on line 26, Worksheet LCA-1. The second year fuel cost is determined by multiplying the first year cost by $\left(1+r_{f}\right)$, (for $r_{f}$ see line 12 of Worksheet LCA-1). For example, if the first year fuel cost is $\$ 400$ and the fuel inflation rate is 7 percent, the second year cost is $(\$ 400 \times 1.07 \Rightarrow \$ 428$. The fuel cost for each succeeding year is determined by multiplying the previous year by (1 + fuel inflation rate). Note that the inflation rate may be changed for each year.

Column [7] is the annual property tax. The first year tax is calculated on line 27 on Worksheet LCA-1 and succeeding years can be escalated by the general inflation rate, g.

Column [11] is the income tax savings calculated by the product of the effective tax rate (on line 19 of Worksheet of LCA-1) and the sum of annual interest paid, in column [5], plus property taxes, column [7].

Column [12] is the annual expense of solar system and is determined by: Column [2] + column [6] + column [7] - column [8] + column [9] + column [10] - column [11]. The first year cash flow is calculated by adding the down payment and subtracting the federal tax credit. .

LIFE CYCLE COST ANALYSIS
CASH FLOW
A. Mortgage interest rate $\qquad$ B. Auxiliary fuel inflation rate $\qquad$ decima 1 C. General inflation rate $\qquad$ decimal

Collector area $\qquad$ Solar fraction of total load (see Worksheet LCA-1, line 5)

System Cost \$ Down Payment \$ $\qquad$ Federal Tax Credit \$ \$

| [1] | [2] | [3] | [4] | [5] | [6] | [7] | [8] | [9] | [10] | [11] | [12] |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Year | Annual Mortgage Payment | Years <br> Left on Mortgage | Frac. of Mortgage as Interest | Interest Paid | Auxiliary Fuel Cost | Property Tax | Insurance | Operating Cost | Maintenance Cost | Income Tax Savings | Expense <br> with <br> Solar |
| 1 |  | 20 |  |  |  |  |  |  |  |  | * |
| 2 |  | 19 |  |  |  |  |  |  |  |  |  |
| 3 |  | 18 |  |  |  |  |  |  |  |  |  |
| 4 |  | 17 |  |  |  |  |  |  |  |  |  |
| 5 |  | 16 |  |  |  |  |  |  |  |  |  |
| 6 |  | 15 |  |  |  |  |  |  |  |  |  |
| 7 |  | 14 |  |  |  |  |  |  |  |  |  |
| 8 |  | 13 |  |  |  |  |  |  |  |  |  |
| 9 |  | 12 |  |  |  |  |  |  |  |  |  |
| 10 |  | 11 |  |  |  |  |  |  |  |  |  |
| 11 |  | 10 |  |  |  |  |  |  |  |  |  |
| 12 |  | 9 |  |  |  |  |  |  |  |  |  |
| 13 |  | 8 |  |  |  |  |  |  |  |  |  |
| 14 |  | 7 |  |  |  |  |  |  |  |  |  |
| 15 |  | 6 |  |  |  |  |  |  |  |  |  |
| 16 |  | 5 |  |  |  |  |  |  |  |  |  |
| 17 |  | 4 |  |  |  |  |  |  |  |  |  |
| 18 |  | 3 |  |  |  |  |  |  |  |  |  |
| 19 |  | 2 |  |  |  |  |  |  |  |  |  |
| 20 |  | 1 |  |  |  |  |  |  |  |  |  |

Annual mortgage payment from LCA-1, line 25
See Figure 12-5
[5] Column [2] x column [4]
6] First year cost from LCA-1, line 26
Second and future years: (previous year cost) $\times(1+$ fuel inflation rate)
[7] See line 27, LCA-1
Second and future years:
(previous year cost) x ( $1+$ general inflation rate)
[8] See line 28, LCA-1 (and use general inflation rate)
[9] First year cost see Line 29, LCA-1 Second and future years:
(previous year cost) $\times(1+$ fuel inflation rate)
[10] First year cost see line 30, LCA-1
Second and future years:
(previous year cost) $x(1+$ general inflation rate)
[11] \{Column [5] + Column [7]\} x line 19, LCA-1
[12] [2] +66$]+[7]+[8]+[9]+[10]-[11]$
[12] For first year, add down payment and subt act federal tax credit

WORKSHEET LCA-4
Worksheet LCA-4 is used to compare life cycle and cash flow analyses for solar and non-solar systems.

Column [1] is the year of analysis.
Column [2] is the total fuel and operating cost for the non-solar system. The first year cost is the total of lines 31 and 32 on Worksheet LCA-1. The costs in succeeding years are determined by multiplying the cost of fuel for the previous year ( $1+r_{f}$ ) and the cost for operation for the previous year by $\left(1+r_{e}\right)$.

Column [3] is the cumulative annual cash flow for the non-solar system.

Column [4] is the present worth factor, determined from Table 12-7.
Column [5] is the present worth of the annual cost for a non-solar system.

Column [6] is the annual cost of the solar system, transferred from columin [12] of Worksheet LCA-3.

Column [7] is the cumulative annual cash flow for the solar system.

Column [8] is the present value of the annual cost of the solar system determined by multiplying column [6] by column [4].

Column [9] is the present worth of savings with a solar system and is determined by column [5] - column [8].

Column [10] is the cumulative present worth of savings with a solar system and is the running sum of column [9].

Column [11] is the cumulative savings in cash flow and is determined by column [3] - column [7].

LIFE-CYCLE COST ANALYSIS
CASH FLOW AND PRESENT WORTH SUMMARIES

| [1] | [2] | [3] | [4] | [5] | [6] | [7] | [8] | [9] | [10] | [11] |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | NON-SOLAR SYSTEM |  |  |  | SOLAR SYSTEM |  |  |  |  |  |
|  |  | $\mathrm{d}=$ |  |  | Collector Area __ft ${ }^{2}$ |  |  |  |  |  |
| Year | Fuel plus Operating Expenses | Cumulative Expenses | $\begin{aligned} & \text { Present } \\ & \text { Worth } \\ & \text { Factor } \end{aligned}$ | Present Worth of Annual Cost | Expense with Solar System | Cumulative Expenses | Present Worth of Annual Cost | Present Worth of Savings | Cumulative Present Worth of Savings | Cumulative Savings (cash flow) |
| 1 |  |  |  |  |  |  |  |  |  |  |
| 2 |  |  |  |  |  |  |  |  |  |  |
| 3 |  |  |  |  |  |  |  |  |  |  |
| 4 |  |  |  |  |  |  |  |  |  |  |
| 5 |  |  |  |  |  |  |  |  |  |  |
| 6 |  |  |  |  |  |  |  |  |  |  |
| 7 |  |  |  |  |  |  |  |  |  |  |
| 8 |  |  |  |  |  |  |  |  |  |  |
| 9 |  |  |  |  |  |  |  |  |  |  |
| 10 |  |  |  |  |  |  |  |  |  |  |
| 11 |  |  |  |  |  |  |  |  |  |  |
| 12 |  |  |  |  |  |  |  |  |  |  |
| 13 |  |  |  |  |  |  |  |  |  |  |
| 14 |  |  |  |  |  |  |  |  |  |  |
| 15 |  |  |  |  |  |  |  |  |  |  |
| 16 |  |  |  |  |  |  |  |  |  |  |
| 17 |  |  |  |  |  |  |  |  |  |  |
| 18 |  |  |  |  |  |  |  |  |  |  |
| 19 |  |  |  |  |  |  |  |  |  |  |
| 20 |  |  |  |  |  |  |  |  |  |  |

2] First year cost, add lines 31 and 32 of LCA-1 Second and future years:
(previous year cost) $\times(1+$ fuel inflation rate)
[3] Accumulate column [2]
[4] See Table 12-7
5] Column [2] x column [4]
[6] Column [12], Worksheet LCA-3
[7] Accumulate column [6]
[8] Column [6] x column [4
[9] Column [5] x column [8]
[10] Running sum of column [9]
[11] Column [3]-column [7]

## EXAMPLE 12-4

Determine the life-cycle cost of the liquid-heating solar system of Example 12-1 with 500 square feet of collectors. Assume the following data apply:

1. $F$, annual solar fraction is 0.68
2. Seven percent of the solar energy collected is required to operate the pumps and control the system
3. $\mathrm{c}_{\mathrm{e}}$, current electricity cost is $3.5 \mathrm{\$} / \mathrm{kWh}$
4. A 20 -year loan at 9 percent is obtainabie with 20 percent down
5. Cost of solar system is $\$ 20 / \mathrm{ft}^{2}$ for collector-related costs plus $\$ 3,000$ for costs not related to collector area. In terms of collector area, the cost is $20+(3000 / 500)$ or $26 \$ / \mathrm{ft}^{2}$ of collector
6. $r_{f}$, fuel inflation rate is 10 percent
7. g, general inflation rate is 6 percent
8. Homeowners insurance is available for a premium of 0.3 percent of insured value
9. Property tax is levied on an assessed value which is 30 percent of market and the mil levy is $\mathbf{2 0 0}$. This is the equivalent of a property tax levied as ( $0.30 \times 0.1$ ), or 3 percent of market value
10. The owner's federal income tax rate is 32 percent and the solar tax is 8 percent
11. Maintenance cost is $\$ 100$ for first year
12. Use a market discount rate of 10 percent

## Project Sunbody Residence

Building Data (see Worksheet B)

1. Annual space heating load 108,3 MMBtu/yr
2. Annual DHW heating load
21.0 MMBtu/yr
3. Total H and DHW load (add lines 1 \& 2) 129.3 MMBtu/yr

Solar System Data
4. Collector area
$500 \mathrm{ft}^{2}$
5. Fraction of annual heating load supplied from solar
0.68 decimal

## Energy Prices

6. $\quad c_{e}$, current energy cost for electricity
7. $c_{f}, c_{f c}$, current cost of fuel 1
(use Figure 12-1 or 12-2)
Terms of Loan
8. $m$, term of the loan for solar system

9. $\alpha$, downpayment $20 \%$
10. i, interest rate on loan $9 \%$

## Economic Data

11. $C_{a}$, installed cost of solar system per
$26 \quad \$ / f t^{2}$
12. $r_{f}$, estimated auxiliary fuel inflation rate

13. $r_{e}, r_{0}$, estimated electric energy
14. $g, r_{m}$ estimated general inflation

15. p, property tax rate (based on market value)
0.03 decimal
0.003 decimal
16. $h$, insurance premium rate
0.32 decimal
17. Federal income tax rate for owner
18. State income tax rate for owner
0.08 decimal
19. $t$, effective income tax rate
\{i.e., (line 17) + (line 18)

- [2 x (line 17) x (line 18) $]\}$

| 0.35 |
| :---: |
| 0.10 decimal |

10.25 \$/MMBtu
10.25 \$/MMBtu

Solar System Cost Items
21. Installed cost (line $4 \times$ line 11)
$13,000 \$$
22. Federal tax credit for solar (30\% of first $\$ 2000$ plus $20 \%$ of next $\$ 8000$ on to total cost of system)
23. Downpayment (line $21 \times$ line 9)
24. Amount of loan (line 21 - line 23)
25. Annual mortgage payment (multiply line 24 by annual mortgage rate from Figure 12-4)
$\frac{2,200 \$}{2,600 \$}$
$10,400 \$$
1, 144 \$/yr
26. $C_{f}$, first year cost of auxiliary heating (line $3 \times(1-1$ in 5$) \times$ line 7 )

424 \$/yr
27. First year property tax (line 21 x line 15)
$390 \$ / y r$
28. First year insurance premium (line $21 \times$ line 16)
$39 \$ / \mathrm{yr}$
29. $C_{0}$, first year cost of operating the solar system (line $3 \times$ (a value between . 05 and .10) $\times$ line 6
30. $C_{m}$, first year maintenance cost
$m^{\prime}$ (estimate)

$100 \$ 1 \mathrm{yr}$

## Non-Solar System Cost Items

31. $C_{f c}$, first year cost of fuel for nonsolar system (line $3 \times$ line 7)

1,325\$/yr
32. $C_{\text {OC }}$, first year cost of operating non-solar system (line $3 x$ $.01 \times$ line 6)

## LIFE-CYCLE COST ANALYSIS

Total Cost for Solar System

## 33. $n$, total years of analysis

34. A, collector area (line 4 of LCA-1)
35. L, annual heat load (1 line 3 of LCA-1)
20 yrs
$500 \mathrm{ft}^{2}$
129.3 MMBtu
36. F, fraction of annual heat provided
by the solar system (line 5 of
LCA-1)
. 68 decimal
37. $P / X(d, g, n)$ (See Tables 12-1 through 12-6)
13.082
38. $P / X(d, 0, m)$ (See Tables 12-1 through 12-6)
39. $P / X(i, 0, m)$ (See Tables 12-1 through 12-6)
8.514
9.176
40. $P / X(d, i, m)$ (See Tables $12-1$ through 12-6)
41. $P / X(0, i, m)$ (see Tables 12-1 through 12-6)
16.710

51,518
42. $(t)\left[\frac{P / X(d, i, m)}{P / X(0, i, m)}\right]=\left(\frac{\text { line } 12 \times 1 \text { ne } 40}{\text { line } 41}\right)$
0.114
43. $(1-t)\left[\frac{P / X(d, 0, m)}{P / X(i, 0, m)}\right]=\left[\frac{(1-1 \text { ind 19) } x(1 \text { line } 38)}{\text { line } 41}\right]$
0.603
44. Add line 42 and line 43
45. 1- -1 - line 9)
46. Multiply: line $44 \times$ line 45
0.717
47. (1-t)(p) +h
48. Multiply: line $47 \times$ line 37
49. $E_{1}=($ line 9$)+(1$ ne 48) + (line 46)
$\frac{0.8}{0.574}$
0.0225
50. $E_{0}=P / X\left(d, r_{0}, n\right)=$ (see Tables

12-1 through 12-6)
18.182
51. $E_{m}=P / X\left(d, r_{m}, n\right)$ (see Tables 12-1 through 12-6)
13.082
52. $E_{f}=P / X\left(d, r_{f}, n\right)$ (See Tables 12-1 through 12-6) 18.182
53. $(A)\left(C_{a}\right)\left(E_{1}\right)=($ line $34 \times$ line $11 \times$ line 49) $13,884-\$$
54. $\quad\left(C_{0} E_{0}=(l i n e 29 \times\right.$ line 50$)$
55. $\quad C_{m} E_{m}=(1$ line $30 \times$ line 51)

56. $(1-F)(L)\left(c_{f}\right)\left(E_{f}\right)=(.32)(129.3)(10.26)(18.182)$ $\qquad$ ( 1-line 36 ) $\times$ line $35 \times$ line $7 \times$ line 52
57. $C_{T}=1$ line $53+$ line $54+$ line $55+$ line $56-1$ line 22

```
21,867_$
```

Total Cost for Non-Solar System
58. $C_{O C} E_{0}=$ line $32 \times$ line 50

59. $L C_{f c} E_{f}=$ line $35 \times$ line $7 \times$ line 52

60. $C_{T C}=$ line $58+$ line 59

$$
24,588, \$
$$

Present Value of Life-Cycle Cost Savings With Solar System
61. Savings $=($ line $60-1$ line 57)

$$
2,721 \$
$$

LIFE CYCLE COST ANALYSIS
CASH FLOW
A. Mortgage interest rate 9 decima
B. Auxiliary fuel inflation rate_lo decimal
C. General inflation rate $\quad 6$ decimal
$\qquad$

500
$\mathrm{ft}^{2}$
Solar fraction of total load . 68 decimal
(see Worksheet LCA-1, line 5)

System Cost \$13,000 Down Payment \$2,600 Federal Tax
Credit
$\$ 2,200$

| [1] | [2] | [3] | [4] | [5] | [6] | [7] | [8] | [9] | [10] | [11] | [12] |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Year | $\left\lvert\, \begin{array}{c\|} \text { Annual } \\ \text { Mortgage } \\ \text { Payment } \end{array}\right.$ | Years Left on Mortgage | Frac. of Mortgage as Interest | Interest Paid | $\begin{aligned} & \text { Aukiliary } \\ & \text { Fuel } \\ & \text { Cost } \end{aligned}$ | Property Tax | Insurance | $\begin{aligned} & \text { Operating } \\ & \text { Cost } \end{aligned}$ | Maintenance Cost | $\begin{aligned} & \text { Income } \\ & \text { Tax } \\ & \text { Savings } \end{aligned}$ | Expense with Solar |
| 1 | 1144 | 20 | 820 | 938 | 424 | 390 | 39 | 64 | 100 | 465 | 2096 * |
| 2 | 1144 | 19 | 805 | 921 | 466 | 413 | 41 | 10 | 106 | 467 | 1773 |
| 3 | 1144 | 18 | 185 | 898 | 513 | 438 | 44 | 17 | 112 | 468 | 1860 |
| 4 | 1144 | 17 | 765 | 815 | 564 | 464 | 46 | 85 | 119 | 469 | 1953 |
| 5 | 1144 | 16 | 745 | 852 | 621 | 492 | 49 | 94 | 126 | 470 | 2056 |
| 6 | 1144 | 15 | . 720 | 824 | 683 | 522 | 52 | 103 | 134 | 411 | 2167 |
| 7 | 1144 | 14 | . 700 | 801 | 751 | 553 | 55 | 113 | 142 | 474 | 2284 |
| 8 | 1144 | 13 | 670 | 166 | 826 | 586 | 59 | 125 | 150 | 413 | 2417 |
| 9 | 1144 | 12 | 640 | 132 | 909 | 622 | 62 | 137 | 59 | 474 | 2559 |
| 10 | 1144 | 11 | 610 | 698 | 000 | 659 | 66 | 151 | 169 | 475 | 2714 |
| 17 | 1144 | 10 | 575 | 658 | 1100 | 698 | 70 | 166 | 179 | 475 | 2882 |
| 12 | 1144 | 9 | 540 | 618 | 1210 | 140 | 14 | 183 | 190 | 475 | 3066 |
| 13 | 1144 | 8 | 500 | 572 | 1331 | 785 | 78 | 201 | 201 | 475 | 3265 |
| 14 | 1144 | 7 | 450 | 515 | 1464 | 832 | 83 | 221 | 213 | 471 | 3486 |
| 15 | 1144 | 6 | . 400 | 458 | 1610 | 882 | 88 | 243 | 226 | 469 | 3724 |
| 16 | 1144 | 5 | . 250 | 400 | 1771 | 935 | 93 | 261 | 240 | 467 | 3183 |
| 17 | 1144 | 4 | .290 | 332 | 1948 | 991 | 99 | 294 | 254 | 463 | 4267 |
| 18 | 1144 | 3 | . 230 | 263 | 2143 | 1050 | 105 | 323 | 269 | 460 | 4574 |
| 19 | 1144 | 2 | .160 | 183 | 2357 | 1113 | 111 | 356 | 285 | 454 | 4912 |
| 20 | 1144 |  | . 085 | 97 | 2593 | 1080 | 118 | 391 | 303 | 447 | 5282 |

2] Annual mortgage payment from LCA-1, line 25
[4] See Figure 12-5
[5] Column [2] x column [4]
[6] First year cost from LCA-1, line 26 Second and future years: (previous year cost) $\times(1+$ fue 1 inflation rate)
[7] See line 27, LCA-1
Second and future years:
(previous year cost) $x(1+$ general inflation rate)
[8] See line 28, LCA-1 (and use general inflation rate)
[9] First year cost see Line 29, LCA-1
Second and future years:
(previous year cost) $\times(1+$ fuel inflation rate)
[10] First year cost see line 30, LCA-1
Second and future years:
(previous year cost) $\times(1+$ general inflation rate)
[11] \{Column [5] + Column [7]\} x line 19, LCA-1
12] [2]+[6]+[7]+[8]+[9]+[10]-[11]
For first year, add down payment and subtract federal tax credit

LIFE-CYCLE COST ANALYSIS
CASH FLOW AND PRESENT WORTH SUMMARIES

| [1] | [2] | [3] | [4] | [5] | [6] | [7] | [8] | [9] | [10] | [11] |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | NON-SOLAR SYSTEM |  |  |  | SOLAR SYSTEM |  |  |  |  |  |
|  |  | $d=0.10$ |  |  | Collector Area $500 \mathrm{ft}^{2}$ |  |  |  |  |  |
| Year | Fuel plus Operating Expenses | Cumulative Expenses | Present Worth Factor | Present Worth of Annual Cost | Expense with Solar System | Cumulative Expenses | Present Worth of Annual Cost | Present Worth of Savings | Cumulative Present Worth of Savings | Cumulative Savings (cash flow) |
| 1 | 1352 | 352 | 909 | 1229 | 2096 | 2096 | 1905 | - 676 | -676 | -744 |
| 2 | 1487 | 2839 | . 826 | 1228 | 1773 | 3869 | 464 | - 236 | -912 | $-1030$ |
| 3 | 1636 | 4475 | .751 | 1229 | 1860 | 5729 | 1397 | - 168 | - 1080 | -1254 |
| 4 | 1800 | 6275 | 683 | 1229 | 1953 | 7682 | 1334 | -105 | -1185 | -1407 |
| 5 | 1979 | 8254 | . 621 | 1229 | 2056 | 9738 | 1271 | - 48 | $-1233$ | $-1484$ |
| 6 | 2177 | 10,431 | 564 | 1228 | 2167 | 11,905 | 1222 | 6 | - 1227 | - 1474 |
| 7 | 2395 | 12,826 | 513 | 1229 | 2284 | 14,189 | 1172 | 51 | - 1.70 | $-1363$ |
| 8 | 2635 | 15,461 | 467 | 1231 | 2417 | 16,606 | 1129 | 102 | -1068 | $-1145$ |
| 9 | 2898 | 18, 359 | 424 | 1229 | 2554 | 19,165 | 1085 | 144 | - 924 | - 806 |
| 10 | 3188 | 21,547 | 386 | 1231 | 2114 | 21, 819 | 1048 | 183 | -741 | -832 |
| 11 | 3507 | 25,054 | . 350 | 1227 | 2882 | $24+761$ | 1009 | 218 | -523 | 293 |
| 12 | 3857 | 28,911 | 319 | 1230 | 3066 | 27,827 | 978 | 252 | -271 | 1084 |
| 13 | 4243 | 33, 154 | 290 | 1230 | 3265 | 31,092 | 947 | 283 | 12 | 2.062 |
| 14 | 41067 | 37, 821 | 263 | 1227 | 3486 | 34,578 | 917 | 310 | 322 | 3243 |
| 15 | 5134 | 42,955 | 239 | 1227 | 3724 | 38,302 | 890 | 337 | 659 | 4653 |
| 16 | 5648 | 48,603 | 218 | 1231 | 3983 | 42,285 | 868 | 363 | 1022 | 6318 |
| 17 | 6212 | 54,815 | 198 | 1230 | 4267 | 46,552 | 845 | 385 | 1407 | 8263 |
| 18 | 6834 | 61,649 | 180 | 1230 | 4574 | 51,126 | 823 | 407 | 1814 | 10523 |
| 19 | 7517 | 69,166 | 1.164 | 1233 | 4912 | 56, 038 | 806 | 427 | 2241 | 13128 |
| 20 | 8269 | 17,435 | .149 | 1232 | 5282 | 61,320 | 781 | 445 | 2686 | 16115 |

[2] First year cost, add lines 31 and 32 of LCA-1 Second and future years:
(previous year cost) $\times(1+$ fue 1 inflation rate)
[3] Accumulate column [2]
[4] See Table 12-7
[5] Column [2] $x$ column [4]
[6] Column [12], Worksheet LCA-3
[7] Accumulate column [6]
[8] Column [6] x column [4]
9] Column [5] x column [8]
[10] Running sum of column [9]
[11] Column [3] - column [7]

## Project

$\qquad$
Building Data (see Worksheet B)1. Annual space heating loadMMBtu/yr
2. Annual DHW heating load3. Total H and DHW load (add lines 1 \& 2)Solar System Data
4. Collector area

$\qquad$ ..... $f t^{2}$5. Fraction of annual heating loadsupplied from solardecimal
Energy Prices
6. $c_{e}$, current energy cost for electricity (use Figure 12-2) ..... $\$ / k W h r$\$/MMBtu
7. $c_{f}, c_{f c}$, current cost of fuel (use Figure 12-1 or 12-2)\$/MMBtu
Terms of Loan8. $m$, term of the loan for solar system

$\qquad$ ..... yrs
9. $\alpha$, downpayment

$\qquad$
\%
10. i , interest rate on loan

$\qquad$
\%
Economic Data
11. $C_{a}$, installed cost of solar system per unit area$\$ / f t^{2}$
12. $\quad r_{f}$, estimated auxiliary fuel inflation rate
decimal
_\%
13. $r_{e}, r_{0}$, estimated electric energy_ $\%$\%
14. $g, r_{m}$, estimated general inflation ..... \%
15. p, property tax rate (based on market value)
decimal
16. $h$, insurance premium rate ..... decimal
17. Federal income tax rate for ownerdecimal
18. State income tax rate for ownerdecimal
19. $t$, effective income tax rate\{i.e., (line 17) + (line 18)- [2 x (line 17) $\times($ line 18) $]\}$decimal
20. d, market discount ratedecimal

## Solar System Cost Items

21. Installed cost (line $4 \times$ line 11) $\qquad$ \$
22. Federal tax credit for solar ( $30 \%$ of first $\$ 2000$ plus $20 \%$ of next $\$ 8000$ on to total cost of system) $\qquad$
23. Downpayment (line $21 \times$ line 9)
24. Amount of loan (line 21 - line 23)
25. Annual mortgage payment (multiply line 24 by annual mortgage rate from Figure 12-4) \$/yr
26. $C_{f}$, first year cost of auxiliary heating (line $3 \times(1-1$ ine 5) $\times$ line 7) \$/yr
27. First year property tax (line 21 x line 15)
\$/yr
28. First year insurance premium (Iine $21 \times$ line 16)
\$/yr
29. $C_{0}$, first year cost of operating the solar system (line $3 \times$ (a value between . 05 and .10) x line 6
\$/yr
30. $C_{m}$, first year maintenance cost

Non-Solar System Cost Items
31. $C_{f c}$, first year cost of fuel for nonsolar system (line $3 \times$ line 7)
\$/yr
32. $C_{C C}$, first year cost of operating non-solar system (line $3 x$ $.01 \times$ line 6)

Worksheet LCA-2
Sheet 1 of 2

## LIFE-CYCLE COST ANALYSIS

Total Cost for Solar System
33. $n$, total years of analysis

34. A, collector area (line 4 of LCA-1)
35. L, annual heat load (line 3 of LCA-1)

36. F, fraction of annual heat provided
by the solar system (line 5 of LCA-1)

37. $\mathrm{P} / \mathrm{X}(\mathrm{d}, \mathrm{g}, \mathrm{n})$ (See Tables 12-1 through 12-6)
38. $P / X(d, 0, m)$ (See Tables 12-1 through 12-6)
 through 12-6)
40. $P / X(d, i, m)$ (See Tables 12-1 through 12-6)
$\qquad$
MMBtu (Ca

P/X (0,i,m) (see Tables 12-1 through 12-6) $\qquad$
42. $(t)\left[\frac{P / X(d, i, m)}{P / X(0, i, m)}\right]=\left(\frac{\text { ine } 12 \times \text { line } 40}{\text { line } 47}\right)$
43. $(1-t)\left[\frac{P / X(d, 0, m)}{P / X(i, 0, m)}\right]=\left[\frac{(1-1 \text { ine } 19) \times(\text { line } 38)}{\text { line } 41}\right]$

44. Add line 42 and line 43
45. 1- $\alpha$ (1 - line 9) $\qquad$
46. Multiply: line $44 \times$ line 45 $\qquad$
47. $(1-t)(p)+h$
(1 - line 19)(line 15) + (line 16) $\qquad$
48. Multiply: line 47 x line 37
49. $E_{1}=(l i n e ~ 9)+(l i n e ~ 48)+(1 i n e ~ 46)$
50. $E_{0}=P / X\left(d, r_{0}, n\right)=$ (see Tables

12-1 through 12-6)
51. $\varepsilon_{m}=P / X\left(d, r_{m}, n\right)$ (see Tables 12-1 through 12-6)
52. $E_{f}=P / X\left(d, r_{f}, n\right)$ (See Tables 12-1 through 12-6)
53. $(A)\left(C_{a}\right)\left(E_{1}\right)=($ line $34 \times$ line $11 \times$ line 49) $\square$
54. $\quad\left(C_{0} E_{0}=\right.$ (line $29 \times$ line 50 )
55. $\quad C_{m} E_{m}=($ line $30 \times$ line 51 )
56. $(1-F)(L)\left(c_{f}\right)\left(E_{f}\right)=(\ldots \quad)(\ldots)(\ldots)(\ldots) \quad \$$ (1 - line 36 ) $\times$ line $35 \times$ line $7 \times$ line 52
57. $C_{T}=$ line $53+$ line $54+$ line $55+$ line 56 - line 22


Total Cost for Non-Solar System
58. $C_{O C} E_{0}=$ line $32 \times$ line 50
59. $L c_{f c} E_{f}=\underset{\text { (maintenance cost } 35 \times \text { line } 7 \text { lected) }}{\text { (mane }}$
60. $C_{T C}=$ line $58+$ line 59


Present Value of Life-Cycle Cost Savings With Solar System
61. Savings $=($ line $60-1$ ine 57)


LIFE CYCLE COST ANALYSIS
CASH FLOW
A. Mortgage interest rate $\qquad$ decimal B. Auxiliary fuel inflation rate
$\qquad$ decimal decimal

## Collector area <br> $\qquad$ Solar fraction of total load (see Worksheet LCA-1, line 5)

System Cost \$ Down Payment \$ Federal Tax Credit \$

| [1] | [2] | [3] | [4] | [5] | [6] | [7] | [8] | [9] | [10] | [11] | [12] |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Year | Annuai i Mortgage Payment | Years Left on Mortgage | Frac. of Mortgage as Interest | Interest Paid | $\begin{aligned} & \text { Auxiliary } \\ & \text { Fuel } \\ & \text { Cost } \end{aligned}$ | Property Tax | Insurance | Operating Cost | Maintenance Cost |  | Expense with Solar |
| 1 |  | 20 |  |  |  |  |  |  |  |  | * |
| 2 |  | 19 |  |  |  |  |  |  |  |  |  |
| 3 |  | 18 |  |  |  |  |  |  |  |  |  |
| 4 |  | 17 |  |  |  |  |  |  |  |  |  |
| 5 |  | 16 |  |  |  |  |  |  |  |  |  |
| 6 |  | 15 |  |  |  |  |  |  |  |  |  |
| 7 |  | 14 |  |  |  |  |  |  |  |  |  |
| 8 |  | 13 |  |  |  |  |  |  |  |  |  |
| 9 |  | 12 |  |  |  |  |  |  |  |  |  |
| 10 |  | 11 |  |  |  |  |  |  |  |  |  |
| 11 |  | 10 |  |  |  |  |  |  |  |  |  |
| 72 |  | 9 |  |  |  |  |  |  |  |  |  |
| 13 |  | 8 |  |  |  |  |  |  |  |  |  |
| 14 |  | 7 |  |  |  |  |  |  |  |  |  |
| 15 |  | 6 |  |  |  |  |  |  |  |  |  |
| 16 |  | 5 |  |  |  |  |  |  |  |  |  |
| 17 |  | 4 |  |  |  |  |  |  |  |  |  |
| 18 |  | 3 |  |  |  |  |  |  |  |  |  |
| 19 |  | 2 |  |  |  |  |  |  |  |  |  |
| 20 |  | 1 |  |  |  |  |  |  |  |  |  |

[2] Annual mortgage payment from LCA-1, line 25
[4] See Figure 12-5
[5] Column [2] x column [4]
[6] First year cost from LCA-1, line 26
Second and future years:
(previous year cost) $\times(1+$ fuel inflation rate)
[7] See line 27, LCA-1
Second and future years:
(previous year cost) x ( $1+$ general inflation rate)
[8] See line 28, LCA-1 (and use general inflation rate)
[9] First year cost see Line 29, LCA-1
Second and future years:
(previous year cost) $\times(1+$ fuel inflation rate)
[10] First year cost see line 30, LCA-1
Second and future years:
(previous year cost) $x$ ( $1+$ general inflation rate)
[11] \{Column [5] + Column [7]\} x line i9, LCA-1
[12] [2]+[6]+[7]+[8]+[9]+[10]-[11]
tax credit

LIFE-CYCLE COST ANALYSIS
CASH FLOW AND PRESENT WORTH SUMMARIES

| [1] | [2] | [3] | [4] | [5] | [6] | [7] | [8] | [9] | [10] | [11] |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | NON-SOLAR SYSTEM |  |  |  | SOLAR SYSTEM |  |  |  |  |  |
|  |  | $\mathrm{d}=$ |  |  | Collector Area ___ft ${ }^{2}$ |  |  |  |  |  |
| Year | Fue] plus Operating Expenses | Cumulative Expenses | Present Worth Factor | Present Worth of Annual Cost | Expense with Solar System | Cumulative Expenses | Present Worth of Annual Cost | Present Worth of Savings | Cumulative Present Worth of Savings | $\begin{aligned} & \text { Cumulative } \\ & \text { Savings } \\ & \text { (cash flow) } \end{aligned}$ |
| 1 |  |  |  |  |  |  |  |  |  |  |
| 2 |  |  |  |  |  |  |  |  |  |  |
| 3 |  |  |  |  |  |  |  |  |  |  |
| 4 |  |  |  |  |  |  |  |  |  |  |
| 5 |  |  |  |  |  |  |  |  |  |  |
| 6 |  |  |  |  |  |  |  |  |  |  |
| 7 |  |  |  |  |  |  |  |  |  |  |
| 8 |  |  |  |  |  |  |  |  |  |  |
| 9 |  |  |  |  |  |  |  |  |  |  |
| 10 |  |  |  |  |  |  |  |  |  |  |
| 11 |  |  |  |  |  |  |  |  |  |  |
| 12 |  |  |  |  |  |  |  |  |  |  |
| 13 |  |  |  |  |  |  |  |  |  |  |
| 14 |  |  |  |  |  |  |  |  |  |  |
| 15 |  |  |  |  |  |  |  |  |  |  |
| 16 |  |  |  |  |  |  |  |  |  |  |
| 17 |  |  |  |  |  |  |  |  |  |  |
| 18 |  |  |  |  |  |  |  |  |  |  |
| 19 |  |  |  |  |  |  |  |  |  |  |
| 20 |  |  |  |  |  |  |  |  |  |  |

[2] First year cost, add lines 31 and 32 of LCA-1 Second and future years: (previous year cost) $\times(1+$ fue 1 inflation rate)
[3] Accumulate column [2]
[4] See Table 12-7
[5] Column [2] x column [4]
[6] Column [12], Worksheet LCA-3
[7] Accumulate column [6]
[8] Column [6] x column [4]
[9] Column [5] x column [8]
[10] Running sum of column [9]
[11] Column [3] - column [7]
Building Data (see Worksheet B)

1. Annual space heating load

MMBtu/yr
2. Annual DHW heating load $\qquad$ MMBtu/yr
3. Total H and DHW load (add lines 1 \& 2) MMBtu/yr

## Solar System Data

4. Collector area $\qquad$
5. Fraction of annual heating load supplied from solar
decimal

## Energy Prices

6. $c_{e}$, current energy cost for electricity
(use Figure 12-2) $\$ / \mathrm{kWhr}$ $\qquad$
7. $c_{f}, c_{f c}$, current cost of fue 1
(use Figure 12-1 or 12-2) $\qquad$
Terms of Loan
8. $m$, term of the loan for solar system $\qquad$
9. $\alpha$, downpayment $\qquad$ \%
10. $i$, interest rate on loan $\qquad$ decimal

## Economic Data

11. $C_{a}$, installed cost of solar system per unit area
$\qquad$
12. $\quad r_{f}, \begin{aligned} & \text { estimated auxiliary fuel inflation } \\ & \text { rate }\end{aligned}$ $\qquad$
13. $r_{e}, r_{0}, \begin{aligned} & \text { estimated electric energy } \\ & \text { inflation }\end{aligned}$
14. $g, r_{m}$, estimated general inflation
$\qquad$
\%
15. p, property tax rate (based on market value)
decimal

## 16. $h$, insurance premium rate

$\qquad$
\%

## 17. Federal income tax rate for owner


18. State income tax rate for owner

19. $\quad t$, effective income tax rate $\quad \begin{aligned} & \{\text { i.e. (line 17) }+ \text { (line 18) } \\ & -[2 \times(\text { line 17) } \times(\text { line 18) ]\} }\end{aligned}$
decimal
20. d, market discount rate decimal

Solar System Cost Items
21. Installed cost (line $4 \times$ line 11) $\qquad$
22. Federal tax credit for solar (30\% of first $\$ 2000$ plus $20 \%$ of next $\$ 8000$ on to total cost of system)

23. Downpayment (line $21 \times$ line 9 )

24. Amount of loan (line 21 - line 23)

25. Annual mortgage payment (multiply line 24 by annual mortgage rate from Figure 12-4) $\qquad$
26. $C_{f}$, first year cost of auxiliary heating (line $3 \times(1-1$ ine 5$) \times$ line 7 ) $\qquad$ \$/yr
27. First year property tax (line 21 x line 15)

28. First year insurance premium (line $21 \times$ line 16)
\$/yr
29. $C_{0}$, first year cost of operating the solar system (line $3 \times$ (a value between .05 and .10) x line 6

30. $C_{m}$, first year maintenance cost (estimate)


Non-Solar System Cost Items
31. ${ }^{\text {C }}$ fc first year cost of fuel for nonsolar system (line $3 \times$ line 7)
\$/yr
32. $C_{o c}$, first year cost of operating non-solar system (line $3 x$ $.01 \times$ line 6)

## Project

Building Data (see Worksheet B)

1. Annual space heating load MMBtu/yr
2. Annual DHW heating load MMBtu/yr
3. Total H and DHW load (add lines $1 \& 2$ ) $\qquad$ MMBtu/yr

Solar System Data
4. Collector area $\qquad$
$f t^{2}$
5. Fraction of annual heating load supplied from solar
decimal
Energy Prices
6. $c_{e}$, current energy cost for electricity
\$/MMBtu
7. $c_{f}, c_{f c}, \begin{aligned} & \text { current cost of fuel } \\ & \text { (use Figure 12-1 or 12-2) }\end{aligned}$ \$/MMBtu

Terms of Loan
8. $m$, term of the loan for solar system $\square$
9. $\alpha$, downpayment $\qquad$ \%
10. i, interest rate on loan $\qquad$ \%
yrs
decima 1

## Economic Data

11. $C_{a}$, installed cost of solar system per
$\ldots / \mathrm{ft}^{2}$
12. $r_{f}$, estimated auxiliary fuel inflation $\qquad$
\%
13. $r_{e}, r_{0}$, estimated electric energy
14. $g, r_{m}$, estimated general inflation
$\qquad$ \%
15. p, property tax rate (based on
16. $h$, insurance premium rate decimal
17. Federal income tax rate for owner decimal
18. State income tax rate for owner decimal
19. $t$, effective income tax rate \{i.e., (line 17) + (line 18) - [2 x (line 17) $\times($ line 18) $]\}$
20. d, market discount rate decimal

Solar System Cost Items
21. Installed cost (line $4 \times$ line 11)

22. Federal tax credit for solar (30\% of first $\$ 2000$ plus $20 \%$ of next $\$ 8000$ on to total cost of system)
23. Downpayment (line $21 \times$ line 9)

24. Amount of loan (line 21 - line 23)
25. Annual mortgage payment (multiply line 24 by annual mortgage rate from Figure 12-4)
\$ \$/yr
26. $C_{f}$, first year cost of auxiliary heating (line $3 \times(1-1$ ine 5$) \times 1$ ine 7 )
 \$/yr
27. First year property tax (line $21 \times$ line 15)
28. First year insurance premium (line $21 \times$ line 16)
29. $C_{0}$, first year cost of operating the solar system (line $3 \times$ (a value between .05 and .10) x line 6 $\qquad$
30. $C_{m}$, first year maintenance cost (estimate)


Non-Solar System Cost Items
31. $C_{f c}$, first year cost of fuel for nonsolar system (line $3 \times$ line 7 )

32. $C_{o c}$, first year cost of operating non-solar system (line $3 x$ $.01 \times$ line 6) $\qquad$ \$/yr

## LIFE-CYCLE COST ANALYSIS

## Total Cost for Solar System

33. $n$, total years of analysis
34. A, collector area (line 4 of LCA-1)

35. L, annual heat load (line 3 of LCA-1) MMBtu
36. F, fraction of annual heat provided by the solar system (line 5 of LCA-1)
37. $P / X(d, g, n)$ (See Tables 12-1
through 12-6)
$\qquad$
$\qquad$
38. $P / X(d, 0, m)$ (See Tables 12-1 through 12-6)

39. $P / X(i, 0, m)$ (See Tables 12-1 through 12-6)
40. $P / X(d, i, m)$ (See Tables 12-1 through 12-6) $\qquad$
41. $P / \times(0, i, m)$ (see Tables 12-7 through 12-6) $\qquad$
42. $(t)\left[\frac{P / X}{P / X(0, i, m)}\right]=\left(\frac{\text { line } 12 \times 1 \text { ine } 40}{\text { line } 41}\right)$
43. $(1-t)\left[\frac{P / X(d, 0, m)}{P / X(i, 0, m)}\right]=\left[\frac{(1-1 \text { ine 19) } \times(\text { line 38) }}{\text { line } 41}\right]$
44. Add line 42 and line 43
45. $1-\alpha$ (1-1ine 9)
46. Multiply: line $44 \times$ line 45
$\qquad$
47. $(1-t)(p)+h$

$$
(1-\text { line } 19)(\text { line } 15)+(\text { line } 16)
$$

$\qquad$
48. Multiply: line $47 \times$ line 37
49. $\mathrm{E}_{\mathrm{\gamma}}=$ (line 9) + (line 48) + (line 46)
50. $E_{0}=P / X\left(d, r_{0}, n\right)=$ (see Tables 12-1 through 12-6)
51. $E_{m}=P / X\left(d, r_{m}, n\right)$ (see Tables 12-1 through 12-6)
52. $E_{f}=P / X\left(d, r_{f}, n\right)$ (See Tables 12-1 through 12-6)
53. $(A)\left(C_{a}\right)\left(E_{\eta}\right)=(1$ ine $34 \times$ line $11 \times$ line 49)

54. $\left(C_{0} E_{0}=\right.$ (line $29 \times$ line 50 )

55. $\quad C_{m} E_{m}=($ line $30 \times$ line 51)

56. $(1-F)(L)\left(c_{f}\right)\left(E_{f}\right)=(\ldots)(\ldots)(\ldots)(\ldots) \quad \$$

$$
(1-1 \text { ine } 36) \times \text { line } 35 \times \text { line } 7 \times \text { line } 52
$$

57. $\mathrm{C}_{\mathrm{T}}=$ line $53+$ line $54+$ line $55+1$ ine $56-1$ ine 22


Total Cost for Non-Solar System
58. $C_{O C} E_{O}=1$ ine $32 \times$ line 50

59. $L c_{f c} E_{f}=\begin{aligned} & \text { line } 35 \times \text { line } 7 \times \text { line } 52 \\ & \text { (maintenance cost neglected) }\end{aligned}$

60. $C_{T C}=$ line $58+$ line 59


Present Value of Life-Cycle Cost Savings With Solar System
61. Savings $=($ line $60-1 i n e ~ 57)$

LIFE CYCLE COST ANALYSIS
CASH FLOW
A. Mortgage interest rate ___ decimal
B. Auxiliary fuel inflation rate
C. General inflation rate $\qquad$ decimal decimal

Collector area
Solar fraction of total load (see Worksheet LCA-1, line 5)

System Cost \$ Down Payment \$ Federal Tax Credit \$ $\qquad$

| [1] | [2] | [3] | [4] | [5] | [6] | [7] | . [8] | [9] | [10] | [11] | [12] |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Year | Annual Mortgage Payment | Years Left on Mortgage | Frac. of Mortgage as Interest | Interest Paid | Auxiliary Fue] Cost | Property $\operatorname{Tax}$ | Insurance | Operating Cost | Maintenance Cost | Income Tax Savings | Expense <br> with <br> Solar |
| 1 |  | 20 |  |  |  |  |  |  |  |  | * |
| 2 |  | 19 |  |  |  |  |  |  |  |  |  |
| 3 |  | 18 |  |  |  |  |  |  |  |  |  |
| 4 |  | 17 |  |  |  |  |  |  |  |  |  |
| 5 |  | 16 |  |  |  |  |  |  |  |  |  |
| 6 |  | 15 |  |  |  |  |  |  |  |  |  |
| 7 |  | 14 |  |  |  |  |  |  |  |  |  |
| 8 |  | 13 |  |  |  |  |  |  |  |  |  |
| 9 |  | 12 |  |  |  |  |  |  |  |  |  |
| 10 |  | 11 |  |  |  |  |  |  |  |  |  |
| 11 |  | 10 |  |  |  |  |  |  |  |  |  |
| 12 |  | 9 |  |  |  |  |  |  |  |  |  |
| 13 |  | 8 |  |  |  |  |  |  |  |  |  |
| 14 |  | 7 |  |  |  |  |  |  |  |  |  |
| 15 |  | 6 |  |  |  |  |  |  |  |  |  |
| 16 |  | 5 |  |  |  |  |  |  |  |  |  |
| 17 |  | 4 |  |  |  |  |  |  |  |  |  |
| 18 |  | 3 |  |  |  |  |  |  |  |  |  |
| 19 |  | 2 |  |  |  |  |  |  |  |  |  |
| 20 |  | 1 |  |  |  |  |  |  |  |  |  |

[2] Annual mortgage payment from LCA-1, line 25
[4] See Figure 12-5
[5] Column [2] x column [4]
[6] First year cost from LCA-1, line 26 Second and future years:
(previous year cost) $\times(1+$ fuel inflation rate)
[7] See line 27, LCA-1
Second and future years:
(previous year cost) $\times(1+$ general inflation rate $)$
[8] See line 28, LCA-1 (and use general inflation rate)
[9] First year cost see Line 29, LCA-1
Second and future years:
(previous year cost) $x(1+$ fuel inflation rate)
[10] First year cost see line 30, LCA-1
Second and future years:
(previous year cost) $x(1+$ general inflation rate)
2] $[2]+[6]+[7]+[8]+[9]+[10]-[11]$
For first year, add down payment and subtract federal
tax credit

LIFE-CYCLE COST ANALYSIS CASH FLOW AND PRESENT WORTH SUMMARIES

| [1] | [2] | [3] | [4] | [5] | [6] | [7] | [8] | [9] | [10] | [11] |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | NON-SOLAR SYSTEM |  |  |  | SOLAR SYSTEM |  |  |  |  |  |
|  |  | d $=$ |  |  | Collector Area _ft $\mathrm{ft}^{2}$ |  |  |  |  |  |
| Year | Fue] plus Operating Expenses | Cumulative Expenses | Present Worth Factor | Present Worth of Annual Cost | Expense with Solar System | Cumulative Expenses | Present Worth of Annual Cost | Present Worth of Savings | Cumulative Present Worth of Savings | Cumulative Savings (cash flow) |
| 7 |  |  |  |  |  |  |  |  |  |  |
| 2 |  |  |  |  |  |  |  |  |  |  |
| 3 |  |  |  |  |  |  |  |  |  |  |
| 4 |  |  |  |  |  |  |  |  |  |  |
| 5 |  |  |  |  |  |  |  |  |  |  |
| 6 |  |  |  |  |  |  |  |  |  |  |
| 7 |  |  |  |  |  |  |  |  |  |  |
| 8 |  |  |  |  |  |  |  |  |  |  |
| 9 |  |  |  |  |  |  |  |  |  |  |
| 10 |  |  |  |  |  |  |  |  |  |  |
| 11 |  |  |  |  |  |  |  |  |  |  |
| 12 |  |  |  |  |  |  |  |  |  |  |
| 13 |  |  |  |  |  |  |  |  |  |  |
| 14 |  |  |  |  |  |  |  |  |  |  |
| 15 |  |  |  |  |  |  |  |  |  |  |
| 16 |  |  |  |  |  |  |  |  |  |  |
| 17 |  |  |  |  |  |  |  |  |  |  |
| 18 |  |  |  |  |  |  |  |  |  |  |
| 79 |  |  |  |  |  |  |  |  |  |  |
| 20 |  |  |  |  |  | , |  |  |  |  |

[2] First year cost, add lines 31 and 32 of LCA-1 Second and future years: (previous year cost) $\times(1+$ fuel inflation rate)
[3] Accumulate col
[4] See Table 12-7
[5] Column [2] x column [4]
[6] Column [12], Worksheet LCA-3
[7] Accumulate column [6]
[8] Column [6] x column [4]
[9] Column [5] x column [8]
[10] Running sum of column [9]
[11] Column [3] - column [7]

