

# Search of nearby resolved neutron stars among optical sources

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## ABSTRACT

Neutron stars are identified as pulsars, X-ray binary components, central objects of supernovae remnants, or isolated thermally emitting sources, and at distances beyond 120 pc. A population extrapolation suggests  $10^3$  objects within that boundary. Potentially, neutron stars could continuously emit gravitational wave signals at sensitivity reach of present instrumentation. As part of our Search for the Nearest Neutron Stars “Five Seasons” project, we search for nearby resolved neutron stars. Based on expected fluxes and magnitudes of thermally cooling neutron stars and pulsars, we selected sources in *Gaia* DR3 with *G*-band absolute magnitudes  $M_G > 16$  mag, parallax signal-to-noise ratios greater than two, and colours  $G_{BP} - G > 0.78$  and  $G - G_{RP} > 0.91$  mag for power-law emitters of flux  $F_\nu \propto \nu^{-\alpha_\nu}$  with spectral indices  $\alpha_\nu < 3$ . The photometric region overlaps with that of white dwarfs, in confluence with most known pulsars in binaries having white dwarf companions. We looked for counterparts in gamma-ray, X-ray, ultraviolet, radio, optical, and infrared catalogues. We find about two X-ray-, 15 ultraviolet-, one radio probable counterparts, and at least four sources with power-law profiles at the ultraviolet–optical(–infrared). Because the sources have  $G \gtrsim 20$  mag, we rely on *Gaia* DR3 single-source parameters. We identify possible binaries based on photoastrometric parameters, visual companions, and flux excesses. Some emission components suggest small thermal radiuses. Source types, relatedness to neutron stars, and properties require further inquiry.

**Key words:** stars: neutron – pulsars: general – white dwarfs – solar neighbourhood

## 1 INTRODUCTION

Neutron stars are extremely compact objects resulting from the collapse of (i) OB transition type stars of roughly eight to twenty solar masses or (ii) accreting white dwarfs. If rotating and axially asymmetric, these compact objects are expected to emit continuously gravitational waves, of very small amplitudes. The wave frequency relates to the rotation frequency, and because ground-based gravitational wave detectors are most sensitive to the  $10^0$ – $10^3$  Hz frequency range (Palomba 2005), targets would have to be rapid rotators. This is fulfilled for example by 0–1 Gyr young pulsars that still have high spin energy or by millisecond pulsars, spun up by accretion. When magnetic fields or magnetic spin-down torques are weak and insignificant, high rotation frequencies are expected to be sustained over long times. Continuous gravitational wave searches are progressively increasing in sensitivity (recent results can be found e.g. in Abbott et al. 2021a,b, 2022a,c,d,e; Ashok et al. 2021; Steltner et al. 2021; Zhang et al. 2021; Covas et al. 2022; Dergachev & Papa 2022; Ming et al. 2022; Steltner et al. 2023).

Young- and millisecond pulsars represent a low percentage of the estimated  $10^8$ – $10^9$  neutron stars in the Galaxy, most of which being expected to be very dim electromagnetically. For a mean inter neutron-star distance of 10 pc (Sartore et al. 2010; Pagliaro et al. 2023), there would be ~10, 1000, and 8000 neutron stars within 20, 100, and 200 pc, respectively. RX J1856.5–3754 at  $d = 123_{-15}^{+11}$  pc

(Walter et al. 1996, 2010) is the nearest known exemplar and it is isolated, X-ray dim, and thermally emitting. As other known thermally-emitting neutron stars (Potekhin et al. 2020), it is expected to cool down quickly over time. Because neutron stars would be numerous within 100–200 pc, some could be still detectable electromagnetically from thermal- or non-thermal emission (see e.g. Toyouchi et al. 2022). These would also be promising targets for continuous gravitational wave searches. Knowing the position of the nearest one would allow for a targeted gravitational-wave search that is more sensitive than broad all-sky searches.

The combination of very high effective temperatures and small radiuses (~10 km) implies that the youngest neutron stars have very high X-ray-to-optical flux ratios, with practically no visible optical counterparts. This led to extensive searches using X-ray sources as reference, in particular with the *ROSAT* All-Sky Survey (RASS; Voges et al. 1999; Boller et al. 2016), to look for optical counterparts, despite the lower X-ray spatial resolution, and identify the sources. Some of these were indeed found to be thermally-emitting neutron stars (see review by Treves et al. 2000). Over the last decades, wide-area optical surveys have become deeper and spatially sharper, as for example the Global Astrometric Interferometer for Astrophysics (*Gaia*) mission (Gaia Collaboration et al. 2016), providing in addition trigonometric parallaxes and proper motions, and the Dark Energy Spectroscopic Instrument (DESI) Legacy Imaging Surveys (Dey et al. 2019). Moreover, several pulsars have been detected in the optical with a significant component of non-thermal origin (see e.g. Zharikov et al. 2021). This motivates us, as part of our Search for the Nearest

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Neutron Stars Five Seasons project, to revisit the search, by using instead faint optical sources as reference and identifying neutron star candidates.

## 2 METHODS

The search methods are as follows:

- (i) First we consider the evolution in luminosity and effective temperature of an isolated thermally emitting neutron star, anchored to an accurately observed object (RX J1856.5–3754), and we compute its emission profile at different ages. We consider also measurement at the ultraviolet–optical–(infrared) of several known thermally-emitting neutron stars and pulsars. For all of these sources, we compute synthetic fluxes and magnitudes at different survey bandpasses.
- (ii) Next we select *Gaia* sources with parallaxes and photometry closest to the expected photometry.
- (iii) Then we prospect the multi-band detectability of neutron stars among these sources.
- (iv) Finally, we crossmatch the sources with catalogue sources at other wavelengths, and verify them in images. We discard unambiguously identified sources and keep potential candidates for searches of continuous gravitational waves.

### 2.1 Expected photometry of resolved neutron stars

After formation, neutron stars are expected to cool mainly through neutrino emission from the core and then through thermal radiation from the surface. The transition time-scale from neutrino- to photon cooling depends on the interior composition and is theoretically estimated to be in the range 0.01–0.1 Myr (see e.g. [Yakovlev et al. 1999, 2004; Page et al. 2006](#)). Observations of young pulsars indicate a decrease and then an increase in the X-ray- and optical to spindown luminosity ratios, that is of the capacity in converting rotational energy to X-ray and optical radiation, for increasing spin-down age. The change occurs at  $\tau \approx 0.01$  Myr and could be associated with the transition to photon cooling ([Zharikov et al. 2006; Zharikov & Mignani 2013](#)). For what follows, we assumed that the cooling is mainly thermal at  $\gtrsim 0.1$  Myr. During thermal cooling, the surface temperature and luminosity can be approximated by  $T \propto t^{-1/2}$  and  $L \propto t^{-2}$  ([Tsuruta 1979; Patruno & Kama 2017](#)), as it roughly depicts, at ages of 0.1–10 Myr, the distribution of thermally-emitting neutron stars in a log–log plane, such as presented in [Potekhin et al. \(2020\)](#). This allows us to estimate the main observables as a function of time:

- the surface temperature

$$T = T_0(t/t_0)^{-1/2} \quad (1)$$

where  $T_0$  and  $t_0$  are the present temperature and age,

- the thermal luminosity

$$L = 4\pi R^2 \sigma T_{\text{eff}}^4 = L_0(t/t_0)^{-2} \quad (2)$$

where  $R$  is the emitting radius,  $\sigma$  the Stefan-Boltzmann constant,  $T_{\text{eff}}$  the effective temperature, and  $L_0$  the present luminosity,

- the bolometric magnitude

$$m_{\text{bol}} = M + 5 \log(d[\text{pc}]/10) \quad (3)$$

where the absolute magnitude

$$M = -2.5 \log(L/L_{\odot}) + M_{\odot}, \quad (4)$$

with  $L_{\odot} = 3.826 \times 10^{33}$  erg s<sup>-1</sup> and  $M_{\odot} = 4.755$  mag for the Sun, and  $d$  is the distance, and

- the flux

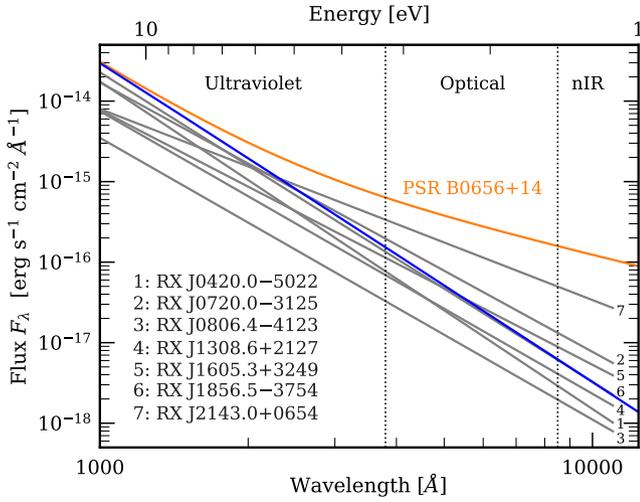
$$F = L/(4\pi d^2). \quad (5)$$

We assumed an emission profile resembling that of RX J1856.5–3754, as a simplified version of emission profiles of known thermally-emitting isolated neutron stars, and because this object is the nearest known neutron star, has an accurate distance measured from trigonometric parallax, and was frequently observed for observational calibration and object comparison at X rays. The template profile is composed of (i) a very soft X-ray blackbody, (ii) ultraviolet and optical fluxes greater than the Rayleigh-Jeans tail of the X-ray blackbody, and (iii) optionally, X-ray emission from accretion of interstellar matter.

We note that RX J1856.5–3754 and the other known X-ray dim thermally-emitting isolated neutron stars would have very strong magnetic fields, similar to those of strong magnetic-field pulsars but weaker than magnetars ([Enoto et al. 2019](#)). We assumed that this affects only weakly the thermal luminosity ([Potekhin et al. 2020](#)) and their potentialities for gravitational wave detection. We note also that the most luminous and youngest thermally-emitting neutron stars are associated with supernova remnants at  $\gtrsim 1$  kpc, and have X-ray luminosities as high as  $10^{34.5}$  erg s<sup>-1</sup> at  $\sim 1$  kyr ([Potekhin et al. 2020](#)), thousand times brighter than RX J1856.5–3754. Finally, we note that millisecond pulsars emit typically less thermally than RX J1856.5–3754, where the low thermal emission is maintained through re-heating (from accretion or internal processes) or from hot polar caps ([Potekhin et al. 2020; Beznogov et al. 2021](#)). However, compared to less young thermally-emitting neutron stars, some isolated millisecond pulsars could turn out to be brighter (see below).

We adopted for RX J1856.5–3754 an unabsorbed X-ray blackbody of temperature  $kT_X^{\infty} = 63.5 \pm 0.2$  eV ( $736\,882 \pm 2321$  K), corresponding to a luminosity  $L^{\infty} = 10^{31.63}$  erg s<sup>-1</sup> ([Burwitz et al. 2003](#)) and an emitting radius  $R^{\infty} = 4.51$  km for the distance  $d = 123$  pc. We assumed an unabsorbed ultraviolet–optical flux excess of factor eight relative to the blackbody Rayleigh-Jeans tail ( $F_{\lambda} \propto \lambda^{-\alpha_{\lambda}}$  with a spectral index  $\alpha_{\lambda} = 4$ , or  $F_{\nu} \propto \nu^{-\alpha_{\nu}}$  with  $\alpha_{\nu} = -2$ ), so that it matches the unabsorbed fit from [van Kerkwijk & Kulkarni \(2001\)](#). It agrees also with the unabsorbed fit from [Kaplan et al. \(2011\)](#). The excess corresponds to a  $-2.26$  mag brighter magnitude. From [Kaplan et al. \(2011\)](#), the seven known thermally-emitting isolated neutron stars have flux excesses of factor 5–12 at 4700 Å and  $\alpha_{\lambda} = 3.2 - 4.2$  at the ultraviolet–optical, except RX J2143.0+0654, which has a flux excess of factor 50 and  $\alpha_{\lambda} = 2.5$ . As shown in fig. 5 of that study, the hotter these objects are at X rays (e.g. compared to RX J1856.5–3754), roughly the smaller their ultraviolet–optical  $\alpha_{\lambda}$  spectral indices and the shallower the slopes, implying less blue colours. This diversity of optical power law slopes motivated us to adopt for RX J1856.5–3754 a blackbody at X rays and a power law in the optical, rather than two blackbodies adjusting the X-ray- and optical fluxes. Figure 1 illustrates the spectral flux density distributions (hereafter spectra, or more generally speaking, spectral energy distributions – SEDs) of the seven objects, scaled to 10 pc using their distances of  $1.2 - 4.1 \times 10^2$  pc compiled in [Potekhin et al. \(2020\)](#), and assuming validity of extrapolation at 8500–11000 Å. Their apparent and absolute spectra are also shown in Fig. 2.

For RX J1856.5–3754, the unabsorbed RASS 0.1–2.4 keV flux is of  $1.5 \times 10^{-11}$  erg s<sup>-1</sup> cm<sup>-2</sup> ([Walter et al. 1996](#)) and translates to  $2.27 \times 10^{-9}$  erg s<sup>-1</sup> cm<sup>-2</sup> at 10 pc; from the blackbody we retrieve a flux of  $2.67 \times 10^{-9}$  erg s<sup>-1</sup> cm<sup>-2</sup> assuming a 100 per cent transmission, which is fairly in agreement. We adopted a present age of 2 Myr ( $t_0$ ), in between the kinetic age of 0.42 Myr ([Mignani et al. 2013](#)) and the spindown age of 3.8 Myr ([van Kerkwijk & Kaplan 2008](#)).



**Figure 1.** 10 pc unabsorbed spectra at 1000–11000 Å. The ultraviolet–optical fits from Kaplan et al. (2011) for the seven known X-ray dim isolated neutron stars are represented by the grey lines. The tail of the X-ray blackbody fit from Burwitz et al. (2003) for RX J1856.5–3754, multiplied by eight, is shown by the blue line, which is very close to the grey line for this object. The fit from Zharikov et al. (2021) for PSR B0656+14 is represented by the orange line.

We assumed that the ultraviolet–optical flux excess is slowly damped over time, by a factor of  $1/\log((2+t/t_0)^2)$  and starting at  $1.16 \times t_0$ . At 400–1000 Å, we assumed a linear transition in logarithmic scale from the X-ray blackbody to the flux excess. For simplicity, we assumed a constant emission radius and that the surface temperature relates with time as in Equation (1) even beyond 10 Myr.

Finally, we adopted an optional, 0.1–2.4 keV X-ray accretion luminosity of  $10^{28}$  erg s<sup>-1</sup> of very low-density gas (table 2 in Blaes & Madau 1993), as in the interstellar surroundings of the Sun, also known as the local cavity or Local Bubble, delimited by dense clouds at 40–180 pc and other neighbouring cavities (see e.g. Vergely et al. 2010). This accretion luminosity could be activated at any time during the thermal evolution of the neutron star.

We then computed the emission profiles for ages of 0.01, 0.05, 0.1, 0.2, 1, 2, 5, 10, 20, 50, 120, 300, 600, 1000, and 5000 Myr. At ages >0.1 Myr, the traced-back luminosities are consistent with the observed luminosities of thermally emitting neutron stars. At younger ages of 0.01 and 0.05 Myr, the traced-back ones are up to  $10^{36}$  erg s<sup>-1</sup> and unrealistically higher than those observed ( $10^{31}$ – $10^{33}$  erg s<sup>-1</sup>), as in fig. 2 in Potekhin et al. (2020).

Similarly as in Toyouchi et al. (2022), we considered the theoretical surface thermal evolution of a pulsar with rotochemical heating and an initial spin period of 1 ms (having the hottest temperature over time) presented in Hamaguchi et al. (2019), which is the same with or without dark matter heating. In this case we did not add any flux factor for any optical excess-mission, for simplicity. We assumed a neutron star radius of 11 km when computing the thermal luminosities.

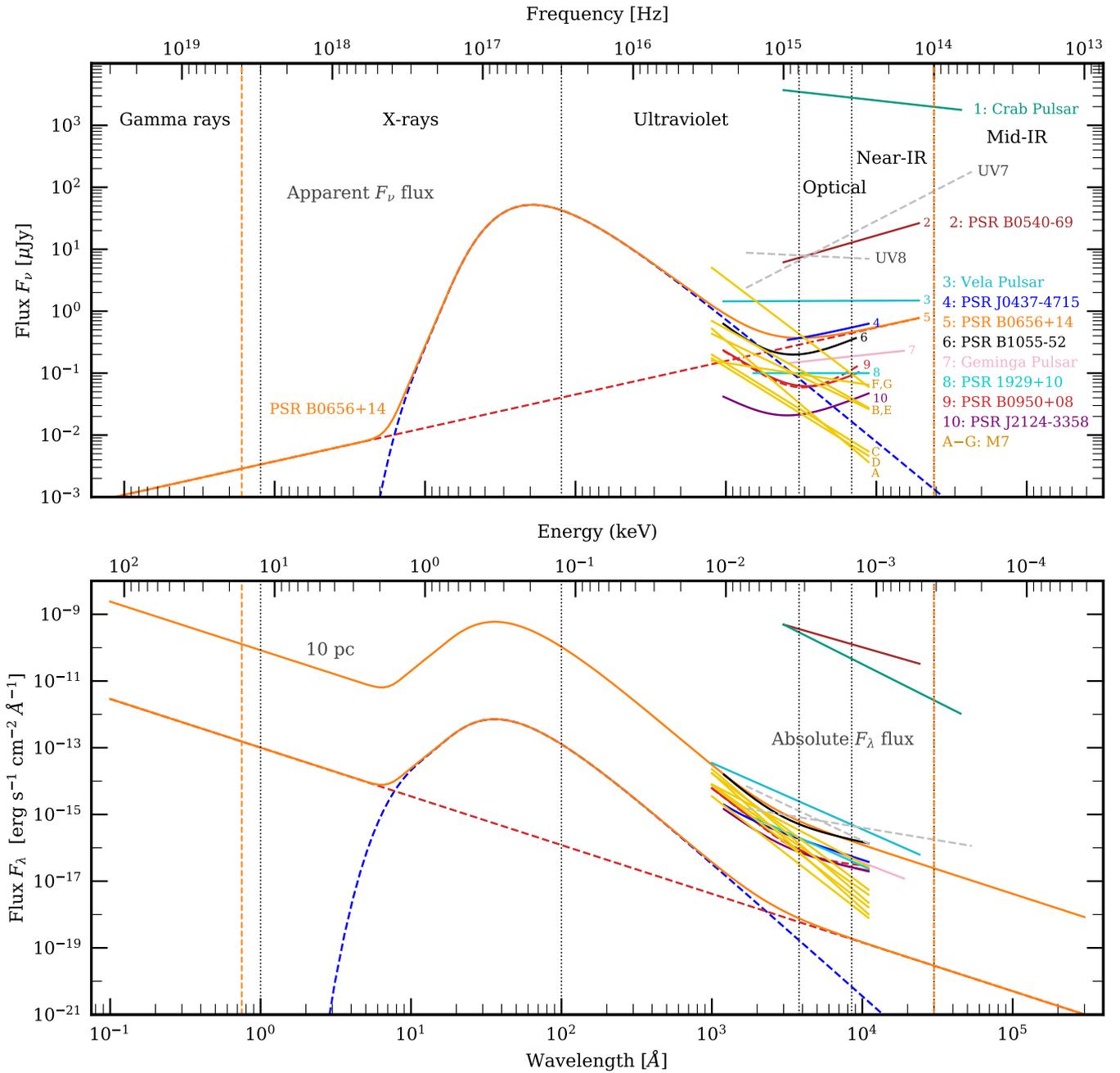
We included also isolated pulsars that are firmly identified and measured photometrically in the ultraviolet–optical–(infrared). In general, isolated pulsars present (i) power-law emission, in the wavelength range between high-energy photons and radio waves, related to the magnetosphere, and sometimes also (ii) hot thermal emission of the neutron-star surface or caps. We considered first PSR B0656+14 (0.11 Myr, 288 pc), which is extensively characterised (Zharikov et al. 2021). From the *N1*0 fit with the G2BB + PL spectral model, it has (i) a power-law component of photon index  $\Gamma = 1.54$  and normalisation  $PL_{\text{norm}} = 1.97 \times 10^{-5}$  photons keV<sup>-1</sup> cm<sup>-2</sup> s<sup>-1</sup> at 1 keV,

and (ii) a blackbody component for the surface ( $kT^\infty = 68$  eV) and another for the hot polar caps ( $kT^\infty = 134$  eV). The bolometric thermal luminosity is of  $\log(L^\infty) = 32.5$  erg s<sup>-1</sup>. Figure 2 shows the spectra in frequency (top panel) and wavelength (bottom panel) of the unabsorbed model fit, where we omitted the Gaussian absorption line at 547 eV, which does not affect significantly the X-ray part. We verified that the relative difference of spectral energy distribution  $(\lambda F_\lambda - \nu F_\nu)/(\lambda F_\lambda)$  is zero over the energy range (standard deviation  $\sigma < 10^{-15}$ ) and thus that the representations are equivalent. This figure shows that, at optical wavelengths, the power-law component has a flux that is about ten times the flux extrapolation of the X-ray blackbody, and a slope that is less blue than those of the seven known thermally-emitting isolated neutron stars (see also Fig. 1), implying photometric colours that are redder, albeit still close to neutral.

We considered the dereddened blackbody- and power-law fit to ultraviolet–optical photometry (1200–9000 Å) of the PSR B1055–52 radio pulsar (0.535 Myr, ~350 pc) obtained by Mignani et al. (2010). The power-law component ( $F_\nu \propto \nu^{-\alpha_\nu}$  with  $\alpha_\nu = 1.05 \pm 0.34$ ) dominates in the optical at >3000 Å and we assumed validity of extrapolation at 9000–11000 Å. We considered also the dereddened blackbody- and power-law fit to ultraviolet–optical photometry of the intrinsically fainter PSR B0950+08 radio pulsar (17.5 Myr, 262 pc) obtained by Pavlov et al. (2017). Although this fit is less certain ( $\alpha_\nu = 1.21 \pm 0.42$ ) and we assumed validity of extrapolation at 9500–11000 Å, it suggests an even redder colour. (Assuming a spectral index of  $\alpha_\nu = 1.63$ , its synthetic  $G - G_{RP}$  and  $G_{BP} - G_{RP}$  colours would be redder by <0.1 and <0.2 mag.)

Next, we considered the  $\alpha_\nu = 0$  dereddened fit to the ultraviolet–near-infrared ( $\approx 1000$ –24000 Å) photometry of the Vela Pulsar (0.011 Myr) obtained by Zyuzin et al. (2013), for its distance of about 285 pc (Dodson et al. 2003). Then, we considered the  $\alpha_\nu = 0.26$  dereddened power-law fit at 3290–19000 Å for the Geminga Pulsar (0.342 Myr) from Shibanov et al. (2006), for its distance of 0.25 kpc (Verbiest et al. 2012). We considered the  $\alpha_\nu = 0$  dereddened power-law fit at 1890–4750 Å for PSR 1929+10 (3.11 Myr) from Mignani et al. (2002), for its distance of 0.31 kpc (Verbiest et al. 2012), and assuming validity of extrapolation up to 11000 Å. Also, we considered the  $\alpha_\nu = -0.27$  dereddened power-law fit at 3000–45000 Å for the Crab Pulsar (1054 kyr) from Sandberg & Sollerman (2009), for its distance of 2 kpc (Trimble 1973), and we considered the  $\alpha_\nu = 0.70$  dereddened power-law fit at 3000–24000 Å for PSR B0540–69 (1700 kyr; in the Large Magellanic Cloud at 48.97 kpc) from Mignani et al. (2012, 2019). The Crab Pulsar and PSR B0540–69 are so young and bright that we did not consider their absolute magnitudes ( $M_G = 3.5$  and 2.8 mag) for the search of nearby neutron stars.

Finally, we included the non-accreting, recycled millisecond pulsars PSR J0437–4715 (Kargaltsev et al. 2004; Durant et al. 2012; González-Caniulef et al. 2019) and PSR J2124–3358 (Rangelov et al. 2017). PSR J0437–4715 (6.7 Gyr) is the nearest known millisecond pulsar, at  $156.3 \pm 1.3$  pc. Its to gamma-ray- to ultraviolet emission distinguishes clearly from the optical–infrared emission of its 4000 K white dwarf companion, which is bright in *Gaia* with  $M_G = 14.4$  mag. We considered the CutPL+3BB fit obtained shortwards of 3300 Å (Durant et al. 2012), composed of a cutoff power law of photon index  $\Gamma = 1.562 \pm 0.013$  ( $\alpha_\nu = \Gamma - 1 = 0.562$ , similar to that of PSR B0656+14), extending from gamma- to X-rays and possibly the ultraviolet, and three consecutive X-ray–ultraviolet blackbodies. Extrapolating the fit to the optical, the power-law contribution dominates the contribution of the Rayleigh-Jean tail of the coolest of the three blackbodies, implying higher fluxes and redder colours in the optical. In the case of PSR J2124–3358 (~11 Gyr, ~410 pc),



**Figure 2.** Unabsorbed spectra in frequency (*top panel*) and wavelength (*bottom panel*) of the model fit adopted for PSR B0656+14, based on observed fluxes in the range delimited by the vertical orange dashed lines (see Section 2.1 and Zharikov et al. 2021). The blackbody component, power law component, and sum of both are represented by the blue dashed-, red dashed-, and orange solid lines, respectively. The other solid lines represent fits to unabsorbed fluxes of other neutron stars, as observed (*top panel*, annotated with numbers and names), and scaled to 10 pc based on their known distances (*bottom panel*). These neutron stars are the Crab Pulsar (green), PSR B0540–69 (brown), the Vela Pulsar (cyan), PSR J0437–4715 (blue), PSR B1055–52 (black), the Geminga Pulsar (pink), PSR 1929+10 (turquoise), PSR B0950+08 (red; the dashed line is for the maximal spectral index), PSR J2124–3358 (purple), and the known X-ray dim isolated neutron stars (M7, yellow) RX J0420.0–5022 (A), RX J0720.0–3125 (B), RX J0806.4–4123 (C), RX J1308.6+2127 (D), RX J1605.3+3249 (E), RX J1856.5–3754 (F) and RX J2143.0+0654 (G). Example of power-law components of the UV7 and UV8 candidates are represented by the grey dashed lines.

it has two ultraviolet and one optical photometric measurements in the range 1200–7000  $\text{\AA}$  (Rangelov et al. 2017), whose values can be associated with thermal- and magnetospheric emissions, respectively. We adopted the blackbody+power-law fit with  $R_{\text{bb}} = 12$  km,  $T_{\text{bb}} = 11.72 \times 10^4$  K, and  $\alpha_\nu = 1$ , and we assumed validity of extrapolation up to 11000  $\text{\AA}$ . In Fig. 2, we show the corresponding apparent- and absolute spectra for these neutron stars.

We then derived synthetic fluxes and magnitudes at different instrumental bandpasses for the above emission profiles and power-law profiles of different spectral indices, using the `PHYPHOT`<sup>1</sup> package from Morgan Fouesneau in the `PYTHON` programming language. We

<sup>1</sup> <https://mfouesneau.github.io/pyphot/>

adopted the  $G_{BP}$ ,  $G$ , and  $G_{RP}$  bandpasses of the *Gaia* Early Data Release 3 (EDR3; [Gaia Collaboration et al. 2021a](#)), which span the wavelength range 3300–10500 Å. Given that we focus on small distances <50–120 pc, we assumed in a first approximation no significant interstellar extinction and reddening.

Possibly some isolated neutron stars emitting as pulsars might have even redder ultraviolet–optical colours than the known pulsars. We can adopt a colour upper bound from radio pulsars, for which many radio observations are available, although the spectral slopes at radio and optical might differ. At low radio frequencies (down to ~100 MHz), spectral indices peak at about  $\alpha_\nu = 1.7$ , and values are typically lesser than 3 ([Kuzmin & Losovsky 2001](#); [Kuniyoshi et al. 2015](#)). We assumed thus in the optical an upper bound for the spectral slope of  $\alpha_\nu = 3$ , which implies colours  $G_{BP} - G = 0.78$ ,  $G - G_{RP} = 0.91$ , and  $G_{BP} - G_{RP} = 1.69$  mag.

## 2.2 Selection of *Gaia* sources with parallaxes

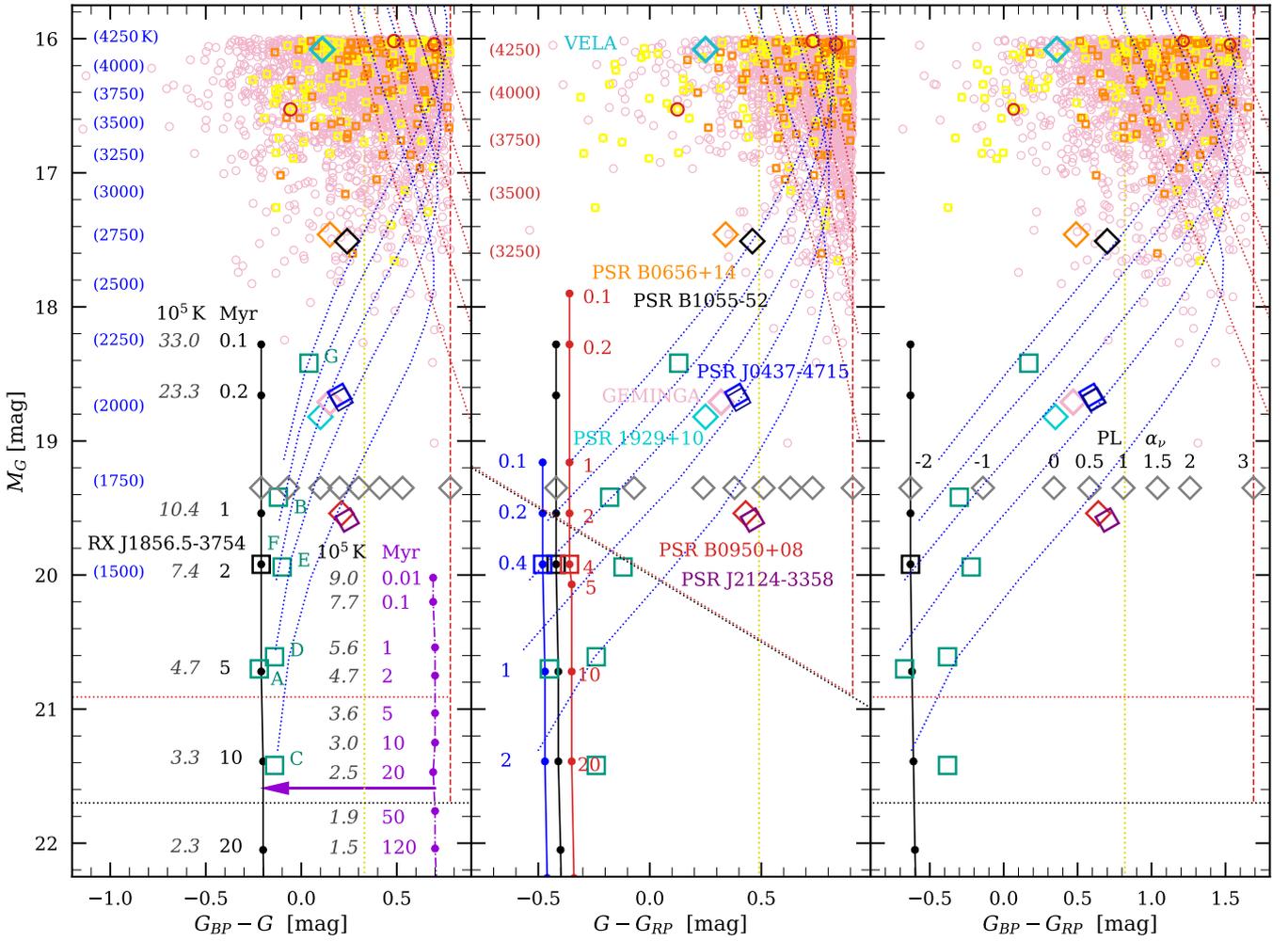
First, we considered the location of neutron stars in the  $M_G$  versus  $G_{BP} - G$ ,  $G - G_{RP}$ , and  $G_{BP} - G_{RP}$  colour–absolute magnitude diagrams, shown in Fig. 3. In the three panels, the black solid line represents the thermal cooling track with ultraviolet–optical excess, anchored to RX J1856.5–3754 (black open square, labelled F in the left panel) at a present age  $t_0 = 2$  Myr. In the middle panel, the blue- and red tracks are for present ages  $t_0 = 0.4$  and 4 Myr, in which cases the  $G$ -band absolute magnitudes at <2 Myr offset by up to +1.5 and –0.4 mag. The other X-ray dim, thermally-emitting neutron stars are represented by green squares: RX J0420.0–5022 (A), RX J0720.0–3125 (B), RX J0806.4–4123 (C), RX J1308.6+2127 (D), RX J1605.3+3249 (E), and RX J2143.0+0654 (G). The Vela (0.011 Myr), PSR B0656+14 (0.11 Myr), PSR B1055–52 (0.535 Myr), Geminga (0.342 Myr), PSR 1929+10 (3.11 Myr), and PSR B0950+08 (17.5 Myr) pulsars are represented by the cyan, orange, black, pink, turquoise, and red diamonds, respectively. The PSR J0437–4715 (6.7 Gyr) and PSR J2124–3358 (11 Gyr) millisecond pulsars are represented by the blue- and purple slightly tilted diamonds. As a curiosity, we note that their potential colours are very close to the expected colours of the Sun,  $G_{BP} - G = 0.33$ ,  $G - G_{RP} = 0.49$ , and  $G_{BP} - G_{RP} = 0.82$  mag ([Casagrande & Vandenberg 2018](#)) delineated by the yellow vertical dotted lines. RX J2143.0+0654 is 1.6 mag brighter at  $M_G$  than RX J1856.5–3754. Given its spin-down age of 3.7 Myr ([Potekhin et al. 2020](#)), its trace-back to ~0.1 Myr would lead to an even brighter  $M_G$ . Also, the absolute magnitudes of the cooling tracks anchored to RX J1856.5–3754 are for an emitting radius at infinity of 4.51 km; for a neutron star emitting from its whole surface, that is with an emitting radius about thrice larger, the magnitudes would be about 2.5 mag brighter (cf. equations (2) and (4)). Besides this, PSR B0656+14, PSR B1055–52 and the Vela Pulsar are also brighter, the last one having  $M_G = 16.1$  mag. Finally, equal-brightness neutron star binaries would have absolute magnitudes brighter by 0.75 mag. For these reasons, for the search of neutron stars older than 0.01–0.1 Myr, it seemed appropriate to us to select *Gaia* source with  $M_G > 16.0$  mag.

We queried *Gaia* sources with  $M_G > 16.0$  mag ( $\text{phot\_g\_mean\_mag} + 5 \log_{10}(\text{parallax}) - 10 > 16$ ) and parallax signal-to-noise  $\text{snr}_\pi > 2$  ( $\text{parallax\_over\_error} > 2$ ). *Gaia* DR3 has 90 and 50 per cent completeness at about  $G = 20.5$  and 21.0 mag, based on a comparison ([Gaia Collaboration et al. 2021b](#)) with the Panoramic Survey Telescope and Rapid Response System (Pan-STARRS; PS1) survey ([Chambers et al. 2016](#)). The query yielded 75 073 sources. Details on the flux uncertainties and sample limits in absolute- and apparent magnitudes are given in Ap-

pendix A. The sources have parallaxes of  $\pi > 8.9$  mas and are in the  $\pi > 8$  mas *Gaia* Catalogue of Nearby Stars (GCNS; [Gaia Collaboration et al. 2021b](#)). Of these, 3312 and 71761 (4.4 and 95.6 per cent) are among the selected- and rejected sources of the GCNS 100 pc (GCNS100pc) sample. The latter ones are either expected to be beyond 100 pc or to have a spurious astrometric solution. Because we are searching for sources that are outliers in terms of absolute magnitude, colour, and kinematics respect to known-population statistics and stellar mock catalogues used as priors for distance estimates, we relied first on the parallaxes and the absolute magnitudes derived directly from the parallaxes. We note that the magnitude criterium is equivalent to the parallax criterium  $\pi > 10^{(26-G)/5}$  mas. This can be converted to a distance criterium for sources with  $\text{snr}_\pi$  well above 3, for which the distance inverse-proportionality to the parallax,  $d = 1/\pi$ , tends to be valid (see e.g. [Messineo & Brown 2019](#)). In this case,  $G = 19$  mag implies  $\pi > 25$  mas and  $d < 40$  pc, and  $G = 21$  mag implies  $\pi > 10$  mas and  $d < 100$  pc. At these distances, neutron stars with transverse physical velocities of  $v_t \leq 200$  kms/s have proper motions ( $pm$ ) of  $\mu \leq 1055$  and 422 mas yr<sup>-1</sup>, since  $\mu = (1000/4.74) v_t/d$ .

We then selected sources less red than the boundary colours defined by a power law of spectral index  $\alpha_\nu = 3$  (see above; vertical red dashed lines in Fig. 3), with  $G_{BP} - G < 0.78$ ,  $G - G_{RP} < 0.91$  mag, and  $\text{snr}_{\text{flux}} \geq 2$  at  $G_{BP}$  and  $G_{RP}$ . It yielded 2464 sources (pink circles in Fig. 3), which have  $\pi = 9.9 - 48.5$  mas and  $pm = 0.1 - 2354$  mas yr<sup>-1</sup>. In Appendix A, we comment about two sources with very blue  $G_{BP} - G$  colours of –2.7 mag, the corrected colour-excess factor ( $\text{phot\_bp\_rp\_excess\_factor\_corrected}$ ), the *Gaia* (E)DR3 bias at low fluxes, and the taking in of sources that are in fact redder than the colour values in the catalogue. The combination of the maximum  $M_G$ ,  $M_{BP}$ , and  $M_{RP}$  of the  $M_G > 16$  mag sample (grey dotted lines) and the colour criteria reduces the maximum  $M_G$  to 20.91 mag at  $G_{BP} - G$  and  $G_{BP} - G_{RP}$  (red dotted lines). (We note that we initially started the study with *Gaia* DR2, which provides much fainter absolute  $G$ -band magnitudes, closer to those of thermal cooling neutron stars; however, the fainter- $M_G$  *Gaia* DR2 sources have spurious astrometric parameters, as described below). The maximum apparent magnitudes at  $G_{BP}$ ,  $G$ , and  $G_{RP}$  in the subsample are of about 21.7, 21.1, and 21.1 mag, as defined by different sources that are real, relatively isolated, and have magnitude errors smaller than about 0.15 mag. Finally, 4 and 29 per cent of the 2464 sources have  $\text{snr}_\pi = 2 - 3$  and  $3 - 5$ , and  $M_G = 16.0 - 16.5$  and 16.0–17.4 mag, respectively.

Some nearby stars with measured parallax and proper motion are not in *Gaia* DR3 or do not have parallax and proper motion in *Gaia* DR3 ([Gaia Collaboration et al. 2021b](#)). We thus checked the list from [Gaia Collaboration et al. \(2021b\)](#) of 1258 sources missing in DR3. We anchored the power law with spectral index  $\alpha_\nu = 3$  to  $M_G = 16$  mag, and we saw that most sources have  $M_H < 14.8$  mag, brighter than this power law would permit at  $H$  band, whereas the fainter ones are all classified as TY-type brown dwarfs. There are 124 sources without  $JH$ -band photometry that have  $M_V$  from –1 to 14 mag and that are also too bright. The remaining sources are either bright multiple stars, low-mass stars, brown dwarfs, or Simbad entries of radial-velocity planets. Besides this, we queried *Gaia* DR2 sources with the same parallax- and colour selection criteria as above and, to limit verification, we considered only the 24 sources at  $M_G = 18.5 - 23.5$  mag that do not have parallax nor proper motion in DR3. From visual verification in optical archive images, we found that these sources are significantly blended within arcseconds and faint, probably causing the spurious DR2 parameters, and therefore these sources can be discarded.



**Figure 3.**  $M_G$  versus  $G_{BP} - G$ ,  $G - G_{RP}$ , and  $G_{BP} - G_{RP}$  colour–absolute magnitude diagrams. In the middle panel, the thermal cooling tracks with ultraviolet–optical excess, anchored to RX J1856.5–3754 for its fiducial-, kinetic-, and spindown ages of 2, 0.4, and 4 Myr, are represented by the black, blue, and red solid lines, respectively. The later two tracks are offset in colour by  $-0.06$  and  $0.06$  mag for clarity. RX J1856.5–3754 is indicated by the black open square and labelled F in the left panel. Other X-ray dim, thermally-emitting isolated neutron stars are represented by green squares and labelled in the left panel: RX J0420.0–5022 (A), RX J0720.0–3125 (B), RX J0806.4–4123 (C), RX J1308.6+2127 (D), RX J1605.3+3249 (E), and RX J2143.0+0654 (G). The thermal model with rotochemical heating for a pulsar of initial period of 1 ms is shown by the violet dash-dotted line (offset in colour by  $+0.9$  mag for clarity); effective temperatures in  $10^5$  K and ages in Myr are indicated left to the track. Only *Gaia* sources with  $M_G > 16$  mag and less red than the colour selection boundaries (red vertical dashed lines) are shown, as pink circles. Those identified as probable white-dwarf photometric candidates in GCNS or else are indicated by yellow- or orange small squares ( $P_{WD} > 0.5$ ; see Appendix A for details) and those part of resolved wide binaries are indicated by red circles (the other components have  $M_G < 16$  mag). The Vela, PSR B0656+14, PSR B1055–52, Geminga, PSR 1929+10, and PSR B0950+08 pulsars are represented by the cyan, orange, black, pink, turquoise, and red diamonds, respectively. The PSR J0437–4715 and PSR J2124–3358 millisecond pulsars are represented by the blue and purple slightly tilted diamonds. A pulsar such as PSR J0437–4715 but with an insignificant thermal emission of  $T_{\text{eff}} < 10^5$  K (dark-blue diamond) has practically the same location as PSR J0437–4715. The grey diamonds represent pure power-law sources of  $\alpha_\nu = -2, -1, 0, 0.5, 1, 1.5, 2,$  and  $3$ , respectively; their  $M_G$  magnitude is arbitrary. The expected colours of the Sun are represented by the yellow vertical dotted lines. The lower grey dotted lines correspond to the maximum  $M_G$ ,  $M_{BP}$ , and  $M_{RP}$  magnitudes of *Gaia* DR3 sources with  $\text{snr}_\pi > 2$ , most of which have red colours and are not shown in the plots. The red dotted lines indicate the combined limit with the colour selection criteria. Theoretical cooling sequences of white dwarfs with pure hydrogen- and pure helium atmospheres (blue- and red dotted curves) are shown for masses of  $0.4, 0.6, 0.8, 1.0,$  and  $1.2 M_\odot$  from top to bottom. H and He effective temperatures for  $0.8 M_\odot$  are indicated in parenthesis in the left- and middle panels.

Fig. 3 shows that despite *Gaia* DR3 allowing us in principle to probe absolute magnitudes as faint as  $M_G \sim 20.9$  mag in the colour-selected subsample, most of the colour-selected sources are very bright and red, and much brighter and redder than the known X-ray dim, thermally-emitting isolated neutron stars. Redwards of the  $G - G_{RP}$  selection boundary, the number of fainter sources increases progressively, down to  $M_G \approx 21.7$  at  $G - G_{RP} \approx 1.8$  mag (not shown in Fig. 3). However in this first step, we consider only neutron stars that are resolved (as those described above) or that do not

have excessively red companions. L- and T-type brown dwarfs have  $M_G \approx 16 - 20$  and  $>20$  mag, and  $G - G_{RP} > 1.55$  and  $>1.8$  mag (Reylé 2018; Smart et al. 2019), and were discarded by the colour-selection criterium. Late-T or Y-type dwarfs, closer to the planetary-mass regime ( $<13 M_{\text{Jup}}$ ), have  $M_G \gtrsim 21$  mag and even redder  $G - G_{RP}$  colours. As unresolved companions, these could remain hidden in the photometry of the brightest colour-selected sources.

In Fig. 3, probable white-dwarf photometric candidates from GCNS and other references are indicated by yellow- and orange small

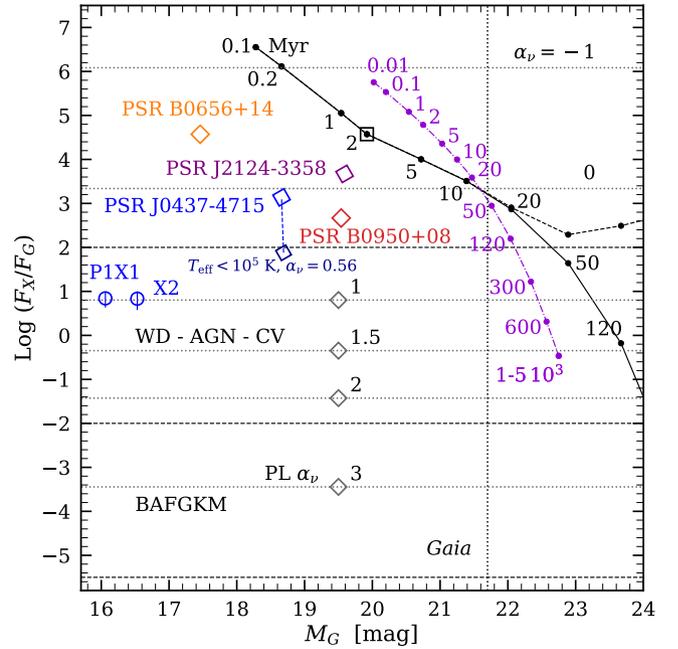
squares, respectively (more information is given in Appendix A). Also, the theoretical cooling sequences of white dwarfs with pure-hydrogen- and pure-helium atmospheres<sup>2</sup> (Bédard et al. 2020) are represented by blue- and red dotted curves, for masses of 0.4, 0.6, 0.8, 1.0, and 1.2  $M_{\odot}$  from top to bottom. From these sequences, white dwarfs with  $M_G > 16$  mag would be older than about 5.0–6.5 Gyr (pure He) and 6.7–8.3 Gyr (pure H), for masses of 1.2–0.4  $M_{\odot}$ . At the considered colours, those with pure-He atmospheres would always be younger than 10 Gyr, the approximate age of the Galaxy, whereas those with pure-H atmospheres would be older than 10 Gyr at  $M_G > 17.0, 16.1, 15.8, 16.3, 21.3$  mag for masses of 0.4, 0.6, 0.8, 1.0, and 1.2  $M_{\odot}$ , respectively.

The distribution of sources in the absolute-magnitude–colour diagrams of Fig. 3 can be explained in part as a faint and diffuse extension of the white dwarf sequence (Scholz 2022), extension consisting of relatively old white dwarfs that are either cooler- (McCleery et al. 2020) or more massive (Kilic et al. 2020, 2021). Because degenerate objects tend to be dominated by the gravitational force, that is by their own weight, those that are more massive, have smaller radii and thus, for surface–light-emitting objects, fainter absolute magnitudes. The distribution of the sources could also be explained by the notion that neutron stars are (a) rare, given that these are probably one order of magnitude less frequent than white dwarfs, mainly because their higher-mass progenitor stars are less frequent, and (b) intrinsically faint, in particular the thermally-emitting ones, expected to cool down and dim to  $M_G \gtrsim 21$  mag in less than a half-dozen Myrs after formation.

### 2.3 Prospects of multi-band detectability of neutron stars among the *Gaia* sources

The spectral energy distributions of white dwarfs can be approximated by single blackbodies of  $T_{\text{eff}} \lesssim 10^5$  K (see e.g. Gentile Fusillo et al. 2019), whereas those of known neutron stars imply typically very hot blackbodies or power laws. Figure 4 shows an X-ray-to-optical flux ratio versus  $M_G$  diagram. The ratio is defined as  $\log(f_X/f_G) = \log(f_X) + 0.4G + 5.10$ , where the flux is in  $\text{erg s}^{-1} \text{cm}^{-2}$  and the constant 5.10 stems from  $-\log(f_G [\text{Vega}])$ , where  $f_G [\text{Vega}]$  is the flux of the Vega star without normalisation by the filter transmission. The ratio is a variant of that defined by Maccauro et al. (1988) and we assume schematically that white dwarfs, active galactic nuclei (AGN), and cataclysmic variables (CV) have log ratios of -2 to 2, and that BAFGKM-type stars have lesser ratios, below -2 (for M dwarfs in *eROSITA*, see Magaudda et al. 2022). Known neutron stars have the greatest X-ray-to-optical flux ratios, typically upped by thermal emission. For pulsars whose thermal emission is insignificant compared to the magnetospheric emission, the log ratio can be in the range [-2, 2], overlapping with that of white dwarfs, or even lower. In Fig. 4, this is illustrated with a pulsar such as PSR J0437–4715 but with  $T_{\text{eff}} < 10^5$  K, represented by the bottom dark-blue lozenge at  $\alpha_{\nu} = 0.56$ , linked with a blue dashed line to the blue lozenge of PSR J0437–4715. Considering PSR B0656+14 instead, similarly, the ratio would decrease to that at  $\alpha_{\nu} \approx 0.55$ . The low ratios are also illustrated with power-law sources of  $M_G = 19.5$  mag and spectral indices of  $\alpha_{\nu} = 1, 1.5, 2,$  and  $3$ . The same example sources are represented in Fig. 3, where we note that removing the thermal component of PSR J0437–4715 does not change its optical photometry.

The X-ray flux versus  $G$ -band apparent magnitude diagram



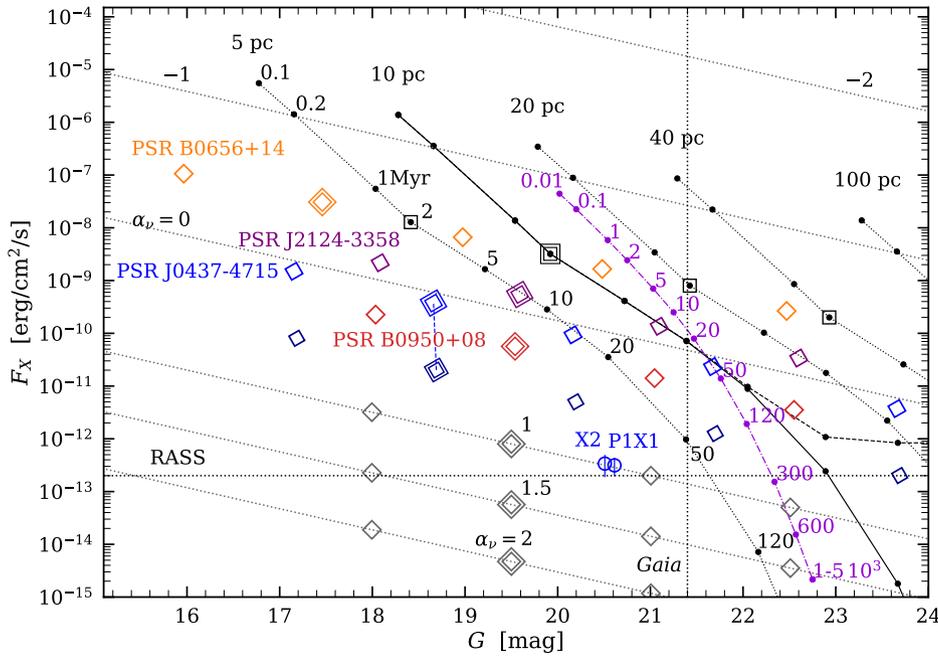
**Figure 4.** X-ray-to-optical flux ratio versus  $G$ -band absolute magnitude diagram. The thermal cooling tracks without- and with interstellar accretion are represented by the black solid and dashed lines. Power-law sources are indicated by the grey dotted lines and the corresponding spectral indices. The P1X1 and X2 RASS crossmatch candidates are indicated by the blue open circles. Same as in Fig. 3.

of Fig. 5 shows that *Gaia* sources similar to known thermal-emitting neutron stars would be very bright at X-rays. We considered RX J1856.5–3754, PSR B0656+14, and PSR J0437–4715, which are measured in RASS. We considered also PSR 1929+10, PSR B0950+08, and PSR J2124–3358, which are not detected in RASS, but when brought nearer to 100 pc, would be detected with fluxes of  $10^{-13}$ – $10^{-11}$   $\text{erg s}^{-1} \text{cm}^{-2}$ . We adopted for PSR B0950+08 a 10 pc unabsorbed flux of  $5.65 \times 10^{-11}$   $\text{erg s}^{-1} \text{cm}^{-2}$  in the RASS 0.1–2.4 keV energy band, from deep X-ray Multi-Mirror Mission (*XMM-Newton*) observations (Becker et al. 2004), and for PSR J2124–3358 a 10 pc unabsorbed flux of  $5.43 \times 10^{-10}$   $\text{erg s}^{-1} \text{cm}^{-2}$  (sum of the thermal- and non-thermal contributions) in the X-ray soft 0.1–2 keV band (Becker 2009 and reference therein). Figure. 5 indicates that neutron stars at  $G < 21.4$  mag resembling (i) PSR J0437–4715 or PSR B0656+14 would be at less than about 40–50 pc, and those resembling (ii) RX J1856.5–3754, PSR B0950+08, or PSR J2124–3358 would be at less than about 20 pc.

On the other side, Fig. 5 indicates that power-law-source neutron stars of  $M_G = 19.5$  mag with no significant thermal emission would elude RASS detection if these are at more than 20 pc for  $\alpha_{\nu} = 1$  and at more than 5 pc for  $\alpha_{\nu} = 1.5$  (assuming a single power law from X rays to the optical).

For a more precise estimation, we produced Figs. 6 and 7, which represent the maximum distances of detectability as function of PS1  $g$ -band absolute magnitude, for different catalogues or surveys and power-law emitters of spectral index  $\alpha_{\nu} = -2.0, -1.0, -0.5, 0.0, 0.5, 1.0, 1.5, 2.0, 2.5,$  and  $3.0$ . The PS1  $g$  band is much narrower than the *Gaia*  $G$  band and is appropriate to anchor power-law components

<sup>2</sup> <https://www.astro.umontreal.ca/~bergeron/CoolingModels/>



**Figure 5.** X-ray flux versus  $G$ -band magnitude diagram. Thermal cooling tracks at distances other than 10 pc are represented by black dotted lines. Double square- or lozenge symbols are for 10 pc. The pulsar thermal track with rotochemical heating (violet dash-dotted line) is at 10 pc. The vertical dotted line at  $G = 21.4$  mag indicates the faintest apparent magnitude reached by *Gaia* DR3 sources of  $M_G > 16$  and  $snr_\pi > 2$ . As expected, the plot indicates that from 10 pc to 100 pc, the X-ray flux decreases by a factor  $10^{-2}$  and the  $G$ -band magnitude increases by 5 mag. Same as in Figs. 3 and 4.

identified in SEDs. From equation (3), we have the dependence between the distance- and magnitude limits:

$$d_{\text{lim}} = 10 \times 10^{0.2(m_{f,\text{lim}} - M_f)}, \quad (6)$$

where we can express the absolute magnitude  $M_f$  at any filter as a function of the absolute magnitude  $M_{f_0}$  at a reference filter (here PS1  $g$  band),

$$M_f = M_{f_0} + (M_{f,0} - M_{f_0,0}), \quad (7)$$

for an arbitrarily flux-scaled SED (subscript 0).

We adopted the following limits (usually point-source limits, see references for details): *X rays*: catalogue deep depth of  $10^{-15}$  erg s $^{-1}$  cm $^{-2}$  for *Chandra* at 0.1–10 keV, also applicable for *XMM-Newton* (Evans et al. 2010; Webb et al. 2020), and survey limit of  $2 \times 10^{-13}$  erg s $^{-1}$  cm $^{-2}$  for RASS at 0.1–2.4 keV (Boller et al. 2016); *Ultraviolet*: Galaxy Evolution Explorer (*GALEX*) typical  $5\text{-}\sigma$  detection depth of  $FUV = 19.9$  and  $NUV = 20.8$ -mag (Bianchi et al. 2017) and Sloan Digital Sky Survey (SDSS) 95 per cent completeness of  $u = 22.0$  mag (Albareti et al. 2017); *Wide optical*: *Gaia* 50 per cent completeness at  $G = 21.0$  mag (Gaia Collaboration et al. 2021b), PS1 stack  $5\text{-}\sigma$  detection depth of  $g = 23.3$ ,  $r = 23.2$ ,  $i = 23.1$ , and  $z = 22.3$  mag ( $\sim 50$  per cent completeness; Chambers et al. 2016); *Infrared*: representative  $5\text{-}\sigma$  detection depths of  $J = 20$  and  $K = 18.5$  mag (see references of near-infrared surveys in Section 3.1), and Wide-field Infrared Survey Explorer (*WISE*) 90 per cent completeness at  $W1 = 17.7$  mag (Marocco et al. 2021); *Radio*: 1.4 GHz NRAO VLA Sky Survey (NVSS) 90 per cent completeness at 3.0 mJy (Condon et al. 1998). We note that the catalogue- or survey limits are not necessarily homogenous over the covered sky regions.

We represented the *Gaia* sources as in Fig. 3, but using as distance the median of the posterior distance estimation from GCNS (dist\_50, hereafter  $d_{50}$ ), which is independent of colour (spectral type) or direction in the sky. The  $d_{50}$  of the 2464 sources is of  $80 \pm 18$  pc in average and in the range of 21–105 pc. Also we used  $g$ -band magnitudes from PS1, else from the National Optical-Infrared Astronomy Research Laboratory (NOIRLab) Source Cat-

alogue (NSC) (Nidever et al. 2021), or else from SDSS (see Section 3.1). Some UV candidates with power-law components (Table 2) and power-law profile sources (Table 5) are represented by horizontal- and vertical diamonds, respectively, in the plots of nearest spectral index. In Section 3.8, we briefly discuss these sources in the diagrams.

The diagrams of Figs. 6 and 7 adjust to modifications of source distances and search limits as follows. If a source is at a smaller or larger distance, it shifts to the left or to the right, respectively, as on detection-limit curves, implying that the detectability of the source is invariant to changes of the source distance (at fixed observed flux and negligible interstellar extinction). From equation (6), if another magnitude- or flux limit (with a prime) is chosen for a given filter, the corresponding distance limit simply changes by a factor of

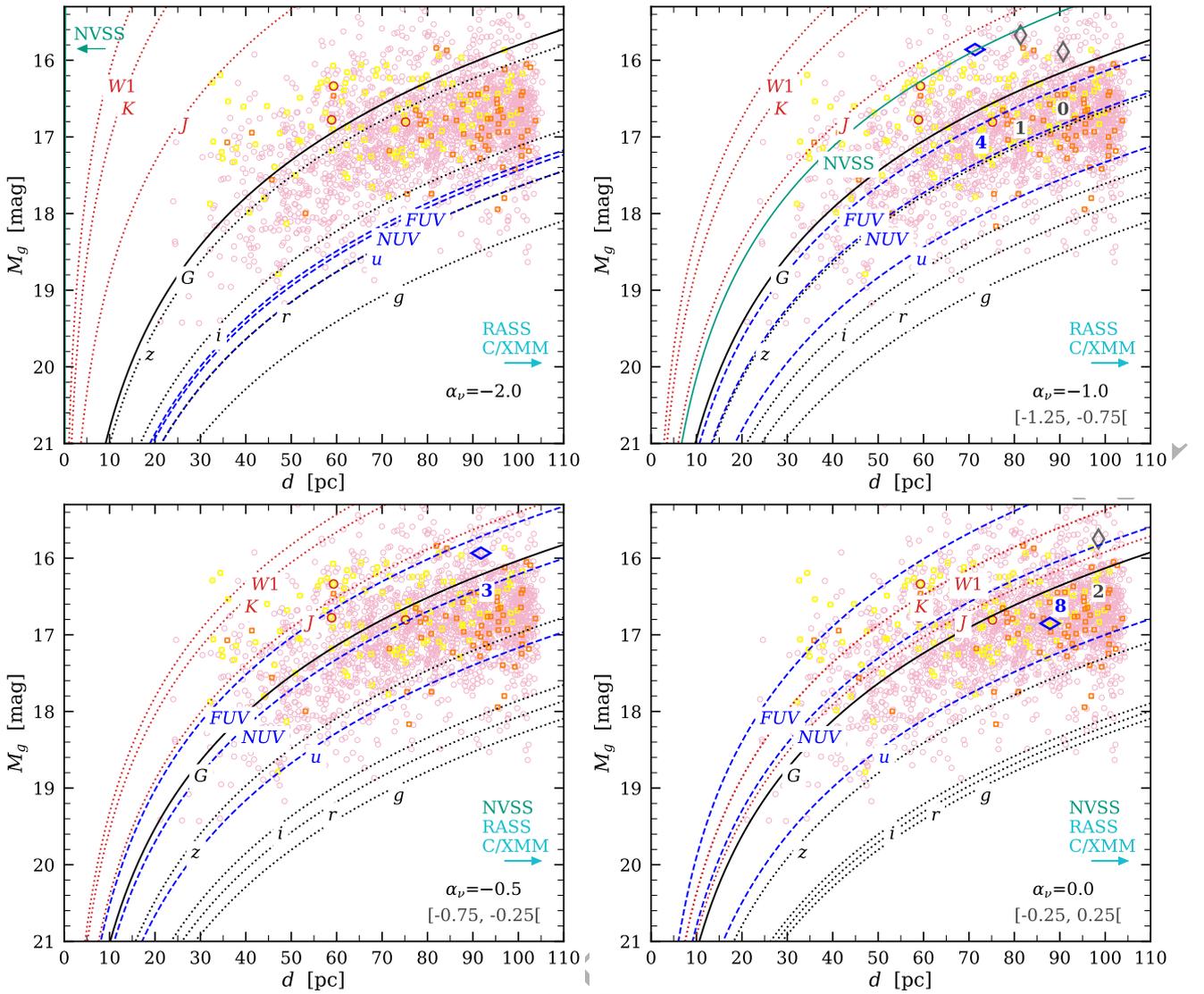
$$10^{0.2(m'_{f,\text{lim}} - m_{f,\text{lim}})} = (F'_{f,\text{lim}}/F_{f,\text{lim}})^{0.5}, \quad (8)$$

implying that the curves visible in the plots can easily be used to compute other search limits.

Bright, power-law-source neutron-stars of  $M_g = 16.50$  mag and  $\alpha_\nu = 1$  (i.e.  $M_G = 16.13$  mag, from Table 6) would be detected both in *Gaia* and at X rays in RASS up to 94 pc (Fig. 7). However those of  $\alpha_\nu = 1.5, 2.0, 2.5$ , and  $3.0$  ( $M_G = 15.99, 15.83, 15.67$ , and  $15.49$  mag) would be detected in *Gaia* up to 100, 108, 116, 128 pc, but not in RASS at  $d > 27, 8, 3$ , and 1 pc, respectively.

At ultraviolet, because of the shallower depth of the *GALEX* wide survey, the known pulsars that we considered can only be detected at less than 20–40 pc, as shown in the  $NUV$ - versus  $G$ -band magnitude-magnitude diagram of Fig. 9. Power-law-source neutron-stars of  $M_G = 19.5$  mag (with no significant thermal emission) would elude *GALEX* detection if these are at more than about 10 pc for  $\alpha_\nu \geq 1$  (assuming a single power law from the ultraviolet to the optical). From Fig. 7, if these have  $M_g = 16.5$  mag, then for  $\alpha_\nu = 1$  these would be detected up to 50 pc, whereas for  $\alpha_\nu = 1.5, 2.0, 2.5$ , and  $3.0$ , these would elude  $NUV$ -band detection at  $d > 41, 34, 29$ , and 24 pc, respectively.

To summarise, we see from Figs. 4, 5, 6, 7, and 9 that if young neutron stars including pulsars, which are still very hot and thermally



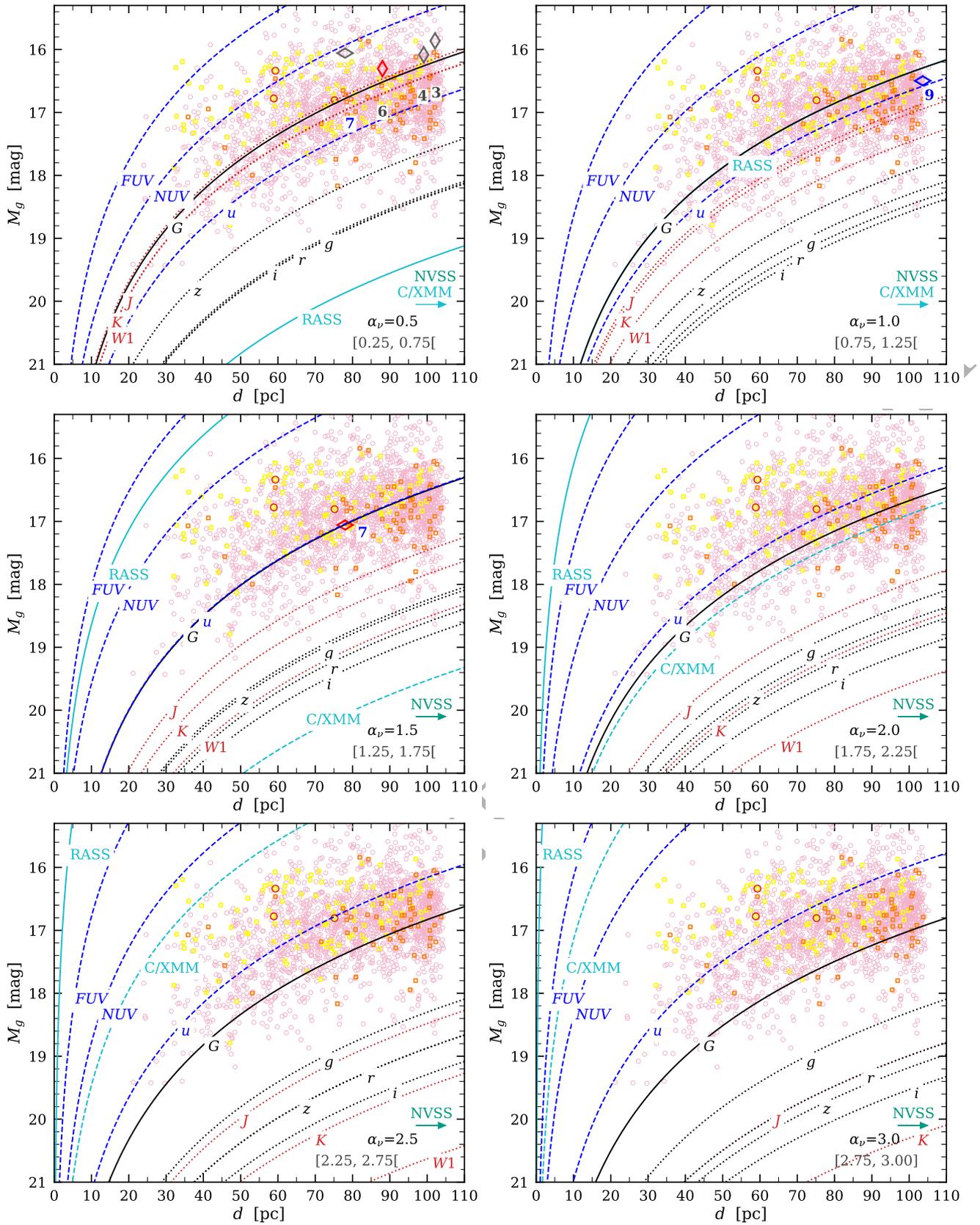
**Figure 6.** Detectability of nearby power-law emitters of spectral index  $\alpha_\nu = -2, -1, -0.5,$  and  $0$ , as a function of their absolute  $g$ -band magnitude. Catalogue- or survey limits are for (see text for details and references): *X rays*: *Chandra* 0.2–10.0 keV (or *XMM*) and RASS 0.1–2.4 keV (cyan dashed- and solid lines, respectively); *Ultraviolet*: *GALEX* *FUV*- and *NUV* bands, and SDSS *u* band (blue dashed lines); *Wide optical*: *Gaia* *G*- and PS1 *griz* bands (black solid- and dotted lines); *Infrared*: WFCAM *JK*- and WISE *W1* bands (red dotted lines); *Radio*: NVSS 1.4 GHz (green solid line). *Gaia* sources are represented as in Fig. 3, but using  $d_{50}$  distances and  $g$ -band magnitudes from PS1, else NSC, or else SDSS. Some ultraviolet- and power-law sources of Tables 2 and 5 are represented by horizontal- and vertical diamonds, in the plots of nearest spectral index (spectral index ranges are indicated at the bottom), and in grey, blue, or red depending on whether their power-law component was determined mostly from the optical, the ultraviolet, or the infrared, respectively.

emitting, are measured in *Gaia*, then they would be detected at X rays in RASS, and to a lesser extent, at *NUV* and *FUV* bands in *GALEX*. On the other hand, pulsar emitters with insignificant thermal emission and power law slopes  $\alpha_\nu \geq 1.5$  would remain undetected in RASS and *GALEX*, at strongly- and weakly decreasing distances for increasing spectral indices. This quantitative reasoning has some overlap with the interpretation of Maoz et al. (1997) that some of the red (and faint) optical sources they identify, using optical *B*- and *R*-band photometry, as candidate counterparts to extreme-ultraviolet sources without RASS X-ray detection, could be nearby neutron stars.

National Facility (ATNF) Pulsar Catalogue version 1.67<sup>3</sup> (Manchester et al. 2005), 315 are in binaries with a known companion type: about 50 per cent have low-mass He-core white dwarf companions and 15 per cent have higher-mass CO- or ONeMg-core white dwarf companions, as shown in Fig. 21, for the pulsars with measured orbital periods and projected semi-major axes. There is a confluence of neutron stars with white dwarfs, though it has not been explored thoroughly at medium to large binary separations. Based on this confluence, pulsars are searched as companions to white dwarfs (e.g. at radio wavelengths, Athanasiadis et al. 2021). If neutron stars are among our candidates and in binaries, then these will probably have white dwarf companions.

Finally, we note that among the 3320 pulsars of Australia Telescope

<sup>3</sup> <https://www.atnf.csiro.au/research/pulsar/psrcat/>



**Figure 7.** Same as Fig. 6, for power-law emitters of spectral index  $\alpha_\nu = 0.5, 1, 1.5, 2, 2.5,$  and  $3$ .

## 2.4 Crossmatches

Next, we crossmatch the coordinates of the 2464 *Gaia* sources of the colour-selected subsample with the coordinates of sources of broad-optical, infrared, gamma-ray, X-ray, radio, ultraviolet, and literature catalogues. We verify the crossmatch candidates in archival images and catalogues using the Aladin Interactive Sky Atlas tool. To better resolve the sources, especially for surveys of low spatial resolution, we query images in high-resolution mode in Aladin or in native pixel sizes with the embedded SkyView image selector.

## 3 RESULTS

### 3.1 Optical- and infrared crossmatches

At the broad optical, we consider the PS1-, SDSS- and NSC catalogues. Best-neighbour cross-identifications with PS1, SDSS, and the Two Micron All Sky Survey (2MASS [Skrutskie et al. 2006](#)) are provided in [GCNS](#) and are from the *Gaia* (E)DR3 external crossmatch tables (see description for *Gaia* DR2 in [Marrese et al. 2019](#)).

Cross-identifications with PS1 are available for 1419 of the 2464 *Gaia* sources. Using Aladin, we noted that the sources with very large proper motions of  $pm > 200 \text{ mas yr}^{-1}$  typically have more than one entry in the PS1 DR1 VizieR catalogue ([Chambers et al. 2016](#); CDS/II/349/ps1), corresponding to different trailing points defining the trajectory of the sources. Among the sources with  $pm > 100 \text{ mas yr}^{-1}$ , for eight with- and four without initial *Gaia*–PS1 cross-identification, we could recover identifications with the widest (*grizy*) bandpass coverage and the best astrometric- and photometric quality. Also, from a cone search within 1 arcsec of the *Gaia* sources, we could find 21 additional cross-identifications, of which one has  $pm = 90 \text{ mas yr}^{-1}$  and the others have  $pm = 3\text{--}20 \text{ mas yr}^{-1}$ , the latter ones being towards the Galactic plane and Bulge and mostly in blends. In total there are thus 1444 sources with PS1 photometry. Using the proper motions of the *Gaia* sources, we propagated their coordinates at epoch 2016.0 to the epochs of the PS1 crossmatches, obtaining same-epoch angular separations of  $0.10 \pm 0.11 \text{ arcsec}$  in average and smaller than 0.89 arcsec. Large separations appear typically for large proper motion sources or binary sources that are not resolved in PS1. We list the angular separations for sources of interest in [Tables E1 and E3](#) (column ‘Sep’). We did not update to PS1 DR2, because DR1 photometry is included in DR2 and 84 DR1 sources, mostly with incomplete bandpass coverage, are missing in DR2.

Cross-identifications with SDSS DR13 ([Albareti et al. 2017](#)) are available for 150 of the *Gaia* sources. The angular separations provided in the *Gaia* DR3 – SDSS external crossmatch table can easily be reproduced by propagating the coordinates to the epochs of the SDSS crossmatches. The angular separations are of  $0.11 \pm 0.08 \text{ arcsec}$  in average and smaller than 0.61 arcsec. Using Aladin, we verified that all of the sources with  $pm > 100 \text{ mas yr}^{-1}$  and in the SDSS catalogue footprint are already cross-identified. We list the angular distances for sources of interest in [Tables E2 and E4](#). For sources having ultraviolet *u*-band fluxes, we also derived the angular separations at *u*-band using the coordinates  $(ra + \text{offset}_{ra\_u}/3600/\cos_{\text{deg}}(\text{dec}), \text{dec} + \text{offset}_{\text{dec\_u}}/3600)$ , where  $\text{offset}_{ra\_u}$  and  $\text{offset}_{\text{dec\_u}}$  are the proper offsets in arcseconds provided in the SDSS catalogue.

For NSC DR2 ([Nidever et al. 2021](#)), we crossmatched using a search radius dependent of the proper motion:  $(pm \times \text{dyr})/1000 + \delta \text{ arcsec}$ , where (i)  $\text{dyr} = 4 \text{ yr}$  is the maximum epoch difference, given that the NSC observation epochs are within 2012.0–2020.0 yr, and (ii)  $\delta = 1.5 \text{ arcsec}$  is the minimum search radius. For the re-

sulting crossmatches, we then propagated the *Gaia* coordinates to the individual NSC epochs and we recomputed the angular separations. As for all the other crossmatches in this study, we omit to formalise the negligible propagated uncertainties caused by the very small coordinate errors (0.11–3.76 mas) and proper motion errors (0.23–4.38  $\text{mas yr}^{-1}$ ) of the *Gaia* sources; these are absorbed in the large search radii. Similarly as for PS1, 27 large proper motion sources have different trailing point measurements in NSC, and we selected the best (single or multiple) epochs of (complementing) widest bandpass coverage, whose *Gaia*–NSC angular separations are not necessarily the smallest but are smaller than 0.17 arcsec. We obtained matches for 2102 *Gaia* sources, with angular separations of  $0.16 \pm 0.16 \text{ arcsec}$  in average and smaller than 1.42 arcsec. The largest separations correspond to multiple sources that are not resolved in the seeing-dependent data of the NSC object catalogue, and may correlate with larger NSC values of semi-major axis radius, full-width-at-half-maximum, and non-stellar classification. We list the angular distances for sources of interest in [Tables E2 and E4](#). At declinations  $\delta > -29^\circ$ , the NSC DR2 photometry for the *grizY* bands are calibrated on the PS1 photometry. At  $\delta < -29^\circ$ , *griz* band photometry are calibrated on ATLAS-Refcat2 ([Tomry et al. 2018](#)). *u*-band photometry at  $\delta < 0^\circ$  are calibrated on SkyMapper DR1 ([Wolf et al. 2018](#)). Finally, *u*- and *Y*-band data are calibrated on model magnitudes at  $\delta > 0^\circ$  and  $< -29^\circ$ , respectively (see [Nidever et al. 2021](#) for details). For the SEDs, we assumed the same bandpass parameters as for SDSS *u*- and PS1 *grizy* bands, for simplicity.

In the *JHK<sub>s</sub>*-band near-infrared catalogue of 2MASS, only one *Gaia* source has a cross-identification, and it corresponds to a brighter- and unrelated source at 1.75 arcsec. We consider thus deeper near-infrared catalogues. Similarly as for the crossmatch with NSC, we crossmatched using  $\delta = 1.5 \text{ arcsec}$ , with the Visible and Infrared Survey Telescope for Astronomy (VISTA) Hemisphere Survey (VHS) DR6 ( $\text{d}y = 8 \text{ yr}$ ; [McMahon et al. 2013](#); [Sutherland et al. 2015](#)), United Kingdom Infrared Telescope (UKIRT) Hemisphere Survey (UHS) DR1 ( $\text{d}y = 3.621 \text{ yr}$ ; [Dye et al. 2018](#)), UKIRT Infrared Deep Sky Survey (UKIDSS) DR11PLUS Large Area Survey (LAS), Galactic Cluster Survey (GCS), and Galactic Plane Survey (GPS;  $\text{d}y = 10.671 \text{ yr}$ ; [Lawrence et al. 2007](#)), VISTA Magellanic Survey (VMC) DR6 ( $\text{d}y = 6.17 \text{ yr}$ ; [Cioni et al. 2011](#)), VISTA Variable in the Via Lactea Survey (VVV) DR5 ( $\text{d}y = 6 \text{ yr}$ ; [Minniti et al. 2010](#)), and VISTA Kilo-degree Infrared Galaxy (VIKING) Survey DR5 ( $\text{d}y = 6.14 \text{ yr}$ ; [Edge et al. 2013](#)) catalogues. Among the UHS-, VVV, and in particular the VHS matches, there were multiple matches from different observing epochs and at close angular separations, also for very small proper-motion sources, and we applied a complex selection accounting for magnitude errors, error flags, multiband coverage, and angular separation. We obtain counterpart numbers of 1170 (VHS), 284 (UHS), 23 (LAS), 24 (GCS), 219 (GPS), 76 (VMC), 228 (VVV), and 15 (VIKING), implying *ZYJHK<sub>s</sub>K*-band photometry for 1957 *Gaia* sources. From the VISTA and UKIRT catalogues, we used the *AperMag3* magnitude, which is the default point source aperture corrected magnitude (2.0 arcsec diameter). The UKIDSS Wide-Field Camera (WFCAM) filters are similar to the VISTA filters, though the *K* filter is shorter; overall, magnitude differences are typically smaller than 0.10 mag ([González-Fernández et al. 2018](#)). In [Table E1](#), we list the *JHK<sub>s</sub>*-band magnitudes next to the PS1 *y*-band magnitudes, and we indicate *ZY*-band magnitudes in the footnotes.

Also, similarly as for the crossmatch with NSC, we crossmatched using  $\delta = 1.75 \text{ arcsec}$  and  $\text{d}y = 6 \text{ yr}$  with the all-sky CatWISE2020 catalog, which is based on *WISE* and *NEOWISE* survey data at 3.4 and 4.6  $\mu\text{m}$  (*W1* and *W2*) obtained within 2010.0–2018.0 yr, and

which has a 90 per cent completeness depth at  $W1 = 17.7$  and  $W2 = 17.5$  mag (Marocco et al. 2021). There are 276 counterparts. We list the mid-infrared magnitudes for sources of interest in Tables E1 and E3. Most of the *Gaia* sources of the colour-selected subsample are not visible in *unWISE* images, because these are either too faint or unresolved in blends with brighter sources.

### 3.2 Gamma ray crossmatches

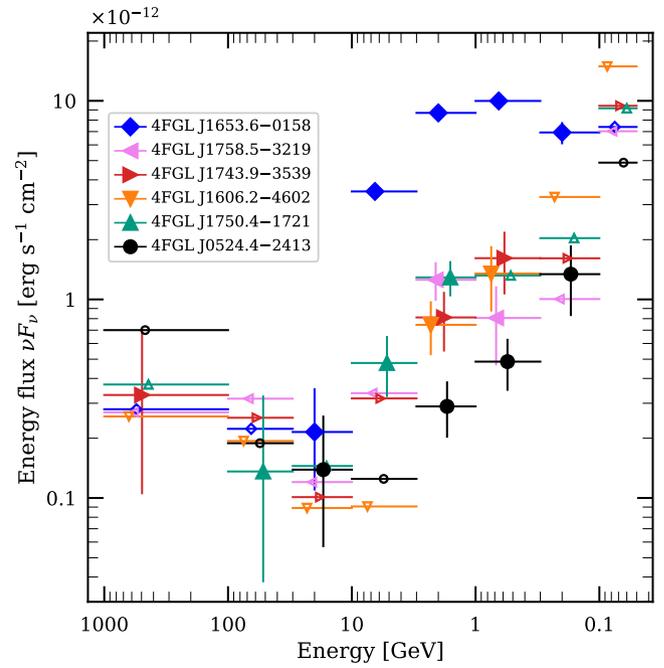
We crossmatched the J2016.0 coordinates of the *Gaia* sources with the coordinates of the 6659 point- and 78 extended sources of the *Fermi* Large Area Telescope Fourth Source Catalogue (4FGL-DR3; Abdollahi et al. 2022), and within the 4FGL confidence- and model positional error ellipses in the sky, respectively.

Within the 68 per cent confidence ellipses, there are five point-source matches. These have the following flags, (*Gaia* DR3, 4FGL) identifications, centroid separations and ellipse semimajor axes (in arcminutes), and total numbers of *Gaia* sources in the ellipses:

-  $\gamma\_a$ ; 4043369078205765888, J1758.5–3219; 7.48, 18.49; 203623,  
-  $\gamma\_b$ ; 4040994030072768896, J1743.9–3539; 9.28, 21.11; 211462,  
-  $\gamma\_c$ ; 5990998826943947520, J1606.2–4602; 18.49, 25.46; 78735,  
-  $\gamma\_d$ ; 4144738037302227072, J1750.4–1721; 3.13, 3.85; 10530,  
-  $\gamma\_e$ ; 2957941232274652032, J0524.4–2413; 17.07, 18.57; 6676.

The likelihood that these are true counterparts is of 4.91, 4.73, 12.7, 95.0, and 150 parts per million, respectively, that is extremely small. Nevertheless, we account for them exploratively and as reminders of the gamma-ray search perspective. Their *Gaia* parameters are listed in Table 7. At a later stage, we crossmatched within the 95 per cent confidence ellipses, because even the brightest 4FGL sources can have true counterparts that are beyond the 68 per cent confidence ellipses. There are 14 additional matches at 0.04–0.25 deg separation of point sources of 95 per cent confidence semimajor axes of 0.04–0.39 deg; to limit the scope of the paper, we did not study them further. Finally, there are 11 matches at 0.16–2.17 deg separation of gamma-ray extended sources of semimajor axes of 0.52–3.0 deg, which we did not consider further, because these are too extended or in crowded regions in the Magellanic Clouds. None of the above *Gaia* sources has also an X-ray- (or radio) counterpart (considering the crossmatches we present in the next Sections), which otherwise would have given it more weight.

The five *Gaia* sources of  $\gamma\_a$ – $\gamma\_e$  are in crowded stellar fields; the first four are at ( $|l| < 11^\circ$ ,  $|b| < 5^\circ$ ), in the foreground of the Galactic Centre, and the fifth ( $\gamma\_e$ ) is at  $(l, b) = (227.1986, -29.3487)^\circ$ , at 1.6 arcmin of the centre of the M 79 globular cluster (NGC 1904), of 4.8 arcmin radius. The average detection significance over the 100 MeV–1 TeV energy range ( $\text{Signif\_Avg}$ ) of  $\gamma\_a$ – $\gamma\_e$  is of 3.9–7.2  $\sigma$  and their spectrum type is log-parabola, except for 4FGL J0524.4–2413 that has a power-law spectrum type. In Fig. 8, we present their SEDs as a function of energy. Pulsar-type sources are identified in 4FGL as having curved- (log-parabola) or significantly curved (subexponentially cutoff power law) spectral shapes (Abdollahi et al. 2022). In Fig. 8, we represent also the 4FGL J1653.6–0158 black-widow millisecond pulsar, which has the typical gamma-ray pulsar properties of a time-stable photon flux and a highly curved spectrum (Nieder et al. 2020a,b). Two *Fermi* point sources have associations in the catalogue. 4FGL J0524.4–2413 has a high probability association with the above mentioned M 79 globular cluster, because the cluster is in the 68- and 95 per cent confidence ellipses (the gamma-ray centroid and cluster centre are separated by 17.1 arcmin). 4FGL J1606.2–4602 has a low confidence association with the ECC G334.57+04.63 source of unknown type. The five *Gaia* sources have red colours suggesting apparent temperatures of



**Figure 8.** SEDs of the gamma-ray point-source crossmatches and the 4FGL J1653.6–0158 millisecond pulsar. Data points at each energy band are slightly offset horizontally to increase visibility. Smaller symbols without vertical error bars are upper limits.

~3000–5500 K (see also the SEDs in Fig. G1, available as online supplementary material).

### 3.3 X ray crossmatches

At X-rays, we considered the second RASS source catalogue (2XRS;  $2 \times 10^{-13}$  erg s $^{-1}$  cm $^{-2}$ ; Boller et al. 2016), the *XMM-Newton* catalogues of serendipitous sources from observations (4*XMM* DR11;  $1 \times 10^{-15}$  erg s $^{-1}$  cm $^{-2}$ ; Webb et al. 2020) and stacked observations (4*XMM* DR11s, Traulsen et al. 2020), the *XMM-Newton* Slew survey catalogue (XMMSL2;  $3 \times 10^{-12}$  erg s $^{-1}$  cm $^{-2}$ ; Saxton et al. 2008), the *Chandra* Source Catalogue (Evans et al. 2010) Release 2.0 (CSC2.0;  $1 \times 10^{-15}$  erg s $^{-1}$  cm $^{-2}$ ), and the *eROSITA* Final Equatorial Depth Survey (eFEDS) X-ray catalogue ( $7 \times 10^{-15}$  erg s $^{-1}$  cm $^{-2}$ ; Brunner et al. 2022; Salvato et al. 2022), where the sensitivities are in the 0.5–2.0 keV energy range and adopted from fig. 14 in Brunner et al. (2022).

For convenience, we crossmatched the *Gaia*- and X-ray sources in two steps. In the first step we used a constant crossmatch radius, defined by the template expression  $(pm_{\max}/1000) dyr + n \sigma_{\text{pos},r} + \delta$  arcsec, where  $pm_{\max}$  is the maximum proper motion in our *Gaia* subsample,  $dyr$  is the absolute value of the epoch difference between *Gaia* DR3 and the farthest- or representative epoch of the counterpart catalogue,  $\sigma_{\text{pos},r}$  is the maximum- or representatively-large positional uncertainty in the counterpart catalogue,  $n$  is an integer factor of  $\sigma$ , and  $\delta$  is to allow for any unaccounted systematic- or source-centroiding uncertainty. In the second step, we required the crossmatches to have angular separations smaller than  $(pm/1000) dyr + n \sigma_{\text{pos}} + \delta$  arcsec, using the individual measurements.

For the *Chandra* CSC2.0 catalogue, we used  $dyr = 16.25$  yr,  $\sigma_{\text{pos},r}$  as the maximum of the major radius of the 95 per cent confidence-level position error ellipse,  $n = 2$ , and  $\delta = 2$  arcsec.

**Table 1.** X-ray crossmatches.

Flag	$Plx$ (mas)	$\mu_{\alpha}^*$ (mas yr $^{-1}$ )	$\mu_{\delta}$ (mag)	$G$ (mag)	$BP - G$ (mag)	$G - RP$ (mag)	$g - r$ (mag)	$r - i$ (mag)	$i - z$ (mag)	P	Sep ( $\prime$ )	L (%)	Rate (cts/s)	HR1	HR2
P1X1	13.3±2.0	-0.2	-1.5	20.61	-0.33±0.08	0.64±0.17	-0.24	-0.21	-0.02	1	44.1	20.0	0.0290±0.0105	1.00±0.50	0.38±0.31
X2	16.1±0.6	99.0	-164.9	20.51	0.19±0.08	0.56±0.09	0.63	0.13	0.13	2	47.7	16.7	0.0313±0.0135	-0.46±0.36	1.00±0.62
X_a	12.3±2.0	4.1	-1.7	20.81	0.25±0.13	0.88±0.10	0.68	0.41	0.10	2	35.0	1.6	0.3833±0.0504	0.95±0.04	0.21±0.09
X_b	21.9±2.1	-12.5	11.7	20.43	0.42±0.11	0.85±0.07	0.63	0.34	0.18	2	37.5	0.5	0.0484±0.0164	0.33±0.21	-0.04±0.28
X_c	16.8±1.9	-6.2	3.7	20.28	0.04±0.12	0.91±0.14	0.51	0.22	0.11	2	42.7	0.3	0.1066±0.0235	1.00±0.11	0.38±0.17
X_d	12.1±2.0	-4.1	-3.7	20.72	0.18±0.15	0.88±0.08	0.70	0.38	0.14	1	57.3	5.0	0.0182±0.0082	1.00±0.41	-0.89±0.26
X_e	13.7±1.6	-8.1	-5.8	20.67	0.15±0.17	0.78±0.13	–	–	–	–	54.3	1.0	0.0441±0.0189	1.00±2.44	-1.00±0.83

$\mu_{\alpha}^*$  stands for  $\mu_{\alpha} \cos \delta$ . Sep is the separation (arcsec) at epoch 1991 between the *Gaia*- and 2RXS centroids.  $L$  is a counterpart likelihood, as the inverse of the number of *Gaia* sources at epoch 1991 within Sep+0.05 arcsec of the X-ray source. The *griz*-band photometric (P) colours are from PS1 (1) and NSC (2). Proper motion component errors are of 0.5–2.3 mas yr $^{-1}$ . From top to bottom, the names of the X-ray sources are: (1) 2RXS J003745.3+440747, (2) 2RXS J210253.8–583920, (3) 2RXS J171535.3–545013, (4) 2RXS J165504.0–304049, (5) 2RXS J165739.0–294945, (6) 2RXS J000819.5+423453, (7) 2RXS J171902.3–603235. The 2RXS hardness ratios HR are defined as HR = (hard - soft)/(hard + soft) with HR1 =  $(H - S)/(H + S)$  and HR2 =  $(V - M)/(V + M)$ , where the  $S$  (soft),  $H$  (hard),  $M$  (medium), and  $V$  (very hard) bands correspond to 0.1–0.4, 0.5–2.0, 0.5–0.9, and 0.9–2.0 keV.

In the first step, 56 matches are found. In the second step, one remains. *Gaia* DR3 4108419965650416128 ( $pm = 4.8$  mas yr $^{-1}$ ) is in a very dense field and at 64 arcsec of the faint ( $SNR_X = 2.4$ ) 2CXO J171032.0–281942 ( $\sigma_{pos} = 43$  arcsec), whose centroid is at 4 arcsec of the optically bright CD–28 12887 star ( $G = 10.1$  mag). Considering also that within 65 arcsec of the X-ray source there are 916 *Gaia* sources, implying a very small counterpart likelihood of  $L = 0.0011$ .

For the *XMM* catalogues, we used  $d_{yr} = |2000 - 2016| = 16$  yr,  $\sigma_{pos,rl}$  as the maximum of the positional 1-sigma uncertainty in the respective *XMM* catalogues,  $n = 3$ , and  $\delta = 2$  arcsec. We find four matches, which are in dense stellar fields. We propagated the coordinates of the *Gaia* sources using their proper motions ( $pm < 15$  mas yr $^{-1}$ ) to the mean epochs of the respective *XMM* matches. *Gaia* DR3 4685846291048239744 is at  $3.58 \times \sigma_{pos}$  of 4XMM J004425.7–732635 ( $\sigma_{pos} = 1.43$  arcsec) of low detection significance ( $SC\_DET\_MIL = 9.3$ ), which has seven *Gaia* sources within  $3.58 \times \sigma_{pos}$ . *Gaia* DR3 4124307015366667776 is at  $3.03 \times \sigma_{pos}$  of 4XMM J173204.2–170613 ( $\sigma_{pos} = 2.83$  arcsec), which has 15 *Gaia* sources within  $3.03 \times \sigma_{pos}$ . *Gaia* DR3 6029397037233478400 is at  $1.04 \times \sigma_{pos}$  of 4XMM J170238.7–295445 ( $\sigma_{pos} = 17.70$  arcsec), which has 79 *Gaia* sources within  $1.04 \times \sigma_{pos}$  and has an extent of  $37.20 \pm 4.71$  arcsec. Finally, *Gaia* DR3 4124500048336584064 is at  $1.41 \times \sigma_{pos}$  of XMMSL2 J173139.7–165636 ( $\sigma_{pos} = 10.69$  arcsec) of low detection significance ( $DET\_ML\_B8 = 9.2$ ), which has 27 *Gaia* sources within  $1.41 \times \sigma_{pos}$ . The four matches have very small counterpart likelihoods of 0.143, 0.067, 0.013 and 0.037, respectively.

We proceeded similarly with the *ROSAT* 2XRS catalogue, with  $d_{yr} = 25.5$  yr,  $n = 3$ , and  $\delta = 3$  arcsec. We adopt  $\sigma_{pos,rl} = \sigma_{pos} = 20$  arcsec as a representatively large value, based on the comparison of 2XRS- with SDSS positions (Boller et al. 2016) and because there are no formal 2XRS positional errors available. In the first step, there are 26 matches. In the second step, seven remain, which are listed in Table 1. Also listed are (i) the angular separation (Sep) at epoch 1991 and (ii) the counterpart likelihood (L), as the inverse of the number of *Gaia* sources at epoch 1991 within Sep+0.05 arcsec of the X-ray source.

*Gaia* DR3 387812285286341504 (P1X1;  $d_{50} = 81$  pc) is in a sparse field and 44.1 arcsec south of the centroid of the faint 2RXS J003745.3+440747. Considering the faintness, uncertain centroid and spread ( $\leq 30$  arcsec), and the pixel locations of the soft and hard counts of the RASS source, the *Gaia* source could be a potential match. Also, the *Gaia* source has low counts in the *GALEX* GR6+7

*NUV*- and *FUV*-band images. Comparing these counts with those of *GALEX* J003744.6+440750 ( $FUV = 20.1 \pm 0.25$  and  $NUV = 19.61 \pm 0.13$  mag) 47.4 arcsec north, it would have  $NUV \sim FUV \sim 20.8 \pm 0.4$  mag, implying  $FUV - NUV \sim 0$  and  $NUV - G \sim 0.2$  mag. Among the seven 2RXS matches, P1X1 has the smallest proper motion ( $pm \sim 1.5 \pm 2.4$  mas yr $^{-1}$ ) and the bluest  $G_{BP} - G$  and PS1 colours. Its blue  $G_{BP} - G$  and very red  $G - G_{RP} = 0.64 \pm 0.17$  mag are reflected in its positive `phot_bp_rp_excess_factor` corrected of 0.58 (see comments on this parameter in Appendix A). Its SED based on the PS1 photometry indicates an almost straight profile over the *griz* bands, with some excess at *zy* band (Fig. 13; see Section 3.7 for details about SEDs and the fitting procedure). Among all the *Gaia* sources of the colour-selected subsample that have PS1 *griz*-band photometry and a spectral-index fitting error smaller than 0.1, it is the only source with a spectral index lesser than zero,  $\alpha_V = -0.86 \pm 0.07$ , and has the highest value of the renormalised unit weight error (`ruwe`) for astrometry, of 7.6 (also the third greatest `ruwe` value in the colour-selected subsample). A value of `ruwe`  $\gtrsim 1.4$  is indicative of an ill-behaved astrometric solution and may indicate binarity or multiplicity (Gaia Collaboration et al. 2021b). Within 44.15 arcsec of the 2RXS centroid and at epoch 1991, there are five *Gaia* sources ( $G = 18.20 - 20.61$  mag), among which P1X1 is the only one with a negative  $G_{BP} - G$  colour (it has also the bluest  $g - r$  colour among the PS1 sources in that area), is the faintest ( $G = 20.61$  mag), and its `ruwe` value is much greater than those of the four other sources (1.0). However *GALEX* J003744.6+440750 is also a potential match at 8.4 arcsec of the 2RXS centroid; it is relatively brighter in the optical (*Gaia* DR3 387812869401900672;  $G = 19.15$ ,  $G_{BP} - G = 0.14$ ,  $G - G_{RP} = 0.29$  mag) and mid infrared, and has a 100 per cent probability of being extragalactic as a quasi stellar object (QSO), in the Northern Extragalactic *WISE*  $\times$  Pan-STARRS (NEWS) catalogue (Khrantsov et al. 2020).

*Gaia* DR3 6456175155513145344 (X2) is in a sparse field and 47.7 arcsec north of the uncertain centroid of the faint 2RXS J210253.8–583920 source. The *Gaia* source has  $G = 20.51$  mag, a large proper motion of  $(99, -165) \pm 0.5$  mas yr $^{-1}$ , and is at  $d_{50} = 62$  pc. It is in GCNS100pc and is a probable white-dwarf photometric candidate (GCNS; Gentile Fusillo et al. 2021). At less than 47.75 arcsec of the 2RXS centroid and at epoch 1991, there are six *Gaia* sources ( $G = 12.04$  and  $20.21 - 21.00$  mag). Among these, X2 has the bluest  $G_{BP} - G_{RP}$  colour, of 0.75 mag. In the Dark Energy Survey (DES) DR1 catalogue (Abbott et al. 2018), X2 corresponds to DES J210255.98–583838.3, with colours of  $g - r = 0.79$ ,  $r - i = 0.23$ , and  $i - z = 0.07$  mag suggesting a cool atmosphere.

**Table 2.** Ultraviolet crossmatches.

Flag	$Plx$ (mas)	$\mu_{\alpha^*}$ (mas yr <sup>-1</sup> )	$\mu_{\delta}$ (mag)	$G$ (mag)	$BP - G$ (mag)	$G - RP$ (mag)	$g - r$ (mag)	$r - i$ (mag)	$i - z$ (mag)	P	Sep ( $\prime\prime$ )	L	$FUV - NUV$ (mag)	$NUV - G$ (mag)	$u - G$ (mag)
UV1	10.6±1.7	-15.8	-3.9	20.89	-0.35±0.13	0.35±0.15	-0.37	-0.25	-0.27	2	0.3	1	0.21±0.41	-0.31±0.23	–
UV2	17.3±1.5	-1.4	-7.1	20.17	-0.25±0.08	0.71±0.10	0.26	0.11	0.02	1	1.6	1*	–	1.98±0.34	–
UV3	12.2±2.0	-1.5	2.6	20.89	-0.19±0.17	0.80±0.15	-0.19	–	–	2	2.2	1	-0.34±0.25	-0.66±0.15	–
UV4	14.4±1.2	1.6	-9.0	20.23	-0.10±0.06	0.83±0.06	-0.13	0.34	0.22	1	0.7	1*	-0.47±0.11	-0.78±0.06	–
UV5	11.9±3.2	-2.6	-2.3	20.90	-0.05±0.16	0.47±0.26	0.30	–	–	2	3.0	0.5	–	1.82±0.40	–
UV6	17.3±1.6	-0.7	-13.4	20.12	-0.04±0.05	0.79±0.05	0.33	0.11	0.05	1	1.7	1	–	1.89±0.36	–
UV7	13.4±1.4	-10.0	3.1	20.56	-0.03±0.10	0.81±0.10	0.08	0.22	0.00	2	1.9	1	–	1.34±0.35	–
UV8	13.0±2.3	-5.9	14.7	20.86	0.15±0.26	0.88±0.15	0.47	0.88	0.52	1	1.9	1	–	0.93±0.35	0.11±0.13
UV9	10.5±3.8	2.3	7.8	20.89	0.26±0.15	0.85±0.13	0.40	0.67	0.55	1	0.9	1	–	1.60±0.28	0.42±0.16
UV10	12.6±2.8	-6.3	-9.5	20.89	0.26±0.17	-0.12±0.30	-0.08	-0.23	0.04	1	0.6	1	-0.41±0.37	1.07±0.26	–
UV11	12.3±3.5	-11.7	-12.9	20.86	0.35±0.28	0.55±0.22	0.51	0.20	0.17	1	1.5	0.5	–	1.10±0.32	1.96±0.55
UV12	13.7±2.9	-4.2	-14.6	20.70	0.36±0.14	0.43±0.19	0.33	0.17	0.08	1	1.5	1*	–	1.73±0.43	1.06±0.19
UV13	15.3±0.7	210.3	149.6	20.19	0.48±0.09	0.53±0.07	0.99	0.24	0.14	1	0.1	1	–	–	-0.31±0.10
UV14	12.7±0.8	195.0	40.2	20.51	0.49±0.15	0.81±0.08	0.89	0.39	0.13	1	0.0	1	–	–	1.17±0.30
UV15	11.6±1.3	100.2	-158.2	20.75	0.58±0.16	0.69±0.11	0.73	0.09	0.24	1	0.6	1	–	–	0.40±0.19

Notes. Proper motion component errors are of 0.5–2.7 mas yr<sup>-1</sup>. The *griz*-band photometric (P) colours are from PS1 (1) and NSC (2). Sep is the separation (arcsec) between the *Gaia*- and (i) *GALEX* centroids at the *GALEX* epochs for UV1–12, and, (ii) SDSS DR13 *u*band centroids at the SDSS epochs for UV13–15. *L* is the counterpart likelihood, as the inverse of the number of unique *Gaia*-, PS1-, and NSC sources within  $3 \times \sigma_{\text{pos}}$  of the ultraviolet source at its epoch. \* Likelihood shared with a visual companion at 0.6 arcsec (i) with separate *Gaia* parameters (UV2 in Table 8) or (ii) only partly resolved in PS1 images (UV4, UV12), and whose relative separation is indicated in column ‘Vis.’ of Table 9.

Within 5.5 arcsec, it has five DES neighbours and it is the second brightest. Its large proper motion can easily be seen in NOIRLab image tiles from 2013 to 2018. (We note that within 47.75 arcsec of the 2RXS centroid, there are 55 NSC sources, which would decrease the counterpart likelihood). The brightest *Gaia* source is *Gaia* DR3 6456175048138766720 ( $G=12.04$  mag, 25.8 mas yr<sup>-1</sup>, 350 pc;  $NUV = 17.84 \pm 0.04$  mag), at 29 arcsec of the 2RXS centroid. It could also be a potential match, because it is an EW–W Ursae Majoris-type eclipsing variable (Richards et al. 2012), a contact binary of orbital period of 0.3456 d (Drake et al. 2017).

For the possible P1X1 and X2 candidates, we converted the 2RXS count rates to fluxes, adopting a conversion factor of  $1.08 \times 10^{-11}$  erg s<sup>-1</sup> cm<sup>-2</sup> for an intrinsic hydrogen column density  $N_H = 0$  and a power-law emission of photon index  $\Gamma = 1$ , and we represent them by blue circles in Figs. 4 and 5.

The five remaining 2RXS matches are located in dense fields close to the plane or centre of the Galaxy, with very small counterpart likelihoods of 0.003–0.05. The relatively bright 2RXS J171535.3–545013 (X\_a match) is associated, as an AGN candidate, with 2MASS 17153752–54500621 at 20 arcsec and the 2SXPS J171537.7–545007 *Swift* X-ray point source (Edelson & Malkan 2012; Tranin et al. 2022). Similarly, the relatively bright 2RXS J165739.0–294945 (X\_c match) can be associated with the 2SXPS J165739.6–294926 AGN candidate (Tranin et al. 2022), at 20 arcsec and in the opposite direction to the X\_c *Gaia* source.

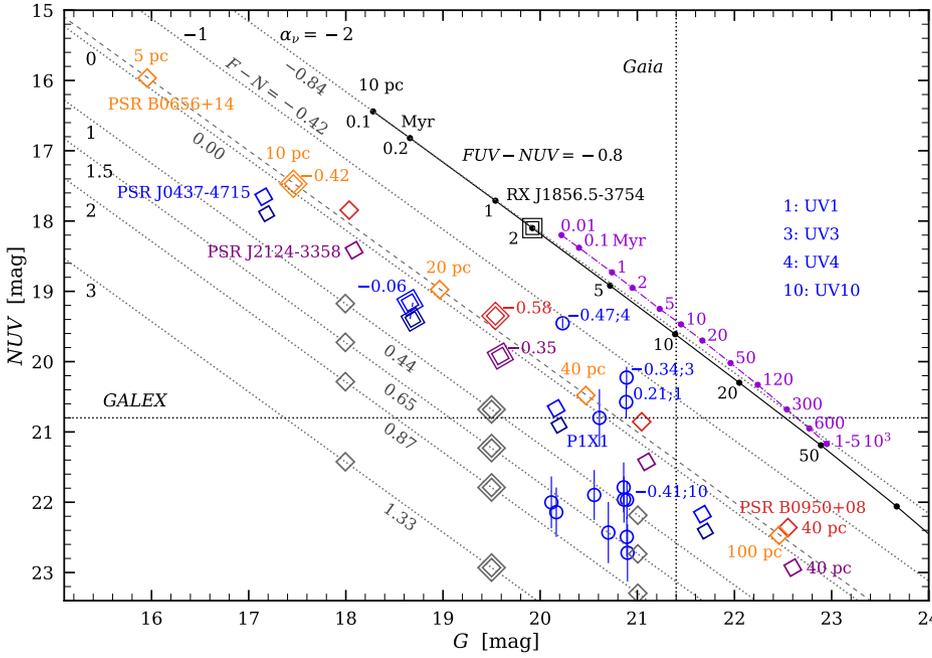
For the eFEDS catalogue, we used  $d_{yr} = 4$  yr,  $\sigma_{\text{pos,rl}}$  as the maximal positional uncertainty,  $n = 3$ , and  $\delta = 3$  arcsec. We find one match. *Gaia* DR3 5763109404082525696 has a proper motion of (-114, 86) mas yr<sup>-1</sup>,  $G/G_{BP}/G_{RP} \approx 20.4$  mag,  $d_{50} = 62$  pc, and is a probable white-dwarf photometric candidate in GCNS100pc and Gentile Fusillo et al. (2019). At the eFEDS epoch, it is at 28.0 arcsec of the centroid of the faint eFEDS J091001.1–022226 ( $\sigma_{\text{pos}} = 16.3$  arcsec), of X-ray count rate of 0.044±0.020 cts/s. The crossmatch likelihood is of 0.5, because there is another *Gaia* counterpart, closer at 11 arcsec and brighter in the optical ( $G = 17.6$  mag) and infrared (2MASS 09100156–0222173).

### 3.4 Ultraviolet crossmatches

At the ultraviolet, we considered the *GALEX* All-Sky Survey GU-Vcat\_AIS GR6+7 catalogue (Bianchi et al. 2017). We propagated the coordinates of the *Gaia* sources to epoch 2008.0, midst of the *GALEX* 2003–2013 epoch range. We then proceeded similarly as for the X-ray crossmatches, with  $d_{yr} = 4.5$  yr,  $\sigma_{\text{pos,rl}} = 3$  arcsec as the maximum positional uncertainty at *NUV*- and *FUV* bands,  $n = 3$ , and  $\delta = 3$  arcsec. The second step yields 38 matches. After visual inspection in archival images, we find 12 true- or probable matches (Table 2). These are all in sparse stellar fields, with typically no other *Gaia* source within 10 arcsec of the *GALEX* centroid (except for UV4 that has five other *Gaia* sources). The 26 remaining matches were discarded, because, the ultraviolet sources (i) have brighter- and closer optical sources that match their coordinates, or (ii) are too far off, given the relatively precise coordinates and proper motions.

The angular separations of the 12 matches at the respective *GALEX* epochs are listed in Table 2. Expressed in multiples of  $\sigma_{\text{pos,NUV}}$ , these are of 0.4–1.0 (five sources), 1.0–1.5 (five sources), 2.4 (UV5), and 3.2 (UV3). Some ultraviolet positional scatter could be explained by the larger pixel size, detector field distortion, and centroiding at faint fluxes. The ultraviolet sources come from coadds (multiple visits), are classified as point source, and have artefact- and source extraction flags of value 0 for the retrieved *FUV* and *NUV* measurements, except for three sources, which have non-zero artefact flags that are not among those causing real concern (Bianchi et al. 2017). *Gaia* DR3 6901051613248041216 (UV4) and *Gaia* DR3 4438623270475014656 (UV11) have both an *NUV*-band artefact flag  $N_{\text{afl}}$  of 17, that is of 1 and 16 indicating a detector bevel edge reflection and a bright star near the field edge, respectively. The first candidate is very bright at *FUV*- and *NUV* bands and the latter candidate is only detected faint at *NUV* band. *Gaia* DR3 837736394742229248 (UV9) has an *NUV*-band source-extraction flag  $N_{\text{exf}}=2$ , though the source is well isolated.

In the *NUV* versus *G* magnitude–magnitude diagram of Fig. 9, we show the 12 candidates, which have  $G = 20.1 - 20.9$  mag and are at  $d_{50} = 60 - 104$  pc. *Gaia* DR3 5777941133043108992 (UV3) and UV4, are well above the equal-magnitude line (grey dashed line),



**Figure 9.** NUV- versus  $G$ -band magnitude diagram. The grey dashed line represents equal magnitudes. Synthetic  $FUV - NUV$  colours of known neutron stars are indicated next to their 10 pc magnitudes. The neutron-star thermal cooling track is shown only at 10 pc, because the tracks at other distances are overlapping with it. The pulsar thermal track with rotochemical heating, also at 10 pc (violet dash-dotted line), is offset in  $G$  band by +0.15 mag for clarity. The *GALEX* crossmatches are indicated by blue open circles, annotated with measured  $FUV - NUV$  colours. The oblique grey dotted lines are for power law sources and are annotated with synthetic  $FUV - NUV$  colours (more colour values are in Table 6). Same as in Fig. 5.

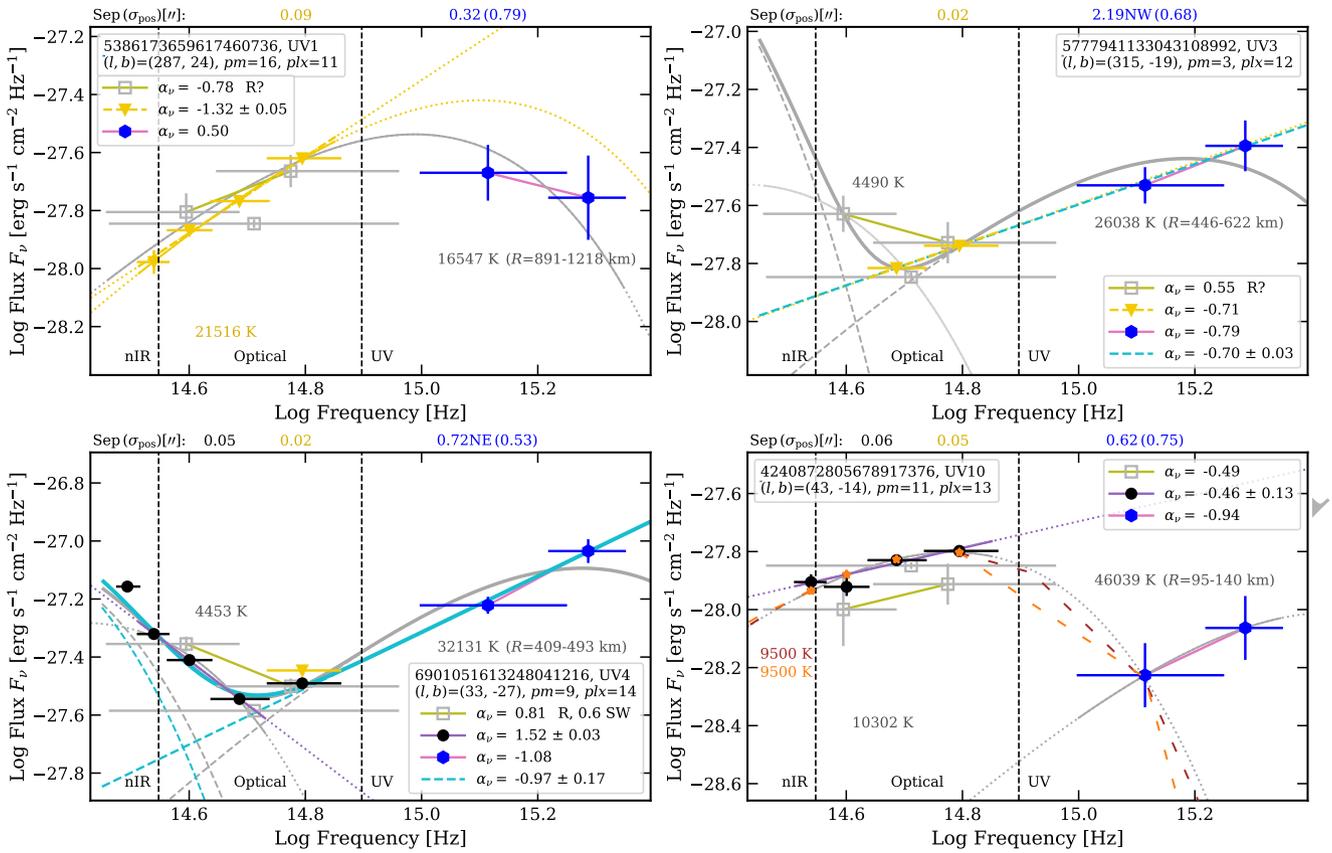
and their location and blue  $FUV - NUV$  colours are consistent with power law profiles of  $\alpha_\nu \approx -1$ . The nine sources well below the equal-magnitude line are located at  $NUV - G$  colours of power-law profiles of  $\alpha_\nu = 0.5 - 2.0$ . Their profiles can be verified with fluxes at narrower bands than the  $G$  band (and with the  $FUV$  band flux in the case of UV10).

In Fig. 10, we show the SEDs of the four candidates having  $FUV$  and  $NUV$  fluxes, Gaia DR3 5386173659617460736 (UV1), UV3, UV4, and Gaia DR3 4240872805678917376 (UV10). These have distances  $d_{50} = 101, 92, 71,$  and  $93$  pc, respectively. None is a white dwarf photometric candidate in catalogues. The SED profile of UV1 (the source above- and closest to the  $NUV = G$  line in Fig. 9) can be approximately fitted by a single hot blackbody, represented by the grey solid line. Alternatively, the profile could consist of (i) a component that is straight-up in the optical, peaking at  $g$  band, and significantly suppressed at  $u$  band, such as the profile of the Gaia DR3 1528861748669458432 DC white dwarf (Fig. 14), and (ii) another component that is related to the ultraviolet emission. UV3 is well fitted at optical-ultraviolet by a power law of  $\alpha_\nu = -0.7$ ; its bright infrared fluxes and red *Gaia* colours indicate that it has a cool companion (the full SED is available in Fig. G3 of the online supplementary material). Similarly, UV4 is well fitted at optical-ultraviolet by a power law of  $\alpha_\nu = -1.0 \pm 0.2$ , summed with a cool blackbody (straight- and leftmost cyan dashed lines, respectively, in Fig. 10, where the cyan thick solid line is the sum). Assuming unbroken power laws, these are expected to be detected at X rays in 2RXS RASS, as indicated in Fig. 6, in the panels for  $\alpha_\nu = -0.5$  and  $-1.0$ . However these are not detected, possibly because the exposure times (as indicated by the 2RXS exposure map) are of only about 130 and 280 s, respectively, close to the minimum exposure time (Boller et al. 2016). Both sources could be binaries. UV3 has a very small proper motion, possibly related to it being binary, faint, or a QSO; it appears as a point-source in *GALEX*. In the case of UV4, the cool component stems from a blended visual companion, 0.6 arcsec south-west of the *Gaia* source. The ultraviolet emission is very bright, extends from the *Gaia* source up to a few arcsec in radius, and appears as a hot nebula or bubble. The blue-optical-ultraviolet fluxes of UV3 and UV4 are better fitted by power-laws than blackbodies,

and the blackbody fits suggest hot temperatures near  $\sim 30\,000$  K. Finally, UV10 has fluxes indicating a hot optical source of  $\sim 10\,000$  K with a slightly lower ultraviolet emission. Assuming that the optical component, of blue slope, has a significantly suppressed  $u$ -band flux (as for Gaia DR3 1528861748669458432 in Fig. 14), and that the ultraviolet component stems entirely from another source that emits thermally, then the latter would have a temperature of  $\sim 45\,000$  K.

Gaia DR3 3150537594577224960 (UV8), UV9, and UV11 have significant  $NUV$ -band flux excesses. Their  $d_{50}$  distances are of 88, 104, and 96 pc and their proper motions of 16, 8, and 17  $\text{mas yr}^{-1}$ , respectively. None is a catalogue white dwarf photometric candidate. The SEDs of UV8 and UV9 (Fig. 18) consist both of a (i) relatively bright, red, and ultra-cool component ( $T_{\text{eff}} < 3250 \pm 230$  K) and (ii) a blue, power-law- or hot blackbody component; we discuss these in detail in Section 4.2.1. UV11 is a cool source ( $T_{\text{eff}} \sim 5250$  K) with a very low  $u$ -band flux compared to the  $NUV$ -band flux (Fig. 11). In fact, the centroid of the *GALEX* source ( $\sigma_{\text{pos}} = 1.41$  arcsec; count spread of about 2 arcsec) is 1.5 arcsec north-east of the *Gaia* source and 2.4 arcsec south-east of the centroid of an extended galaxy or nebula (SDSS J162911.33+055225.9), which are both clearly resolved and bright in a NOIRLab  $u$ -band stack image. The counterpart likelihood for UV11 is thus of 0.5.

The five remaining *Gaia* sources with a *GALEX* counterpart are Gaia DR3 6829498931265990656 (UV2), Gaia DR3 6585452983927662080 (UV5), Gaia DR3 6858721824326705536 (UV6), Gaia DR3 6529021095092491648 (UV7), and Gaia DR3 4465431356821050496 (UV12). These appear to have blackbody profiles peaking at the red-optical-near-infrared and a low  $NUV$ -band flux excess relative to the blackbody extrapolation (UV7 is shown as example in Fig. 11; the others are shown in Fig. G3 of the online supplementary material). Their  $d_{50}$  distances are of 60–98 pc. UV2, UV6, and UV12 have high values of *Gaia* photo-astrometric parameters associated with binarity (see Table 9 and Section 4.2.2). UV5 and UV7 have no- and slight photo-astrometric indication of binarity, respectively. The SED of UV7 has a clear power-law component when infrared fluxes are taken into account (Fig. 18), which we discuss in detail in Section 4.2.1. UV5 has a counterpart likelihood of 0.5, because the *GALEX* centroid ( $\sigma_{\text{pos}} = 1.25$  arcsec) is



**Figure 10.** SEDs of the four candidates with *GALEX* *FUV* and *NUV* fluxes, UV1, UV3, UV4, and UV10. The *Gaia* DR3 source ID, galactic coordinates in deg, proper motion in  $\text{mas yr}^{-1}$ , parallax in mas, and photo-astrometric- and visual-companion binary indicators (columns ‘Ast.’ and ‘Vis.’ in Table 9) are indicated in the legend boxes. The  $\Delta \log F_\nu$  ordinate span is of 1.2 dex, else if it is greater, it is explicit. In general, also for the next SED figures, *Gaia*, PS1, SDSS, NSC, *GALEX*, and additional infrared fluxes are represented by grey squares, black dots, blue upward triangles, yellow downward triangles, blue hexagons, and red open circles, respectively. Above the top axis, we indicate the angular separations in arcsec between the counterpart and the *Gaia* source at the mean observation epoch of the counterpart; at mid-infrared and ultraviolet, we also indicate the positional uncertainty ( $\sigma_{\text{pos}}$ ) in parenthesis, and the cardinal direction if the separation is larger than  $3 \sigma_{\text{pos}}$  and 0.75 arcsec, at the mid-infrared, and larger than  $1 \sigma_{\text{pos}}$  at the ultraviolet. Observed fluxes are fitted by power laws (coloured segments), black bodies (curves), and theoretical He- and H atmosphere white-dwarf grid points (brown- and orange small stars and dashed lines). Effective temperatures indicated in the optical range are for the single blackbody fits (thin solid curves) ‘passing through’ the optical fluxes. Example two-blackbody- and blackbody+power-law fits are represented by grey- and cyan thick lines, respectively (dashed lines for individual components and solid lines for their sums); in these cases, only the effective temperature of the hot blackbody component is indicated, in the ultraviolet range. Thermal radiuses derived from the ultraviolet blackbody fits are indicated in kilometres and account for distance uncertainties (listed in Table 9).

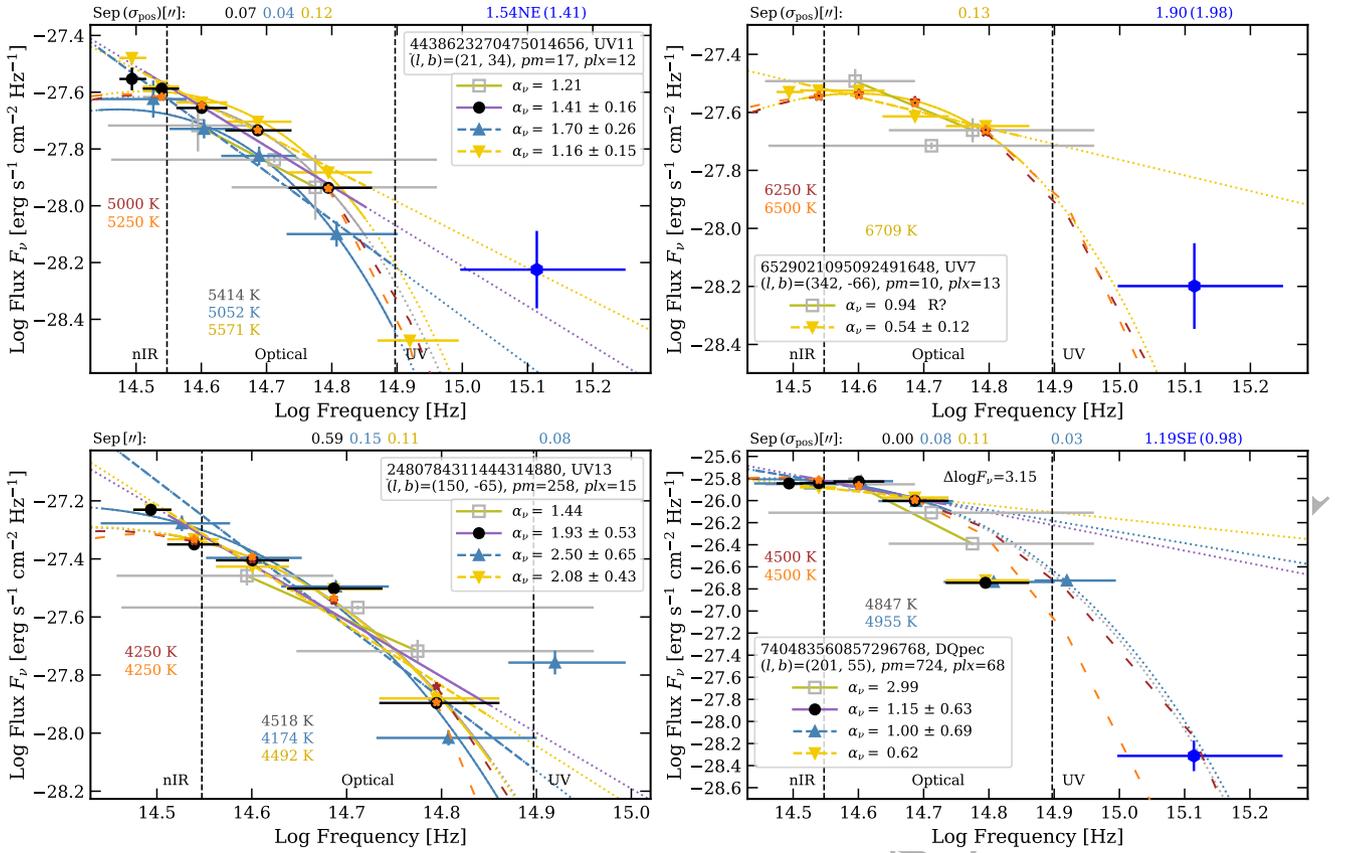
3.04 east of it and 3.3 arcsec west of another optical source, NSC DR2 160974\_6762, which is 0.25 mag fainter at g-band.

Finally, we identified six SDSS sources with *u*-band flux excesses, using the selection criterium  $u - g < g - r$ , for *u*-band point-spread-function (PSF) magnitude errors smaller than 0.45 mag. UV8 is already commented above. *Gaia* DR3 2480784311444314880 (UV13), *Gaia* DR3 1900830823016998144 (UV14), and *Gaia* DR3 2807663865638075264 (UV15) have cool *griz*-band components of  $\sim 4000\text{--}5000$  K, large proper motions of about 260, 200, and 190  $\text{mas yr}^{-1}$ , and *d50* distances of 66, 82 and 90 pc, are well isolated in sparse fields, and are white dwarf photometric candidates in GCNS (UV13 and UV14 also in Gentile Fusillo et al. 2021). The SED of UV13 is shown in Fig. 11 and those of UV14 and UV15 are shown in Fig. G3 of the online supplementary material. UV15 appears to have (i) a slight flux dip at *i* band compared to an overall curved *griz*-band profile, and (ii) a high mid-infrared, *W1*-band flux excess. UV13 and UV15 have significant *u*-band flux excesses, and UV14 has a low flux excess that agrees within 1–2 sigma with the blueward extrapolations of the PS1, SDSS, and NSC blackbody

fits. The two remaining sources, *Gaia* DR3 430017946216189145 and *Gaia* DR3 4518304014850969088, have large *u*-band errors of 0.41–0.44 mag and their counts in the *u*-band image appear as noise compared to similar features around these sources.

### 3.5 Radio crossmatches

We crossmatched the list of *Gaia* sources with the Master Radio Catalogue (as revisited on 2022 December 12th), provided by the High Energy Astrophysics Science Archive Research Centre (HEASARC; <https://heasarc.gsfc.nasa.gov>) and that contains radio sources from many catalogues, using a crossmatch radius of  $(pm/1000 \times 50) + 15$  arcsec. There are 27 multiple radio matches for 12 *Gaia* sources, all within 90 arcsec. Ten *Gaia* sources have a match in images of the 1.4 GHz NRAO VLA Sky Survey (NVSS; epochs 1993–1997; Condon et al. 1998). We compiled the positional uncertainties- and mean observation epochs of the radio sources in the different catalogues. We then propagated the *Gaia* coordinates to these epochs and we recomputed the angular separations. Four *Gaia*



**Figure 11.** *Upper left panel:* SED example of UV11 with significant *NUV*-band flux excess (UV8 and UV9 are shown in Fig. 18). *Upper right panel:* SED example of UV7 with low *NUV*-band flux excess (UV2, UV5, UV6, and UV12 are shown in Fig. G3 of the online supplementary material). *Lower left panel:* SED example of UV13 with significant SDSS *u*-band flux excess (UV15 is shown in Fig. G3 of the online supplementary material). *Lower right panel:* For comparison, SED of the LHS 2229 DQpec white dwarf (commented in Appendix D), with a very low *NUV*-band flux. Same as in Fig. 10.

**Table 3.** Radio crossmatches.

Flag	$Plx$ (mas)	$\mu_{\alpha^*}$ (mas yr $^{-1}$ )	$\mu_{\delta}$ (mag)	$G$ (mag)	$BP - G$ (mag)	$G - RP$ (mag)	$g - r$ (mag)	$r - i$ (mag)	$i - z$ (mag)	P	Sep ( $\mu$ )	n ( $\sigma_{pos}$ )	L (%)	Name	$F_{radio}$ (mJy)	Band (MHz)
Rad1	11.3 $\pm$ 1.1	-91.2	65.5	20.78	-0.07 $\pm$ 0.12	0.52 $\pm$ 0.22	0.37	0.47	0.05	1	5.6	1	100.0	(1)	2.3 $\pm$ 0.5	1400
Rad_a	10.9 $\pm$ 1.7	38.8	18.1	20.87	0.13 $\pm$ 0.29	0.41 $\pm$ 0.22	0.48	0.28	0.05	1	13.2	3	25.0	(2)	4.8 $\pm$ 0.4	1400
Rad_b	17.1 $\pm$ 2.3	-2.8	-15.7	20.56	-0.01 $\pm$ 0.10	0.58 $\pm$ 0.11	-0.01	0.10	-0.02	2	1.6	1	0.6	(3)	36.0 $\pm$ 7.2	4850
Rad_c	17.9 $\pm$ 2.3	-14.1	7.2	20.10	-0.01 $\pm$ 0.13	0.89 $\pm$ 0.05	0.64	0.38	-0.02	1	11.6	2	5.0	(4)	3.5 $\pm$ 0.5	1400
Rad_d	11.9 $\pm$ 3.1	-0.1	8.8	20.64	-0.10 $\pm$ 0.34	0.77 $\pm$ 0.12	1.15	0.65	0.40	1	11.8	20	16.7	(5)	31.0 $\pm$ 1.0	1400
Rad_e	19.8 $\pm$ 2.1	-0.3	-3.9	20.93	0.60 $\pm$ 0.20	0.88 $\pm$ 0.12	1.11	0.38	0.55	1	10.3	12	20.0	(6)	23.7 $\pm$ 1.2	1400
-	-	-	-	-	-	-	-	-	-	-	11.1	6	20.0	(7)	173.1 $\pm$ 19.2	150
Rad_f	12.9 $\pm$ 2.0	-3.0	-1.7	20.87	0.38 $\pm$ 0.08	0.54 $\pm$ 0.08	0.88	0.52	0.24	1	7.6	1	6.7	(8)	95 $\pm$ 9	4850
-	-	-	-	-	-	-	-	-	-	-	12.7	14	1.8	(9)	227.9 $\pm$ 6.71	1420
-	-	-	-	-	-	-	-	-	-	-	6.3	11	14.3	(10)	279.1 $\pm$ 9.1	1400
-	-	-	-	-	-	-	-	-	-	-	4.2	1	2.6	(11)	560	408
-	-	-	-	-	-	-	-	-	-	-	6.3	27	14.3	(12)	739 $\pm$ 40	365
-	-	-	-	-	-	-	-	-	-	-	6.0	3	14.3	(13)	1710.0 $\pm$ 171.8	150
-	-	-	-	-	-	-	-	-	-	-	9.1	3	6.7	(14)	2085.49 $\pm$ 75.367	74
Rad_g	10.9 $\pm$ 2.8	-1.0	-2.8	20.88	0.18 $\pm$ 0.21	0.28 $\pm$ 0.26	0.88	0.33	0.16	1	12.1	4	3.0	(15)	8.1 $\pm$ 1.2	1400

Notes. Proper motion component errors are of 1.1–2.8 mas yr $^{-1}$ . The *griz*-band photometric (P) colours are from PS1 (1) and NSC (2). Radio source name (catalogue, if distinct from the source name acronym): (1) NVSS J053905+820343, (2) NVSS J201013+540843, (3) PMN J0050–7235, (4) NVSS J165455–293302, (5) NVSS J174923–034832, (6) NVSS J075143–221953, (7) TGSSADR J075143.6–221952 (GMRTAS 150M), (8) GB6 J1927+2526, (9) CGPS J192720+252626 (CGPSNGPCAT), (10) NVSS J192721+252624, (11) B2.2 1925+25A (B2), (12) TXS 1925+253 (TEXAS), (13) TGSSADR J192721.0+252623 (GMRTAS 150M), (14) VLSSr J192721.2+252627, and (15) NVSS J174425–144134. Catalogue references are given in the Master Radio Catalogue.

**Table 4.** Comparison of Rad1 and the AR Scorpii pulsar white dwarf (psrWD).

Source	$G$ (mag)	$F_{\text{radio}}$ (mJy)	$F_G$ (mJy)	$F_{\text{radio}}/F_G$
Rad1	$20.784 \pm 0.012$	$2.3 \pm 0.5$	$0.01568 \pm 0.00017$	$147 \pm 33$
psrWD	$>14.990 \pm 0.031$	$5.0 \pm 0.5$	$<3.259 \pm 0.093$	$>1.53 \pm 0.23$

sources were discarded because their sky separations of 28–77 arcsec are too far off to the radio sources, of coordinate uncertainties of a few arcseconds. In Table 3, we list the matches of the remaining eight *Gaia* sources, together with the separation at the radio epoch, the multiple  $n$  of the radio positional-uncertainty ellipse ( $\sigma_{\text{pos}}$ ) required to include the match, and the counterpart likelihood in percent, as the inverse of the number of *Gaia* sources located at the radio epoch in the enlarged ellipse.

*Gaia* DR3 557277267992311808 (Rad1;  $d50 = 91.5$  pc), a  $pm = 112$  mas yr $^{-1}$  probable white dwarf candidate in GCNS100pc and Gentile Fusillo et al. (2019), appears as a probable, unique optical counterpart to the relatively faint NVSS J053905+820343 radio source, with a coordinate offset of only 5.6 arcsec at the NVSS epoch. Within the positional uncertainty region of  $(\Delta RA, \Delta Dec) = \pm(58.4, 6.7)$  arcsec, there are no other optical–infrared source. The 1.4 GHz radio flux density is of  $2.3 \pm 0.5$  mJy $^4$  (Table 3). NVSS J053905+820343 was observed at 1.4 GHz five times in about 1995 (Ofek & Frail 2011). As shown in Table 4, the radio flux density is  $147 \pm 33$  times greater than the  $G$ -band broad-optical flux density, which is represented in Fig. 12 ( $10^{-27.80}$  erg s $^{-1}$  cm $^{-2}$  Hz $^{-1}$ ).

Significant radio emission in white dwarfs is not frequent and it could be produced by magnetic interaction with a close companion, such as for the AR Scorpii pulsar white dwarf (116 pc) that has a close M-type dwarf companion of orbital period of 3.6 h (Marsh et al. 2016; Stanway et al. 2018). AR Scorpii has an NVSS 1.4 GHz flux density of  $8.4 \pm 0.5$  mJy, but it includes flux of a neighbour object at 14 arcsec and of  $3.49 \pm 0.08$  mJy at 1.5 GHz (Stanway et al. 2018); we assumed that AR Scorpii has a deblended 1.4 GHz flux density of  $5.0 \pm 0.5$  mJy. Also, the  $G$ -band flux of AR Scorpii (*Gaia* DR3 6050296829033196032) includes a significant contribution of the M-type companion, which is brighter at the red-optical (Marsh et al. 2016). Thus the radio-to-optical flux ratio of the pulsar white dwarf is probably greater than 1.53 (Table 4). The `ipd_gof_harmonic_amplitude`, `ipd_frac_multi_peak`, `ipd_frac_odd_win`, and `ruwe` (see Section 4.2.2) values of Rad1 are of 0.065, 0 per cent, 0 per cent, and 0.977. These are very close to the median values of *Gaia* DR3 sources with six-parameter solutions at  $G = 21$  mag (Table 7), suggesting no obvious signature of a companion. In the case of AR Scorpii, these parameters are also unrevelatory, except possibly for `ruwe` that has a value of 1.393, greater than the median value of 1.104 at  $G = 15$  mag.

Alternatively, if the 1.4 GHz radio flux of NVSS J053905+820343 were to be emitted by a neutron-star pulsar, then it is comparable to the fluxes of a few mJy of low-luminosity radio millisecond pulsars located at a few hundred pc (see e.g. Bailes et al. 1997). Assuming that at  $G$  band, the pulsar flux is lesser than the white dwarf flux, then the  $F_{\text{radio}}/F_G$  ratio would be greater than  $147 \pm 33$  and compatible

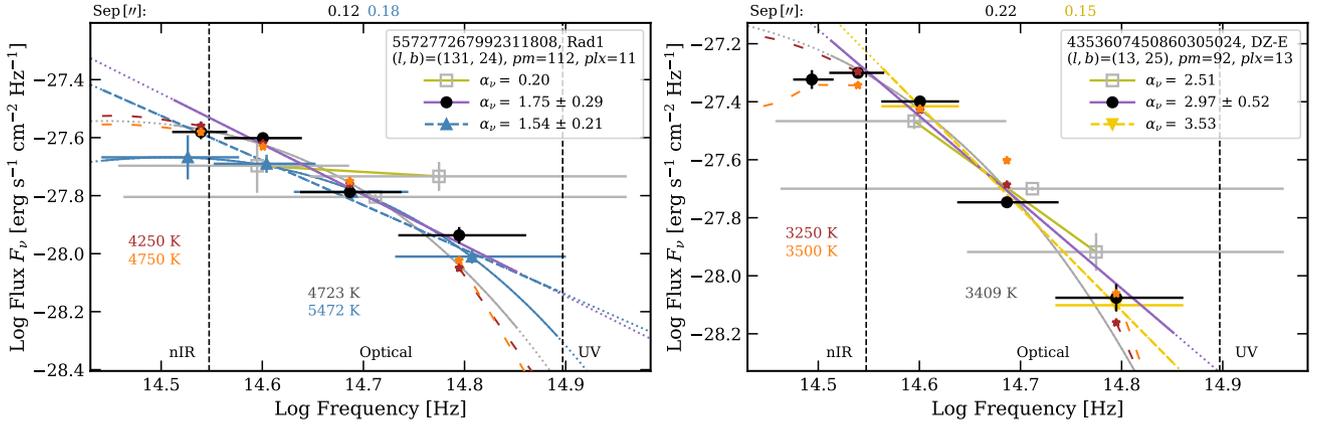
<sup>4</sup> The Jansky unit corresponds to the amount of energy that reaches the Earth per unit collecting area and frequency, i.e. the brightness per unit frequency or flux density, measured in  $10^{-26}$  W m $^{-2}$  Hz $^{-1}$  or  $10^{-23}$  erg s $^{-1}$  cm $^{-2}$  Hz $^{-1}$ .

with a power law of spectral index  $\alpha_\nu \geq 1$  (assuming a non-broken power law from radio to optical).

The PS1 fluxes at epoch 2013.40 of Rad1 are not reproduced by the theoretical pure He- or H atmosphere white-dwarf fluxes nor a blackbody (Fig. 12). In fact, the PS1 SED has a feature in common with the SED of *Gaia* DR3 4353607450860305024 (‘DZ-E’, right panel in Fig. 12), a DZ white dwarf of  $T_{\text{eff}} = 3830 \pm 230$  K with an atmosphere enriched in lithium, sodium, potassium, and calcium ascribed to planetesimal accretion (Kaiser et al. 2021). The feature in common is the significantly depressed  $r$ -band flux, reflected in slightly unequal colours  $g - r < r - i$ . The PS1  $r$  band is defined at 5500–6890 Å, with an effective wavelength of 6170 Å. In the spectrum of *Gaia* DR3 4353607450860305024, the feature is caused by the intense Na I D (5893 Å) absorption line (fig. 1 in Kaiser et al. 2021). Rad1 is completely isolated within 19 arcsec and its PS1 DR1 and DR2 photometric flags indicate good-quality measurements, suggesting that these are reliable. The SDSS fluxes at epoch 2006.23 have larger uncertainties at  $riz$  bands, and the SDSS bandpasses are broader and overlapping, possibly causing the absorption line to not being resolved in the SDSS flux profile. Rad1 could thus be a white dwarf with significant sodium absorption.

Atmospheric enrichment in sodium could stem either from surfacing (e.g. through convective dredge-up, such as the dredge-up of carbon from the interior proposed for some white dwarfs that are enriched in carbon, Blouin & Dufour 2019; Bédard et al. 2022) or from accretion or collection of external matter. In the broader context of the origin of the elements (Johnson 2019), sodium is expected to originate in exploding massive stars, that is supernova of type II, which are progenitors of neutron stars. Indications of on-going accretion of planetesimals through photometric transit observations have been found in WD 1145+017, a white dwarf with a metal-enriched atmosphere and a debris disc (Vanderburg et al. 2015; see also introduction in Hollands et al. 2022). In the case of Rad1, radio observations and optical spectroscopy are required to confirm whether there is radio emission (furthermore of synchrotron-, pulsating type) and chemical enrichment of the atmosphere, respectively.

The seven remaining *Gaia* sources are towards the Galactic plane ( $|b| < 12^\circ$ ), except one of them, and have low counterpart-likelihoods. We note that the  $\sigma_{\text{pos}}$  of some radio sources could be lower values, as for VLSSr J192721.2+252627 at 74 MHz, where it does not include ionospheric corrections, possibly of the order of tens of arcseconds (Lane et al. 2014). *Gaia* DR3 2185585922087166720 (Rad\_a) is in a sparse field and 13 arcsec west of NVSS J201013+540843, which has three closer optical–infrared sources but none is in its positional error ellipse of  $(\Delta RA, \Delta Dec) = (5.1, 3.1)$  arcsec. Two *Gaia* sources have radio cross-identifications in the SPECIND V3.0 catalogue (Stein et al. 2021). *Gaia* DR3 4688982132605446784 (Rad\_b;  $b = -45^\circ$ ) is at 1.6 arcsec of PMN J0050–7235 of position accuracy  $(\Delta RA, \Delta Dec) = (36.2, 30.6)$  arcsec using the relations in Wright et al. (1994). In SPECIND, there are three other radio identifications associated with PMN J0050–7235 and these are centred 1.2 arcmin to the west (survey beam sizes of 18–98 arcsec), the four radio flux measurements being consistent with a single power law. The optical–near-infrared SED of the *Gaia* source indicates blackbody emission and, as for Rad1, an  $r$ -band flux dip (Fig G4, available as online supplementary material). The *Gaia* parameters (e.g. `ruwe`) indicate that it could be a resolved binary. *Gaia* DR3 2024652913390061952 (Rad\_f) is close to multiple radio components, for example B2.2 1925+25A (Colla et al. 1972) at 4.2 arcsec, or NVSS J192721+252624, TGSSADR J192721.0+252623, and TXS 1925+253 at 6 arcsec, the three being consistent with the same coor-



**Figure 12.** The PS1 SED of Rad1 (*left panel*) is similar to that of Gaia DR3 4353607450860305024 (*right panel*), a DZ white dwarf with an atmosphere enriched in lithium, sodium, potassium, and calcium ascribed to planetesimal accretion, and whose reduced flux at  $r$  band is caused by intense sodium line absorption. Same as in Fig. 10.

ordinates within 2 arcsec and, in SPECFIND, with a radio power-law emission of  $\alpha_\nu = 0.7$ . NVSS J174923–034832 (Rad\_d) and NVSS J075143–221953 (Rad\_e) appear to have PSO J267.3500–03.8089 and PSO J117.9316–22.3316 as optical counterparts within  $1 \sigma_{\text{pos}}$ .

Finally, we crossmatched the list of *Gaia* sources within 30 arcsec with the full catalogue of transients of the Transient Name Server (TNS<sup>5</sup>; as of 2022 September 22th), which contains the complete catalogue of fast radio bursts (FRBs), and we find no match.

### 3.6 Crossmatches with sources reported in the literature

We queried the Simbad database (as revisited on 2023 February 1st) on the *Gaia* coordinates, propagated to epoch 2000 ( $d_{\text{yr}} = -16.0$  yr), and within  $\delta = 10$  arcsec. The visual check with the Aladin tool and the verification in the literature and catalogues yielded 97 matches. These have  $M_G^\pi = 16.0 - 17.4$  mag and  $d_{50} = 32 - 98$  pc. From a crossmatch with the Montreal White Dwarf Database<sup>6</sup> (as of 2022 December 20th; Dufour et al. 2017), we recovered additional spectral types estimated from spectra.

There are 86 probable white dwarf photometric candidates (Gentile Fusillo et al. 2019, 2021; Torres et al. 2019; GCNS). Among these, 19 are spectroscopically confirmed white dwarfs, and have  $M_G^\pi = 16.0 - 17.1$  mag. Fifteen have DC-type (continuous, feature-less) spectra, three have DZ-type (metal-polluted) spectra, and one ([IIB2000] F351-50) has a feature-less DA-type spectrum. Also among these (and simultaneously in our subsample of 2464 sources), 25 are in the selection of Scholz (2022) of faint,  $pm > 30$  mas yr<sup>-1</sup> white dwarf candidates, of which some could be ultra-massive ( $\gtrsim 1.05 M_\odot$ ; Althaus et al. 2022). Finally, one source has an uncertain spectroscopic classification, sdA: subdwarf (SDSS J120918.83+470940.3, Kepler et al. 2016); its SED based on PS1, SDSS, and NSC fluxes indicates a blackbody profile of  $\sim 7500$  K.

In the colour–magnitude– and colour–colour diagrams forwards, such as Figs. 19 and F1, we plot the white dwarfs that are confirmed spectroscopically, with labels related to their spectral type. In Section 3.5, we comment on Gaia DR3 4353607450860305024 (‘DZ-E’), a cool DZ white dwarf which has an atmosphere enriched in

lithium, sodium, potassium, and calcium (Kaiser et al. 2021), because the SED of Rad1 bears resemblance to its SED. In Appendix B, we comment on Gaia DR3 3905335598144227200 (‘DC1’), an example of nearby DC white dwarf, and Gaia DR3 283928743068277376, a hot white-dwarf source with an apparent flux excess at  $i$  band.

### 3.7 Power-law profiles at the broad-optical and infrared

We identify power-law profiles using the PS1-, SDSS-, or NSC photometry of the *Gaia* sources, and then we extend the search using infrared photometry.

For that purpose, we fitted the observed fluxes in the  $\log(F_\nu) - \log(\nu)$  plane with power law- and black body functions, by non-linear least-squares using the SCIPY.OPTIMIZE.CURVE\_FIT function. Magnitude uncertainties were previously converted to logarithmic-flux uncertainties and used as relative weights. The best fit minimises the chi-square expression

$$\chi^2 = \sum_{n=1}^N \left( \frac{\log(F_{\nu,i}) - Y_i}{\sigma_i} \right)^2, \quad (9)$$

where  $N$  is the total number of bandpasses,  $Y$  is the fitting function, and  $\sigma_i$  are the uncertainties. The output variance of a parameter, for instance of the  $\alpha_\nu$  spectral index, is the variance of the parameter as obtained from  $\chi^2$  and then multiplied by  $f_\sigma^2$ , an uncertainty scaling factor equal to the reduced chi-square of the optimal fit,  $\chi^2[\text{optimal parameters}]/(N - p)$ , where  $p$  is the number of parameters. The square root of the output variance (the standard deviation) informs us thus on the dispersion- or deviation of the observed SED profile relative to the model profile. To avoid weight sensitivity at very small  $\sigma_i$  uncertainties, these were artificially enlarged to 0.008 dex, equivalent to 0.02 mag or 2 per cent in flux.

In the SED figures, the power law fits are represented by the coloured segments (spectral indices are given in the legend) and the blackbody fits are represented by the curves (effective temperatures are indicated in the plot, in the same colours as the curves).

For the blackbody fitting of the observed fluxes in  $\text{erg s}^{-1} \text{cm}^{-2} \text{Hz}^{-1}$ , we used the Planck flux density function  $\pi B_\nu(\nu, T)$  in the form

$$\pi B_\nu(\nu, T) f_{\text{sc}} = \pi \frac{2h\nu^3}{c^2} \frac{1}{e^{h\nu/(k_B T)} - 1} f_{\text{sc}} \quad (10)$$

<sup>5</sup> <https://www.wis-tns.org>, developed by O. Yaron, A. Sass, N. Knezevic, L. Manulis, E. Ofek and A. Gal-Yam.

<sup>6</sup> <https://montrealwhitedwarfdatabase.org/>

where  $h$  [J/Hz],  $k_B$  [J/K], and  $c$  [m/s] are the constants of Planck, Boltzmann, and light velocity, respectively. We fitted for the parameters of temperature  $T$  and scaling factor  $f_{sc}$ . Then, using the Stefan-Boltzmann  $\sigma T^4$  frequency-integrated blackbody flux [J/s/m<sup>2</sup>] as normalisation factor, we retrieved the bolometric flux in erg s<sup>-1</sup> cm<sup>-2</sup>:

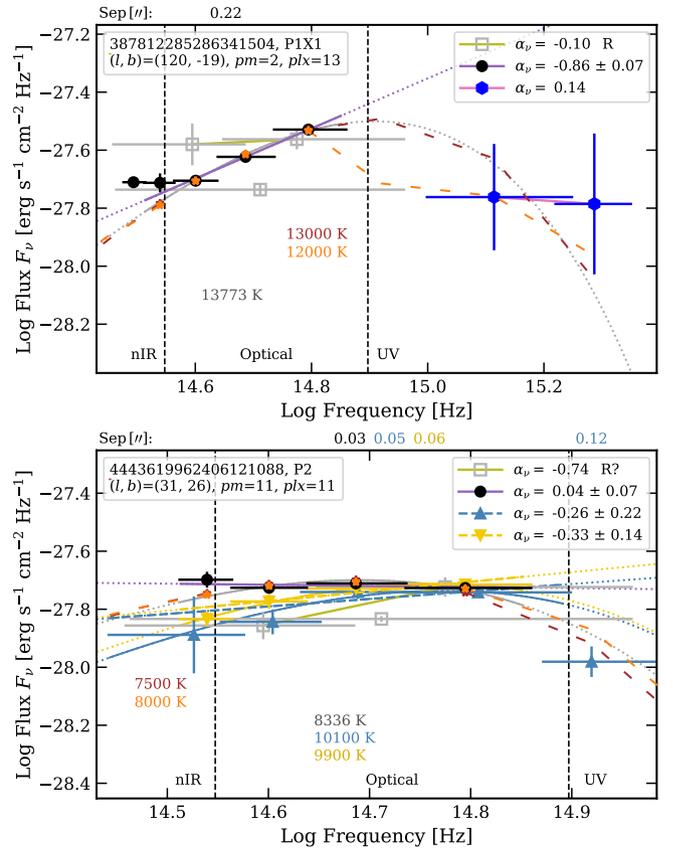
$$F_{bol} = f_{sc} \sigma T^4. \quad (11)$$

We verified that the resulting blackbody density function with this approach is identical to that using the `BLACKBODY` model from the `ASTROPY` package, with relative  $F_\nu$  differences lesser than 0.02 per cent.

For illustrative purpose and to guide in the interpretation, we also show in the SED figures the closest matches of the theoretical grid fluxes of white dwarfs of pure He- and pure H atmospheres (brown- and orange small stars, extended by brown- and orange dashed lines, respectively) and masses of 0.4, 0.6, 0.8, 1.0, and 1.2 M<sub>⊙</sub> (same reference as above). The closest match is that having the flux-error-weighted mean distance that is smallest between the observed- and theoretical fluxes at *griz* bands. The default observed fluxes that are matched are those of PS1 (black dots), SDSS (blue upward triangles), or NSC (yellow downward triangles), depending on which has most *griz* coverage. At effective temperatures cooler than ~5000 K and compared to the He atmosphere fluxes, the H atmosphere fluxes tend in most cases to depart to less red red-optical- and infrared colours, and thus to differ more from blackbody- and power law fluxes (see e.g. the colour-colour diagrams and the SEDs in the online supplementary material).

For the 1104 *Gaia* sources that have PS1 PSF magnitudes in the four *griz* bands, we fitted their *griz*-band fluxes as described above, with a power law function of unconstrained  $\alpha_\nu$  spectral index. We used the bandpass effective wavelengths listed in [Schlafly et al. \(2012\)](#) and an AB magnitude zero-point flux of 3631 Jy. We then selected the sources with  $\alpha_\nu$  errors smaller than 0.1. Because the PS1 *grizy* bandpasses do not overlap in wavelengths, these enable us to obtain a neat description of the broad-optical profiles and, to some extent, to distinguish power-law profiles from blackbody profiles. However, the profile identification becomes more efficient when considering also SDSS- or NSC *u*-band fluxes and infrared fluxes, as shown below. Besides this, the  $G_{BP}$  and  $G_{RP}$  fluxes of the faint sources can also support estimating the slopes and temperatures at the broad-optical, provided these fluxes are accurate enough.

Among the PS1 *griz*-band power-law profile sources, 44 have  $\alpha_\nu < 3$  and five have  $\alpha_\nu > 3$ . We were particularly interested in the former. One has  $\alpha_\nu < 0$ , five have  $\alpha_\nu = 0.0 - 0.8$ , and 38 have  $\alpha_\nu = 0.9 - 3$ . Their minimum- and maximum *griz*-band formal magnitude errors are of (0.003, 0.003, 0.005, 0.006) and (0.139, 0.122, 0.112, 0.446) mag, respectively. We checked all the candidates in archival images and catalogues. From visual inspections of the SEDs including ultraviolet- and infrared fluxes, few have overall straight profiles and most have curved profiles. For illustrative- and verification purposes, and to limit redundancy, we consider here explicitly only 35 of the 44 sources with  $\alpha_\nu < 3$ . These are listed in Table 5, some are shown in Figs. 13 and 15, and all are shown in Fig. G5, available as online supplementary material. The five sources with  $\alpha_\nu > 3$  are Gaia DR3 2022581399133091968, Gaia DR3 4109505149313851264, Gaia DR3 2022751273695068544, Gaia DR3 1827956227460470144, and Gaia DR3 2173177211819325568. These are towards the Galactic centre and plane, at  $l = [-1, 97]^\circ$  and  $b = [-2, 8]^\circ$ , and have small proper motions of  $pm = 3 - 13$  mas yr<sup>-1</sup>, suggesting that these are probably more distant and their optical power-law profiles stem from



**Figure 13.** SEDs of PIX1 and P2, with PS1 *griz*-band power-law profiles. Same as in Fig. 10.

interstellar extinction and reddening. The PS1 source with a negative slope is PIX1 ( $\alpha_\nu = -0.86 \pm 0.07$ ; Fig. 13), at  $d_{50} = 81$  pc. It is also an X-ray crossmatch candidate (Section 3.3), appears very faint in *GALEX* ultraviolet images, and is fainter at ultraviolet than at *g* band. The source has the highest *ruwe* value among the sources of Table 5 (and those of Tables 7 and 8) and is possibly a binary (see Section 4.2.2).

The sources with  $\alpha_\nu \approx 0 - 0.9$  are outwards of the Galactic plane, at latitudes  $|b| = 19 - 65^\circ$ . Gaia DR3 4443619962406121088 (P2, see Fig. 13) has PS1 *griz*-band log  $F_\nu$  fluxes that are relatively close to one another, within 0.03 dex ( $\alpha_\nu = 0.04 \pm 0.07$ ). However the NSC- and SDSS profiles are slightly curved, with an *u*-band flux that is suppressed relative to the power-law- and blackbody fits, suggesting a white-dwarf type. It is unclear whether- and to what extent the difference between the flat- and curved profiles is related to P2 possibly being a binary.

Among the sources of Table 5, Gaia DR3 3257308626125076480 (P15;  $\alpha_\nu = 1.48 \pm 0.09$ ) is a white dwarf photometric candidate in *GCNS*, with  $P_{WD} = 0.81$ , whereas the other sources have  $P_{WD} < 0.35$  and a mean  $\langle P_{WD} \rangle = 0.04 \pm 0.08$ . In [Gentile Fusillo et al. \(2021\)](#), Gaia DR3 4125016578273139456 (P27;  $\alpha_\nu = 2.18 \pm 0.07$ ) and Gaia DR3 1833552363662146944 (P36;  $\alpha_\nu = 2.95 \pm 0.04$ ) are probable white dwarf photometric candidates, with  $P_{WD} = 0.98 - 1.00$ . None of the three sources is reported in *Simbad*. Six sources of Tables 5 and 7 are in [Gentile Fusillo et al. \(2021\)](#), and P27 is the only source with a *G*-band *excess\_flux\_error*  $> 4$  ( $=7.404$ ), indicating that it could be variable.

Some sources have photometry affected by blends with second components and that might contribute to the *griz* power-law profile.

**Table 5.** Sources with power-law profiles at *griz* bands or approximately straight profiles at the optical and infrared.

Flag	$Plx$ (mas)	$\mu_{\alpha^*}$ (mas yr <sup>-1</sup> )	$\mu_{\delta}$ (mag)	$G$ (mag)	$BP - G$ (mag)	$G - RP$ (mag)	$g - r$ (mag)	$r - i$ (mag)	$i - z$ (mag)	P	PL $\alpha_{\nu}$ at <i>griz</i>	Profile UV-Opt-IR	Comment
P0	14.2±4.3	6.1	-6.2	20.89	-0.16±0.23	0.02±0.20	-0.26	-0.20	-0.05	3	-0.89±0.02	S [ <i>U, z</i> ] or C	–
P1X1	13.3±2.0	-0.2	-1.5	20.61	-0.33±0.08	0.64±0.17	-0.24	-0.21	-0.02	1	-0.86±0.07	C?	–
P2	11.3±2.1	10.8	-3.7	20.86	-0.17±0.08	0.20±0.11	0.04	-0.04	0.07	1	0.04±0.07	S [ <i>g, y</i> ] or C	–
P3	11.1±4.0	-4.8	-3.3	20.81	0.09±0.16	0.33±0.17	0.29	-0.04	0.03	1	0.38±0.14	~S [ <i>g, W 2</i> ]	Recovered from infrared
P4	11.6±3.6	-2.6	1.4	20.90	0.27±0.19	0.74±0.17	0.05	0.08	0.32	2	0.52±0.22	~S [ <i>g, W 2</i> ]	Recovered from infrared
P5	12.5±3.2	-1.0	-2.3	20.84	-0.14±0.17	0.07±0.36	0.18	0.18	0.05	1	0.71±0.05	C	–
P6	13.9±3.4	0.2	0.4	20.69	-0.29±0.31	0.21±0.36	0.19	0.23	0.09	1	0.81±0.05	~S [ <i>u, W 2</i> ] or C	Recovered from infrared
P7	14.0±1.5	-2.9	-16.0	20.50	0.16±0.10	0.87±0.07	0.30	0.20	0.07	1	0.97±0.08	C	–
P8	11.8±2.4	4.6	-0.5	20.92	0.57±0.32	0.46±0.20	0.32	0.21	0.17	1	1.09±0.02	C	–
P9	21.1±1.2	2.3	-7.3	19.78	0.12±0.07	0.81±0.05	0.36	0.21	0.10	1	1.09±0.07	C	–
P10	10.8±2.9	-7.0	-10.5	20.85	0.10±0.14	0.47±0.11	0.35	0.23	0.21	1	1.22±0.03	C	–
P11	11.2±2.4	-3.9	-10.1	20.87	-0.05±0.17	0.51±0.25	0.36	0.27	0.18	1	1.24±0.03	S [ <i>g, y</i> ]	–
P12	15.5±2.3	-3.9	-7.3	20.67	0.49±0.23	0.72±0.15	0.33	0.27	0.21	1	1.25±0.02	C	–
P13	10.8±3.9	-4.2	4.1	20.95	0.20±0.17	0.82±0.17	0.38	0.28	0.25	1	1.39±0.03	C	–
P14	12.6±1.9	-8.3	-1.8	20.65	0.61±0.12	0.58±0.07	0.40	0.33	0.09	1	1.40±0.09	C	–
P15	12.2±3.0	33.0	-64.1	20.89	0.22±0.17	0.84±0.17	0.47	0.26	0.19	1	1.48±0.09	C	–
P16	16.0±2.2	3.0	4.5	20.69	0.13±0.14	0.84±0.09	0.45	0.28	0.23	1	1.49±0.05	C	–
P17	22.3±1.6	-3.9	1.3	20.20	0.16±0.06	0.89±0.04	0.52	0.28	0.20	1	1.56±0.09	C	–
P18	13.5±1.7	-88.6	-15.7	20.78	0.24±0.19	0.91±0.15	0.42	0.36	0.22	1	1.59±0.03	C	Comoving with M dwarf
P19	17.4±3.0	3.5	7.2	20.77	-0.22±0.19	0.82±0.13	0.48	0.29	0.32	1	1.67±0.08	C	Blend photometry
P20	21.9±2.2	-16.5	0.7	20.36	0.15±0.15	0.81±0.09	0.49	0.37	0.28	1	1.77±0.02	C?	Blend photometry
P21	19.5±2.4	-3.6	-4.4	20.45	0.01±0.11	0.76±0.15	0.53	0.37	0.16	1	1.83±0.06	C	–
P22	12.6±1.6	-0.7	0.4	20.65	0.43±0.14	0.89±0.06	0.63	0.41	0.27	1	2.13±0.05	C	–
P23	12.2±2.6	-15.2	-9.2	20.85	0.08±0.15	0.82±0.11	0.62	0.44	0.29	1	2.13±0.05	C	–
P24	15.5±3.9	-10.1	-1.8	20.94	0.66±0.39	0.68±0.11	0.55	0.57	0.24	1	2.17±0.06	C	–
P25	19.6±2.0	8.3	-0.5	20.76	0.64±0.24	0.90±0.03	0.62	0.49	0.25	1	2.17±0.07	C	–
P26	12.2±2.3	-7.7	-0.3	20.69	0.40±0.09	0.65±0.13	0.65	0.42	0.37	1	2.17±0.07	C	–
P27	13.4±1.3	-1.5	1.1	20.39	0.69±0.07	0.68±0.05	0.64	0.46	0.29	1	2.18±0.07	C	–
P28	20.7±2.6	-2.7	9.6	20.94	-0.22±0.24	0.84±0.16	0.67	0.46	0.26	1	2.30±0.06	C	–
P29	12.0±3.4	-5.0	0.4	20.87	0.75±0.39	0.15±0.08	0.70	0.49	0.35	1	2.39±0.06	C	–
P30	11.1±2.8	-22.3	-26.9	20.84	0.67±0.23	0.82±0.11	0.69	0.54	0.35	1	2.41±0.05	C	–
P31	11.5±2.6	-0.7	-11.0	20.82	0.62±0.20	0.80±0.11	0.70	0.49	0.38	1	2.42±0.05	C	–
P32	17.1±2.6	8.2	-3.6	20.35	0.53±0.11	0.88±0.04	0.69	0.50	0.38	1	2.43±0.03	C	–
P33	13.1±2.4	-6.9	1.5	20.69	0.31±0.16	0.62±0.07	0.84	0.35	0.36	1	2.44±0.08	C	–
P34	11.1±3.5	-3.3	-3.9	20.83	0.33±0.26	0.87±0.14	0.80	0.60	0.37	1	2.75±0.07	C	–
P35	13.2±2.3	-5.4	-1.0	20.62	0.73±0.09	0.75±0.11	0.89	0.50	0.37	1	2.84±0.07	C	–
P36	12.7±3.2	-1.5	-3.6	20.87	0.64±0.20	0.86±0.14	0.83	0.68	0.40	1	2.95±0.04	C	–
P37	16.1±2.3	-5.5	-4.1	20.48	0.78±0.09	0.75±0.11	0.80	0.64	0.45	1	2.96±0.01	C	–
UV7	13.4±1.4	-10.0	3.1	20.56	-0.03±0.10	0.81±0.10	0.08	0.22	0.00	2	0.54±0.12	~S [ <i>NUV, W 2</i> ]	Recovered from infrared

Notes. Proper motion component errors are of 0.7–3.1 mas yr<sup>-1</sup>. The *griz*-band photometric (P) colours are from PS1 (1), NSC (2), and SDSS (3). SED profiles based on ultraviolet, optical, and infrared photometry are classified as straight (S) or curved (C); for the former, the bandpass range is given.

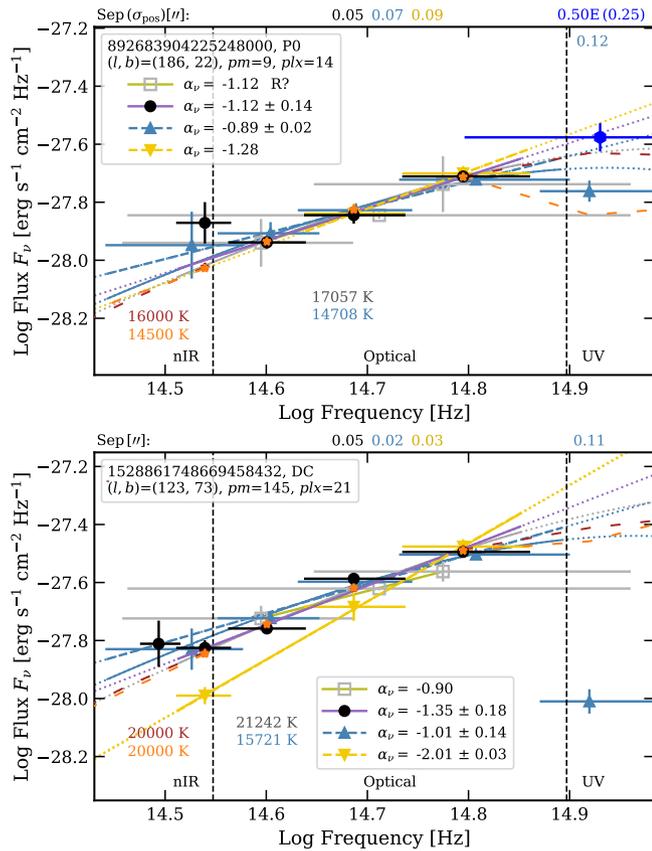
For example, Gaia DR3 4149950169090938240 (P20;  $\alpha_{\nu} = 1.8$ ), at  $d50 = 48$  pc. It has a tight second component 0.37 arcsec north-east, Gaia DR3 4149950169090938112, which is 0.2 mag brighter at  $G$  band, has no parallax nor proper motion (Table 8), and appears as the slightly bluer part in their blend in the PS1 images. Both components are measured as a single source in the PS1 catalogue. The second component might be the cause of the high values of photoastrometric binarity parameters for P20, such as a ruwe of 1.6 (see Tables 7 and 9). We define the parameters and discuss binarity further in Section 4.2.2. Furthermore, the tight visual binary is located towards the crowded Galactic Centre, suggesting that if the distance is underestimated, then the power-law profile might also be caused by reddening. Another case is Gaia DR3 309921197948007936 (P19;  $\alpha_{\nu} = 1.7$ ;  $d50 = 67$  pc). Although, it is a well isolated, in a field at  $(l, b) = (128, 33)^{\circ}$  far from the Galactic plane, large parts of its red (and infrared) fluxes stem from a second component 1.0 arcsec north-

west. Both components are almost resolved in the PS1 colour images and identified as a single source in the PS1 catalogue. In the case of Gaia DR3 3948582104883237632 (P18;  $\alpha_{\nu} = 1.6$ ), the photometry might be affected by its 5.1 mag brighter M-type neighbour, located 5.3 arcsec south (Gaia DR3 3948582104883968384); we found that these two objects form a large proper-motion-, 886 au-wide stellar binary at 168 pc (Appendix C).

Five PS1 sources, P2, Gaia DR3 3910666820788919936 (P5), Gaia DR3 4486941991858372352 (P12), P15, and P19 have SDSS  $u$ -band magnitudes with uncertainties smaller than 0.5 mag, in the range 0.12–0.40 mag. The SEDs (Figs. 13 and G5) indicate that the SDSS  $u$ -band fluxes are not only below the extrapolations of the optical power-law fits, but also 0–3 sigmas below the extrapolations of the blackbody fits. We noted that 20 arcsec south of P5, there is a point-like radio source of  $45.1 \pm 5.9$  mJy at 150 MHz (TGSSADR J112929.6+073719), and  $5.97 \pm 0.154$  mJy (FIRST

**Table 6.** Power-law colours for *GALEX*, *Gaia* DR3, SDSS  $u^*g^*$ , PS1 *grizy*, WFCAM *JK*, and *WISE* filters. BB stands for a blackbody of  $7.37 \times 10^5$  K.

$\alpha_V$	<i>FUV</i> – <i>NUV</i> (mag)	<i>NUV</i> – <i>G</i> (mag)	<i>BP</i> – <i>G</i> (mag)	<i>G</i> – <i>RP</i> (mag)	<i>G</i> – <i>g</i> (mag)	$u^*$ – $g^*$ (mag)	$g^*$ – <i>g</i> (mag)	<i>g</i> – <i>r</i> (mag)	<i>r</i> – <i>i</i> (mag)	<i>i</i> – <i>z</i> (mag)	<i>z</i> – <i>y</i> (mag)	<i>y</i> – <i>J</i> (mag)	<i>J</i> – <i>K</i> (mag)	<i>K</i> – <i>W1</i> (mag)	<i>W1</i> – <i>W2</i> (mag)
BB	-0.81	-1.82	-0.21	-0.42	0.20	-0.58	-0.06	-0.54	-0.43	-0.31	-0.23	0.35	-0.27	-0.10	-0.05
-2.0	-0.84	-1.84	-0.21	-0.42	0.20	-0.59	-0.06	-0.55	-0.43	-0.31	-0.23	0.35	-0.27	-0.11	-0.05
-1.5	-0.63	-1.37	-0.14	-0.24	0.14	-0.44	-0.05	-0.41	-0.32	-0.24	-0.17	0.49	0.04	0.11	0.13
-1.0	-0.42	-0.88	-0.07	-0.07	0.06	-0.30	-0.03	-0.27	-0.22	-0.15	-0.11	0.63	0.34	0.34	0.29
-0.5	-0.22	-0.38	0.01	0.10	-0.03	-0.15	-0.02	-0.13	-0.11	-0.08	-0.05	0.77	0.65	0.57	0.46
0.0	0.00	0.13	0.10	0.24	-0.13	0.00	0.00	0.00	0.00	0.00	0.00	0.92	0.95	0.80	0.64
0.5	0.22	0.65	0.20	0.38	-0.24	0.15	0.02	0.13	0.11	0.08	0.05	1.06	1.26	1.03	0.81
1.0	0.44	1.18	0.30	0.51	-0.37	0.30	0.04	0.27	0.21	0.15	0.12	1.19	1.58	1.25	0.98
1.5	0.65	1.73	0.41	0.63	-0.51	0.45	0.05	0.40	0.32	0.23	0.17	1.34	1.88	1.48	1.16
2.0	0.87	2.29	0.53	0.73	-0.67	0.61	0.06	0.54	0.42	0.31	0.22	1.49	2.18	1.72	1.32
2.5	1.10	2.85	0.65	0.83	-0.83	0.76	0.08	0.67	0.52	0.38	0.29	1.62	2.50	1.95	1.49
3.0	1.33	3.43	0.78	0.91	-1.01	0.92	0.10	0.79	0.64	0.45	0.34	1.77	2.81	2.18	1.66

**Figure 14.** *Top panel:* SED of P0, an SDSS *griz*-band power-law candidate. The *u*- and *Swift*/UVOT *U* bandpasses have their upper frequency-limit at  $10^{15.0}$  Hz. *Bottom panel:* SED of Gaia DR3 1528861748669458432, an example of large proper-motion DC white dwarf with a *griz*-band flux profile that is almost straight (small  $\alpha_V$  errors), peaking at *g* band, and with significantly suppressed *u*-band flux. Same as in Fig. 10.

J112929.7+073718) and  $8.9 \pm 0.5$  mJy (NVSS J112929+073715) at 1.4 GHz, which coincides with the very faint mid-infrared source CWISE J112929.68+073717.9 (*W1W2*  $\sim 17$  mag). Gaia DR3 3622634116211982976 (P6) has an NSC *u*-band flux above the PS1 power-law fit extrapolation (Fig. 15), however its NSC *ugriz*-band fluxes are higher overall and have a wide spread, suggesting vari-

ability or other observational aspects. The source is well isolated in optical- and infrared images, has a very small proper motion and might be nearby or extragalactic.

Similarly as for the PS1 sources, we proceeded with the power-law fitting of the 135 SDSS- and 1195 NSC sources that have PSF- and aperture *griz*-band magnitudes, respectively, with magnitude uncertainties smaller than 0.5 mag. Four SDSS sources have  $\alpha_V$  errors smaller than 0.1. After visual check of their SEDs, we kept two as candidates, P19 and Gaia DR3 892683904225248000 (P0;  $\alpha_V = -0.89 \pm 0.02$ ; Fig. 14). Even though P0 has a *z*-band excess relative to the power-law fit, it has an *u*-band flux almost on par with the *g*-band flux. Based on the finding charts that we generated from survey images at different wavelengths, P0 is very bright and a point-like source in *U*- and *UVW1*-band images from the *Swift* Ultraviolet and Optical Telescope (UVOT; Roming et al. 2005). An *U*-band flux measurement (and  $U_{AB} = 20.34 \pm 0.11$  mag) is provided for this source in the *Swift*/UVOT Serendipitous Source Catalogue (Yershov 2014) and we represent it also in the SED of P0. It indicates an even higher ultraviolet flux and possibly some ultraviolet variability. If the emission of P0 is thermal, then it would be relatively hot ( $\sim 15$  000 K). We noted that about 2 arcsec west of P0, there is a very small, faint, and slightly red nebula that could be the origin of the mid-infrared *W1W2*-band fluxes. There are 41 NSC sources with power-law  $\alpha_V$  errors smaller than 0.1. These include the P5 source. After visual check of their SEDs, we noted and concluded that most of the PS1, SDSS, NSC optical power-law profile sources fall into two categories. Either these have slightly curved profiles with blue slopes of  $\alpha_V < 1$ , and suppressed *u*-band flux, which can be ascribed to white dwarfs. As an indicative example, the SED of the Gaia DR3 1528861748669458432 DC white dwarf, with power-law slope errors of 0.1–0.2, is shown in Fig. 14. Or these have straight profiles with red slopes of  $\alpha_V > 1$ , and the sources are towards the plane and centre of the Galaxy, which suggests these sources are reddened and distant.

We also searched for power-law profiles among the 28 sources with hybrid catalogue coverage of the *griz* bands, that is with (i) at most three of these bands covered in each of the PS1, SDSS, and NSC catalogues, and (ii) all four bands covered when combining these catalogues. We did not find any other interesting- or unambiguous candidate.

There are 66 SDSS- and 107 NSC sources with *u*-band magnitudes of uncertainties smaller than 0.45 mag. We did not find any other, *ugri*-band power-law profiles among these. The sources typically

have curved *griz*-band profiles with *u*-band fluxes that are either suppressed (as for the Gaia DR3 1505825635741455872 DC white dwarf, Fig. B1) or in prolongation of blackbody profiles.

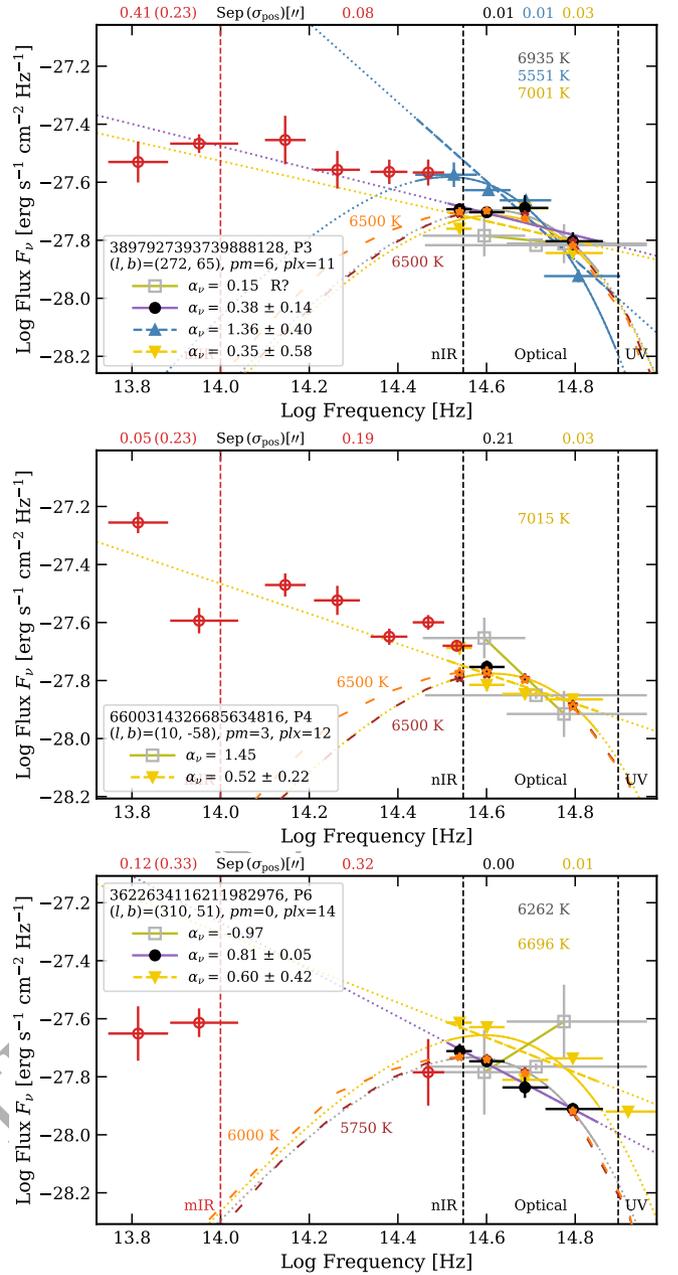
Interestingly, *griz*-band profiles that are straight or almost straight and with significantly-negative slopes are very infrequent among the PS1-, SDSS-, and NSC sources in our subsample; there are only 14 with  $\alpha_V < -0.8$  and  $\sigma_{\alpha_V} < 0.3$ . By requiring that the straightness prolongs to the *u* band, only one remains, P0. Neither the UV candidates with power-law components (Section 3.4) nor P0 have the  $\alpha_V = -2$  spectral index of a Rayleigh-Jeans tail, which would correspond to a very hot thermally emitting source ( $\geq 10^5$  K) such as a young neutron star. At wavelengths  $\lambda$  greater than 1340 Å—the minimum wavelength of the *GALEX FUV* bandpass, the Rayleigh-Jeans approximation is valid if  $T_{\text{eff}}$  is equal- or greater than for example  $7.37 \times 10^5$  K (a comparison of colours is given in Table 6), when  $hc/(\lambda k_B T_{\text{eff}}) = 0.15 \ll 1$ , where  $h$ ,  $k_B$ , and  $c$  are the constants of Planck, Boltzmann, and light velocity, respectively.

Finally, we searched for infrared power-law profiles among the 1936 sources having photometry between the *z*- and *W2* bands. First, independent of slope uncertainties, we looked at sources having infrared- and optical slopes that coincide within 0.6, the optical ones being computed from photometry at at least two of the *griz* bands. We recovered UV7 (which we discuss further in Section 4.2.1) and P6, and we found two additional sources with approximately straight infrared–optical profiles, Gaia DR3 3897927393739888128 (P3) and Gaia DR3 6600314326685634816 (P4), whose SEDs are shown in Fig. 15. P3 and P4 are both classified as point source and as probable quasar in the star-quasar-galaxy classification catalogue of Hughes et al. (2022), which is based on optical–infrared photometry and astrometry. Second, also independent of  $\alpha_V$  uncertainties, we looked at the remaining sources having infrared slopes, with special attention to those having large proper motions or wide bandpass-coverage at the infrared, but we did not find any other candidate, many sources having overall curved profiles or mid-infrared flux excesses that can be ascribed to blends with nearby brighter sources.

For curiosity, we looked also at the sources with extremely blue- or red slopes, independent of the slope uncertainties. Those with the bluest slopes are typically small- to large proper-motion white dwarfs having a curved flux-profile peaking at *gr* bands and a significantly suppressed *u*-band flux, such as the profile of Gaia DR3 1505825635741455872 (Fig. B1). The five sources with the reddest slopes have M-type colours, are in sparse stellar fields, and have no indication of binarity; we describe these in Appendix D, and their SEDs are shown in Fig. G6 (available as online supplementary material).

### 3.8 Blueward- and redward detectability of the power-law profile sources

The blueward- and redward detectability of the power-law components of sources of interest can be assessed using the diagrams of Figs. 6 and 7, which show the maximum distances of average detectability for different catalogues or surveys and power-law slopes, as function of the *g*-band absolute magnitude. We represent P0, P1, P2, P3, P4, and P6 (Table 5) by vertical diamonds and UV3, UV4, UV7, UV8, and UV9 (Table 2) by horizontal diamonds, in the plots of nearest spectral index (spectral index ranges are indicated at the bottom). Their colours are grey, blue, or red depending on whether their power-law component was determined mostly from the optical (*griz* bands), the ultraviolet, or the infrared, respectively. For P6, we adopt the infrared slope of  $0.25 \pm 0.16$  in the [*y*, *W2*] range and we assume as anchor a *g*-band magnitude that is 0.15 mag brighter than



**Figure 15.** SEDs of P3, P4, and P6, which have approximately-straight infrared–optical profiles (UV7 is shown in Fig. 18). Same as in Fig. 10.

that of PS1 (red symbol in  $\alpha_V = 0.5$  diagram). In the case of UV7, we represent it once with its slope and anchor magnitude from the optical (grey symbol in  $\alpha_V = 0.5$  diagram) and once with its slope as obtained when infrared- (and *NUV*-band) fluxes are also accounted for ( $\alpha_V = 1.25$ ; see Section 4.2.1 and Fig. 18), and assuming an anchor magnitude that is 1.0 mag fainter ( $\Delta \log F_V = -0.4$  dex) than that of NSC (red symbol in  $\alpha_V = 1.5$  diagram).

PIX1 (optical  $\alpha_V = -0.86$ ) is represented in the upper right panel of Fig. 6. For its optical spectral index, it is indeed detected in RASS and at the limit in the *NUV* and *FUV* bands, but much fainter, for equivalent spectral indices of  $\alpha_V = 1$  and 0 at X rays and the ultraviolet, respectively (Figs. 4, 5 and 9). P2 (optical  $\alpha_V = 0.04$ ) is represented in the lower right panel of Fig. 6. It would be detectable at the limit at *NUV* band, but there is no *GALEX* coverage; however

**Table 7.** *Gaia* DR3 parameters for the sources. The footnote is at Table 8.

Gaia DR3	RA (deg)	DEC (deg)	<i>Plx</i> (mas)	<i>pmRA</i> (mas yr <sup>-1</sup> )	<i>pmDEC</i> (mas yr <sup>-1</sup> )	gha	fmp (%)	fow (%)	ruwe	ef <sub>BR</sub>	<i>G</i> (mag)	<i>G<sub>BP</sub></i> (mag)	<i>G<sub>RP</sub></i> (mag)	Flag
4043369078205765888	269.490361	-32.362352	19.4±2.2	-0.61±1.06	-5.18±1.08	0.072	6	5	1.515	0.078	19.863±0.010	20.425±0.346	19.032±0.017	γ_a
4040994030072768896	265.851130	-35.777425	12.6±1.6	-3.61±2.50	-2.87±1.28	0.144	0	0	1.095	-0.103	20.697±0.009	21.233±0.444	20.177±0.106	γ_b
599099826943947520	241.492455	-45.738245	10.9±2.6	-1.70±2.01	-10.47±1.63	0.157	0	0	1.049	-0.072	20.822±0.011	21.598±0.177	20.064±0.091	γ_c
4144738037302227072	267.657497	-17.354523	18.2±2.1	-19.26±1.25	-0.67±0.82	0.153	0	0	1.135	-0.005	20.146±0.011	20.869±0.133	19.325±0.072	γ_d
2957941232274652032	81.037758	-24.498135	15.7±2.4	2.77±1.71	0.61±1.39	0.221	3	0	1.435	0.318	20.658±0.025	20.805±0.214	19.828±0.161	γ_e
6456175155513145344	315.733396	-58.644124	16.1±0.6	99.02±0.48	-164.89±0.58	0.023	0	0	0.996	0.120	20.512±0.006	20.695±0.083	19.949±0.085	X2
5922780280824141056	258.890741	-54.828155	12.3±2.0	4.08±2.12	-1.71±1.69	0.161	2	0	1.466	0.296	20.809±0.020	21.055±0.131	19.924±0.099	X_a
602797457838271280	253.774144	-30.672080	21.9±3.1	-12.49±2.31	11.72±1.42	0.343	2	0	2.223	0.167	20.432±0.015	20.855±0.112	19.581±0.071	X_b
6029621818614152576	254.404875	-29.838886	16.8±1.9	-6.22±1.60	3.66±1.29	0.207	12	6	1.568	0.454	20.820±0.013	20.322±0.121	19.369±0.136	X_c
384577010978265344	2.083260	42.597460	12.1±2.0	-4.13±1.14	-3.71±1.16	0.141	0	0	1.422	0.345	20.719±0.012	20.892±0.149	19.831±0.077	X_d
591400991961757952	259.742551	-60.530903	13.7±1.6	-8.12±1.62	-5.78±1.72	0.335	3	0	1.031	0.288	20.674±0.026	20.816±0.168	19.890±0.124	X_e
5386173659617460736*	174.551694	-36.912644	10.6±1.7	-15.83±2.15	-3.88±2.17	0.362	3	0	1.236	0.429	20.885±0.026	20.537±0.128	20.531±0.151	UV1
6829498931265990656*	319.524762	-20.989340	17.3±1.5	-1.43±1.74	-7.08±1.36	0.428	30	0	1.995	0.543	20.166±0.018	19.921±0.080	19.454±0.096	UV2
5777941133043108992*	250.754760	-76.519108	12.2±2.0	-1.47±2.21	2.60±1.72	0.328	0	0	1.208	0.559	20.889±0.028	20.697±0.168	20.090±0.146	UV3
6901051613248041216	307.001186	-11.663427	14.4±1.2	1.61±1.23	-9.00±1.07	0.844	9	0	1.769	0.504	20.235±0.016	20.129±0.058	19.406±0.053	UV4
658545298327662080	325.322938	-39.263001	11.9±3.2	-2.62±2.13	-2.26±2.45	0.070	0	0	0.998	0.238	20.901±0.016	20.845±0.158	20.427±0.262	UV5
6858721824326705536	311.394787	-18.525829	17.3±1.6	-0.66±1.57	-13.42±1.07	0.299	33	3	2.048	0.421	20.119±0.016	20.080±0.048	19.330±0.048	UV6
6529021095092491648	352.073550	-43.968727	13.4±1.4	-10.00±1.77	3.12±1.85	0.302	0	0	1.138	0.430	20.560±0.018	20.530±0.094	19.749±0.094	UV7
315053759457224960	118.499092	11.106838	13.0±2.3	-5.87±2.40	14.71±1.08	0.295	1	0	1.440	0.361	20.863±0.019	21.007±0.257	19.979±0.146	UV8
837736394742229248	168.202576	49.120746	10.5±3.8	2.31±1.62	7.81±2.44	0.036	0	0	1.091	0.267	20.895±0.013	21.150±0.146	20.039±0.127	UV9
4240872805678917376*	300.256515	2.242324	12.6±2.8	-6.31±2.73	-9.46±1.77	0.098	0	0	1.028	-0.215	20.894±0.018	21.157±0.166	21.017±0.304	UV10
4438623270475014656	247.297403	5.872890	12.3±3.5	-11.68±2.22	-12.95±1.88	0.010	0	0	1.036	0.016	20.867±0.015	21.214±0.273	20.312±0.218	UV11
4465431356821050494	247.534452	15.293884	13.7±2.9	-4.24±2.17	-14.60±2.29	0.300	3	6	1.418	-0.053	20.706±0.025	21.066±0.135	20.269±0.192	UV12
2480784311444314880*	23.825818	-4.664492	15.3±0.7	210.30±0.73	149.63±0.62	0.065	0	0	1.148	-0.067	20.191±0.006	20.670±0.087	19.664±0.073	UV13
1900830823016998144	336.869018	31.233036	12.7±0.8	194.99±0.49	40.17±0.90	0.029	0	0	0.986	0.105	20.514±0.007	21.000±0.148	19.700±0.078	UV14
2807663865638075264	8.667106	25.961247	11.6±1.3	100.22±1.46	-158.19±1.40	0.046	0	0	1.279	-0.024	20.750±0.010	21.326±0.163	20.060±0.111	UV15
557277267992311808	84.762430	82.061317	11.3±1.1	-91.17±2.80	65.51±1.13	0.065	0	0	0.977	0.279	20.784±0.012	20.710±0.114	20.261±0.223	Rad1
218558922087166720	302.548637	54.145194	10.9±1.7	38.78±1.15	18.08±1.48	0.119	0	0	0.909	0.075	20.874±0.015	21.005±0.286	20.458±0.218	Rad_a
4688982132605446784	12.552640	-72.595269	17.1±2.3	-2.76±2.40	-15.70±2.13	0.185	9	0	2.100	0.270	20.564±0.022	20.547±0.097	19.980±0.112	Rad_b
6029611888623577088*	253.732467	-29.553519	17.9±2.3	-14.08±1.96	7.17±1.29	0.294	14	6	2.313	0.484	20.096±0.017	20.084±0.129	19.205±0.049	Rad_c
4176647926320238720	267.346904	-3.807569	11.9±3.1	-0.10±1.53	8.79±2.15	0.108	0	0	1.005	0.465	20.641±0.014	20.535±0.340	19.864±0.118	Rad_d
5711114877897853696	117.929719	-22.333737	19.8±2.1	-0.28±1.75	-3.88±2.58	0.203	0	0	1.359	0.092	20.927±0.019	21.532±0.203	20.051±0.114	Rad_e
2024652913390061952	291.838453	25.438382	12.9±2.0	-3.05±1.50	-1.69±2.04	0.055	0	0	1.154	-0.007	20.870±0.013	21.243±0.084	20.329±0.076	Rad_f
4149153813464969856	266.106683	-14.689611	10.9±2.8	-0.99±2.14	-2.80±1.50	0.087	0	0	1.086	-0.016	20.879±0.016	21.052±0.209	20.601±0.256	Rad_g
892683904225248000	113.064577	33.159563	14.2±4.3	6.06±2.35	-6.17±1.85	0.118	0	0	1.095	0.122	20.885±0.018	20.721±0.230	20.868±0.195	P0
387812285286341504	9.438664	44.117580	13.3±2.0	-0.24±1.79	-1.49±1.65	0.371	7	0	7.570	0.577	20.613±0.031	20.282±0.076	19.969±0.169	P1X1
4443619962406121088*	258.237430	9.819276	11.3±2.1	10.78±2.37	-3.68±1.13	0.173	0	0	1.309	0.199	20.856±0.014	20.685±0.074	20.659±0.108	P2
3897927393739888128	180.320681	5.415227	11.1±4.0	-4.84±2.49	-3.27±1.32	0.181	0	0	0.991	0.064	20.815±0.016	20.905±0.158	20.479±0.168	P3
6600314326685634816	336.849435	-34.658736	11.6±3.6	-2.57±1.93	1.41±1.51	0.064	0	0	1.038	0.184	20.899±0.019	21.164±0.189	20.152±0.165	P4
3910666820788919936	172.374777	7.627222	12.5±3.2	-0.99±2.22	-2.35±1.31	0.343	0	0	0.926	0.120	20.840±0.018	20.702±0.169	20.772±0.360	P5
3622634116211982976	197.465908	-11.356244	13.9±3.4	0.19±2.17	0.35±1.94	0.071	1	0	1.196	0.301	20.685±0.018	20.400±0.307	20.479±0.355	P6
4234582018625351936*	296.376750	-3.156466	14.0±1.5	-2.85±1.77	-15.95±1.07	0.300	0	0	1.387	0.339	20.501±0.015	20.665±0.097	19.634±0.067	P7
5606206865714606208	107.879946	-29.719308	11.8±2.4	4.56±1.44	-0.51±2.61	0.051	0	0	1.008	-0.146	20.919±0.015	21.486±0.315	20.454±0.202	P8
4085595994026913792*	286.098462	-19.089506	21.1±1.2	2.35±1.10	-7.26±1.00	0.206	0	0	2.692	0.325	19.776±0.014	19.900±0.074	18.964±0.044	P9
6041917107322758016*	241.484552	-28.603047	10.8±2.9	-6.98±2.17	-10.49±2.16	0.097	0	0	1.083	0.128	20.948±0.011	20.948±0.140	20.375±0.108	P10
1959239908639738240	329.732295	40.088230	11.2±2.4	-3.91±1.71	-10.12±1.94	0.113	0	0	1.054	0.256	20.874±0.017	20.821±0.165	20.362±0.251	P11
4486941991858372352	263.143271	7.169085	15.5±2.3	-3.93±2.79	-7.26±1.56	0.137	0	0	1.135	0.040	20.670±0.021	21.163±0.227	19.945±0.152	P12
4494124177899820800	263.879087	12.664908	10.8±3.9	-4.16±1.92	4.10±2.57	0.064	0	0	0.875	0.284	20.957±0.019	21.152±0.174	20.130±0.167	P13
4112307735705947264	255.680142	-25.165337	12.6±1.9	-8.26±2.41	-1.79±1.49	0.112	0	0	1.093	-0.105	20.648±0.016	21.253±0.114	20.070±0.073	P14
3257308626125076480	57.510592	-0.647049	12.2±3.0	32.98±1.85	-64.15±1.08	0.168	0	0	1.022	0.279	20.896±0.011	21.117±0.171	20.052±0.168	P15
5648417357621486208	135.832152	-27.235757	16.0±2.2	-3.03±2.87	4.52±1.68	0.127	2	0	1.486	0.339	20.691±0.016	20.817±0.142	19.852±0.087	P16
5642345785702095616	131.226259	-29.453312	22.3±1.6	-3.90±0.99	1.29±1.68	0.387	3	0	2.274	0.354	20.206±0.012	20.366±0.054	19.317±0.033	P17
3948582104883273632	187.599802	18.886339	13.5±1.7	-88.59±2.11	-15.68±1.15	0.061	0	0	1.040	0.318	20.781±0.014	21.021±0.193	19.873±0.153	P18
309921197948007936	17.766838	29.792370	17.4±3.0	3.49±1.61	7.25±2.26	0.172	0	0	1.201	0.599	20.770±0.018	20.550±0.193	19.942±0.127	P19
4149950169099038240	266.931455	-12.899114	21.9±2.2	-16.46±1.90	0.67±1.23	0.390	5	18	1.639	0.306	20.368±0.030	20.513±0.148	19.555±0.089	P20
6033410078502966784	255.370346	-26.810632	19.5±2.4	-3.65±2.32	-4.42±1.82	0.445	29	16	2.237	0.372	20.452±0.028	20.458±0.108	19.684±0.147	P21
2928185797635630720	107.537105	-22.555094	12.6±1.6	-0.66±1.07	0.38±1.87	0.186	1	0	1.153	0.194	20.647±0.010	21.075±0.136	19.757±0.063	P22
4137297229808521728	264.041050	-14.652376	12.2±2.6	-15.16±2.55	-9.24±2.07	0.050	0	0	1.029	0.359	20.857±0.016	20.938±0.147	20.032±0.112	P23
4124968474672413440	264.497724	-15.685675	15.5±3.9	-10.08±2.76	-1.77±2.04	0.149	0	0	0.980	-0.067	20.937±0.016	21.591±0.389	20.256±0.110	P24
411586015469775168	258.698370	-21.012065	19.6±2.0	8.27±1.15	-1.01±1.52	0.067	0	4	1.917	0.089	20.756±0.014	21.401±0.242	19.858±0.031	P25
4124806709024391424	263.996996	-16.524072	12.2±2.3	-7.74±										

**Table 8.** *Gaia* DR3 parameters for other sources of interest.

<i>Gaia</i> DR3	RA (deg)	DEC (deg)	$Plx$ (mas)	$pmRA$ (mas yr <sup>-1</sup> )	$pmDEC$ (mas yr <sup>-1</sup> )	gha	fmp (%)	fow (%)	ruwe	$ef_{BR}$	$G$ (mag)	$G_{BP}$ (mag)	$G_{RP}$ (mag)	Flag
283928743068277376	76.501845	59.055930	27.7±0.3	17.44±0.30	-345.56±0.27	0.045	0	0	1.025	0.139	19.635±0.004	19.503±0.048	19.506±0.079	OP
4353607450860305024	251.071265	-4.830122	12.7±0.9	80.58±0.95	-45.40±0.75	0.051	1	0	1.042	0.041	20.522±0.007	21.171±0.152	19.686±0.057	DZ-E
3905335598144227200	185.201364	9.235241	26.7±0.3	-346.18±0.48	-388.23±0.28	0.065	0	2	1.006	-0.084	19.606±0.005	20.031±0.069	19.160±0.059	DC1
740483560857296768*	152.922607	28.763239	67.9±0.1	-124.83±0.06	-713.24±0.04	0.019	0	0	0.997	0.012	16.547±0.004	17.352±0.007	15.649±0.006	DQpec
900742499823605632	123.541222	30.313644	11.1±2.9	-4.49±2.17	-15.64±1.32	0.070	0	0	1.073	0.123	20.821±0.021	21.260±0.420	20.017±0.218	RC1
4389594118549228416	263.707709	5.145780	10.8±2.8	-9.01±2.24	-9.89±1.39	0.094	0	0	1.005	0.153	20.942±0.016	21.301±0.287	20.159±0.128	RC2
4780916942594976768	66.245093	-52.624239	11.1±2.6	29.24±2.44	-28.41±2.17	0.094	0	0	1.159	0.120	20.901±0.015	21.474±0.394	20.009±0.135	RC3
3618788707439181440	208.721840	-8.839919	14.6±3.0	-8.85±1.90	10.41±1.81	0.139	0	0	1.012	0.103	20.861±0.018	21.421±0.416	20.000±0.169	RC4
4906188219358053248	5.036097	-59.829282	10.7±2.0	53.79±2.67	-19.03±2.10	0.031	0	0	1.148	0.157	20.879±0.014	21.356±0.420	20.003±0.142	RC5
6584418167391671808	326.985302	-40.591551	35.8±0.5	-84.11±0.42	-112.39±0.42	0.057	0	0	1.059	-0.028	19.959±0.008	20.949±0.089	19.024±0.046	DZQH
5616323124310350976*	109.188531	-26.081808	33.6±0.2	-51.00±0.14	200.30±0.20	0.008	0	0	0.996	-0.008	18.910±0.003	20.143±0.040	17.829±0.012	VR
6829498935560722560**	319.524667	-20.989472	–	–	–	0.664	14	66	–	3.029	20.629±0.019	19.263±0.507	19.156±0.143	(UV2)
5777941133042341632**	250.745035	-76.517860	–	–	–	0.395	52	1	–	0.494	16.089±0.014	16.129±0.004	15.137±0.004	(UV3)
6029611888623576960**	253.732744	-29.553470	–	–	–	1.068	16	73	–	0.419	20.288±0.060	20.717±0.005	19.141±0.115	(Rad_c)
3948582104883968384*	187.600219	18.884928	5.9±0.0	-90.56±0.04	-15.72±0.03	0.009	0	0	0.987	0.013	15.694±0.003	16.995±0.005	14.565±0.004	(P18)
4149950169090938112**	266.931536	-12.899047	–	–	–	0.481	1	20	–	-0.067	20.188±0.022	20.720±0.081	19.612±0.106	(P20)
6033410082822657280**	255.370155	-26.810740	–	–	–	0.642	8	33	–	0.612	20.404±0.039	20.278±0.128	19.466±0.148	(P21)
4115860154696775296**	258.698092	-21.012248	–	–	–	0.114	0	30	–	0.256	20.985±0.028	22.030±0.337	19.713±0.218	(P25)
4313639928323511936**	285.198566	11.797409	–	–	–	0.036	0	36	–	9.066	20.592±0.019	20.557±0.393	17.169±3.012	(P32)
Median DR3 6ps	–	–	–	–	–	0.031	1.0	3.8	1.029	–	20	–	–	–
Median DR3 6ps	–	–	–	–	–	0.071	0.5	2.1	1.048	–	21	–	–	–

Notes. gha, fmp, fow, and  $ef_{BR}$  stand for the `ipd_gof_harmonic_amplitude`, `ipd_frac_multi_peak`, `ipd_frac_odd_win`, and `phot_bp_rp_excess_factor_corrected` *Gaia* DR3 parameters. \* or \*\*: 5- or 2- instead of 6-parameter solutions (6ps). For comparison, median values for *Gaia* DR3 6ps sources are indicated at the bottom. Abbreviations: optically peculiar (OP), enriched DZ (DZ-E), red colour (RC), and very red (VR). Sources of interest near the main sources are indicated with the associated flag in parenthesis; except for *Gaia* DR3577941133042341632, their angular separation and relative orientation are indicated in the binarity-indicator column ‘Vis.’ in Table 9.

its suppressed SDSS  $u$ -band flux and slightly curved SDSS- and NSC  $griz$ -band SED peaking at  $gr$  bands suggest a white dwarf profile (Fig. 13). For its optical spectral index, it would also be detectable in RASS but it is not, suggesting that it may indeed have mostly a curved profile. Similar verifications can be done for the other sources that are represented in Figs. 6 and 7. Assuming unbroken power-law profiles, sources with slopes  $\alpha_\nu > -0.5$  would be detectable at radio in NVSS, and those with  $\alpha_\nu > 1.0 - 1.5$  would be undetectable in RASS (as commented already in Section 2.3). This makes the latter type of sources also interesting for the search of nearby pulsars.

Besides this, the various colour–colour diagrams in the on-line supplementary material, starting with Fig. F7 and based on  $ugrizyJHK_sW1W2$ -band magnitudes, allow us to assess the colours of the sources with regard to the power-law spectral indices. The expected power-law colours involving PS1- and SDSS photometry are represented by the pink- and blue dashed lines. The assessment is relatively easy for sources having almost one single SED component at the involved bandpasses, such as UV7, P3, and P4 in the  $i - W1$  versus  $r - i$  (Fig. F15) and  $J - W1$  versus  $r - J$  diagrams (Fig. F16). Several of the plotted sources present a spread in their individual PS1- (pink), SDSS- (blue), and NSC (yellow) photometry (linked with solid lines), of up to 0.3–0.5 mag or more, as shown in the colour–colour diagrams involving the  $g - r$  and  $r - i$  (Fig. F7), and especially the  $i - z$  (Fig. F8) and  $z - y$  colours (Fig. F11). This could be caused by observational- and calibration differences, variability, and binarity. For example, in the  $z - J$  versus  $i - z$  diagram of Fig. F12, several of the SDSS blue symbols connected with the blue lines to the PS1 pink symbols are to the right and lower. For some of these, this could be explained partly by the SDSS  $z$ -band filter being broader, redwards, than the PS1  $z$ -band filter, implying that, in principle, for sources that are persistently red the SDSS  $i - z$  colour is redder and the  $z - J$  colour is bluer than when using PS1 photometry (see for example the SED of UV13), and vice versa for persistently blue sources (the magnitude difference  $m_1 - m_2$  increases with the flux ratio  $F_2/F_1$ ).

## 4 DISCUSSION

We find about two X-ray-, 15 ultraviolet-, one radio- and about five power-law profile candidates. Their *Gaia* parameters are in Table 7, their PS1- and infrared photometry in Table E1, and SDSS- and NSC photometry in Table E2. Also we find five isolated red-colour dwarfs with M-type colours, white dwarf distances, and no indication of binarity, whose classification depends on their true distances (Appendix D). For these five objects and some other sources discussed in this study, the parameters and photometry are listed in Tables 8, E3, and E4.

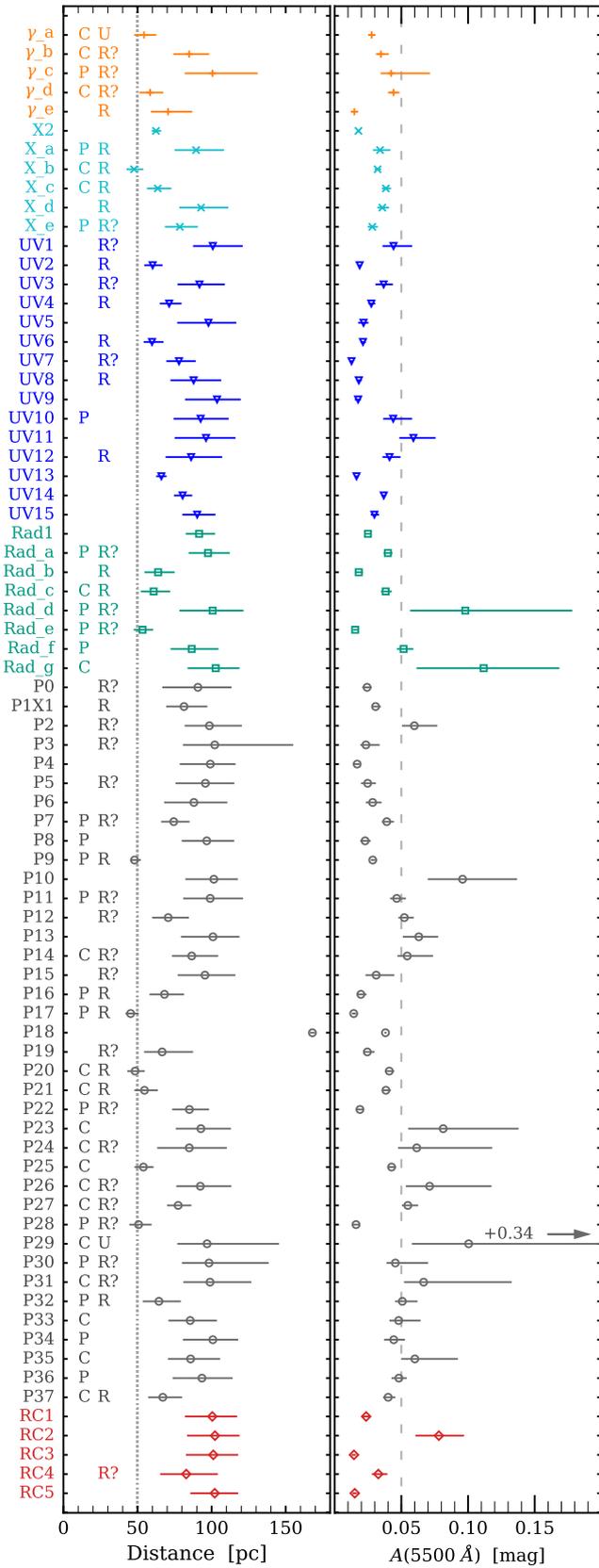
Sources of Tables 7 and 8 are represented in the following colour–absolute magnitude diagrams:  $M_z$  versus  $i - z$  (Fig. 19), and  $M_G$  versus  $G_{BP} - G$  (Fig. F1),  $G - G_{RP}$  (Fig. F2),  $G_{BP} - G_{RP}$  (Fig. F3),  $G - J$  (Fig. F4),  $i - z$  (Fig. F5), and  $i - J$  (Fig. F6). These are also represented in the colour–colour diagrams:  $r - i$  versus  $g - r$  (Fig. F7),  $i - z$  versus  $g - r$  (Fig. F8),  $g - r$  versus  $u - g$  (Fig. F9),  $r - i$  versus  $u - g$  (Fig. F10),  $z - y$  versus  $i - z$  (Fig. F11),  $z - J$  versus  $i - z$  (Fig. F12),  $J - K_s$  versus  $i - z$  (Fig. F13),  $J - H$  versus  $z - J$  (Fig. F14),  $i - W1$  versus  $r - i$  (Fig. F15),  $J - W1$  versus  $r - J$  (Fig. F16), and  $W1 - W2$  versus  $r - J$  (Fig. F17). The figures prepended with a letter are available as online supplementary material.

The SEDs comprising infrared, optical, and ultraviolet fluxes of the sources are available as online supplementary material and grouped per search category:  $\gamma$ -ray (Fig. G1); X-ray (Fig. G2); ultraviolet (Fig. G3); radio (Fig. G4); close-to power-law profile (Fig. G5); red-colour dwarf (Fig. G6).

### 4.1 Interstellar extinction and sky distribution

To characterise the sources further, we consider the amount of interstellar extinction these could have and their sky distribution.

We considered the high-resolution, spectro-photometrically calibrated, *Gaia* (E)DR3-2MASS 3D map of the Galactic extinction



**Figure 16.** Distance (*left panel*) and cumulative  $A_{5500 \text{ \AA}}$  extinction (*right panel*) of the sources ordered as in Tables 7, 8, and 9. Some sources are towards the Galactic plane ( $|b| < 15^\circ$ ; ‘P’) or centre ( $|l| < 15^\circ$ ,  $|b| < 15^\circ$ ; ‘C’), or have a photo-astrometric indication (Table 9) that these could be resolved (‘R’), possibly resolved (‘R?’), or unresolved (‘U’) binaries.

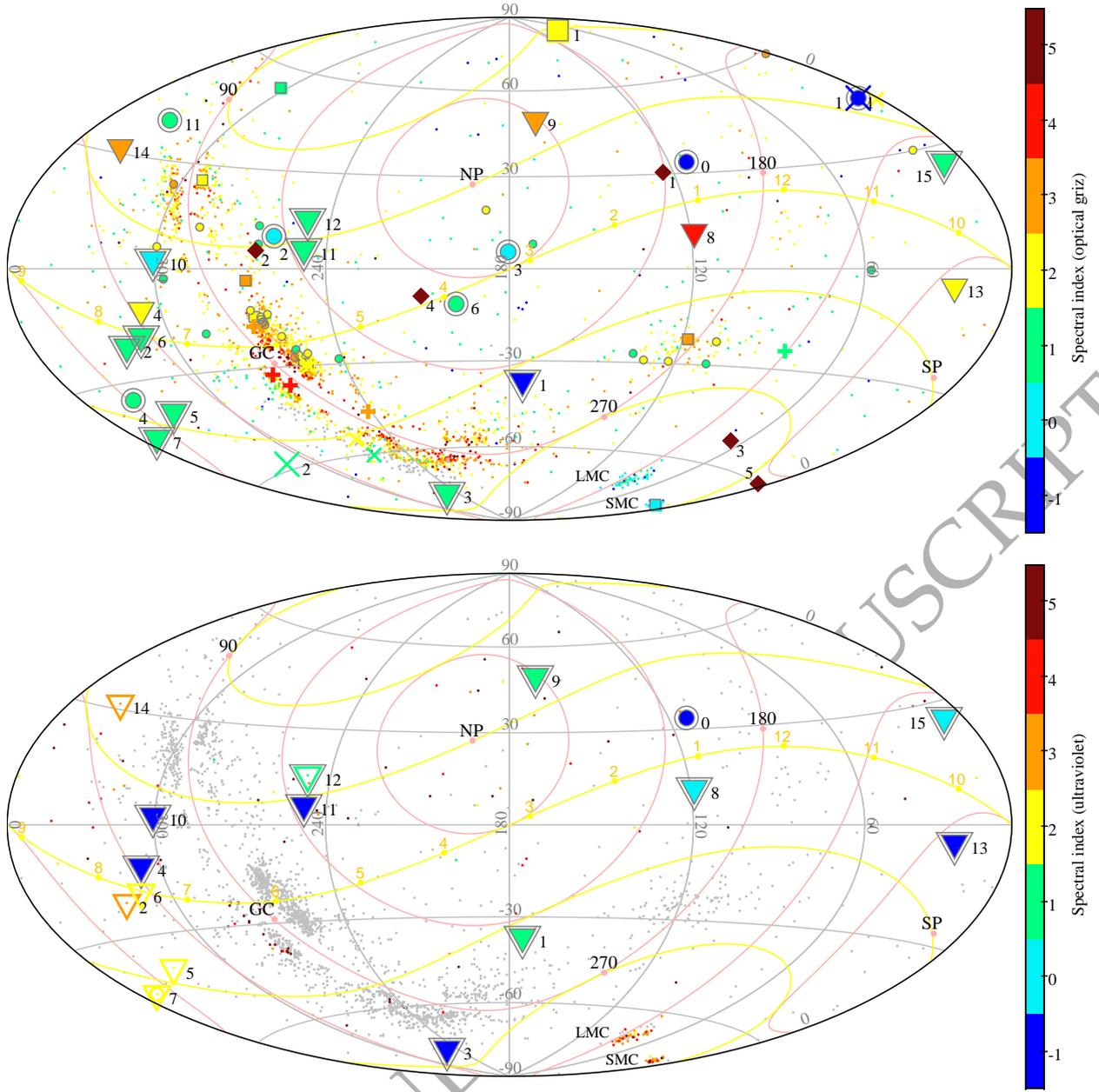
density from Vergely et al. (2022). We used the associated tool<sup>7</sup> to retrieve the  $A_{5500 \text{ \AA}}$  cumulative monochromatic extinction as a function of distance, at the sky coordinates of the sources. In the left- and right panels of Fig. 16, we show the ranges of distance and cumulative extinction for each of the sources as ordered and labelled in Tables 7 and 8. The  $A_{5500 \text{ \AA}}$  ranges do not include the uncertainties in the cumulative extinction, which, at the upper distance, are always smaller than 0.005 mag and thus negligible. In the left panel, we indicate the sources that are towards the Galactic plane ( $|b| < 15^\circ$ ; ‘P’) or centre ( $|l| < 15^\circ$ ,  $|b| < 15^\circ$ ; ‘C’), and those that have a photo-astrometric indication that these could be resolved (‘R’), possibly resolved (‘R?’), or unresolved (‘U’) binaries (see Section 4.2.2 and Table 9). Most candidates of interest are at higher Galactic latitudes ( $|b| > 15^\circ$ ) and their  $A_{5500 \text{ \AA}}$  values are smaller than 0.10 mag and a priori negligible.

Nevertheless, the distances on which the cumulative extinctions are estimated depend primarily on the parallax measurements and whether the sources are binaries. The upward-corrected distance from 79 pc ( $d_{50}$ ) to 168 pc of P18, which is comoving with a brighter star (Appendix C), and the white-dwarf distances of the five isolated red-colour sources (Appendix D), which if these were M-type dwarfs would be 3–9 times farther, indicate that the distances of the sources with low  $snr_\pi$  ( $< 10$ ) should be considered with caution.

In Fig. 17, we show the sky distribution of the sources in equatorial coordinates. The 2464 *Gaia* sources from the colour-selected subsample are represented by very small dots. Probable candidates are represented by larger symbols and numbered as in their labels. The sources are colour-coded as a function of the spectral index or slope  $\alpha_\nu$ . At the (red-)optical (*top panel*), we derived PS1, SDSS, and NSC slopes separately and based on at least two of the *griz* bands; we adopted the one with the largest number of bands covered and smallest uncertainty. For  $\gamma_e$  and X<sub>e</sub>, we adopted the  $G_{BP} - G_{RP}$  slope, and for UV3 the  $r - G_{RP}$  slope. At the blue-optical-ultraviolet (*bottom panel*), we adopted preferentially the slopes based on contiguous bands at the shortest wavelengths, that is *NUV* and *FUV*, else *u* and *NUV*, else *g* and *NUV*, else *g* and *u* (derived from SDSS and NSC separately; *gU* in the case of P0). Only one source has a slope at optical-ultraviolet of  $\alpha_\nu < -1.5$  (UV13w at *gu*). For the red components,  $\alpha_\nu$  values of  $-1.5$  to  $6.5$  correspond roughly to  $T_{\text{eff}}$  of 25 000 to 2 000 K. For the blue components and as measured at varying blue-optical-ultraviolet bands,  $\alpha_\nu$  values of about  $[-1, 1]$  correspond roughly to  $T_{\text{eff}}$  of 10 000–50 000 K.

From Figs. 16 and 17, and Table 9, we see that PIX1–X2, UV1–UV15, Rad1, P0–P6, and RC1–RC5 are relatively far from the direction of the Galactic plane. Differently,  $\gamma_a$ – $\gamma_d$  and most of P7–P37 are towards the Galactic plane or Bulge (though P15, P18, and P19 are clear exceptions); they have red spectral slopes of  $\alpha_\nu = 2.9 - 4.4$  and  $1.0 - 3.0$ , respectively. Six of P7–P37 cluster near  $(l, b) = (10, 9)^\circ$ , towards the Galactic centre. *Gaia* DR3 4124968474672413440 (P24), P26, and P27 cluster within 30 arcmin (all three have  $\alpha_\nu$  of about 2.17), followed by *Gaia* DR3 4137297229808521728 (P23;  $\alpha_\nu = 2.13$ ) at about 1.4 deg and *Gaia* DR3 4138259749157475200 (P29;  $\alpha_\nu = 2.39$ ) and P20 ( $\alpha_\nu = 1.77$ ) at 3 and 4 deg. Generally, the gamma-ray- and reddest P sources tend to appear towards crowded stellar regions, indicating that their current trigonometric distances might be spurious and probably underestimated. Their profiles might be shaped by interstellar extinction cumulated over large distances. The optical profiles of the outward-located sources are more likely to be intrinsic.

<sup>7</sup> G-TOMO at <https://explore-platform.eu/project/deliverables>



**Figure 17.** Sky distribution in equatorial coordinates (Aeiff projection). The 2464 *Gaia* sources from the colour-selected subsample are represented by very small dots.  $\gamma$ -, X-, ultraviolet-, radio-, power-law profile-, and very red-colour flagged sources are indicated by pluses, crosses, triangles, squares, circles, and lozenges, respectively. Probable candidates are represented by larger symbols and numbered. Sources are colour-coded as a function of the  $\alpha_v$  spectral index (i.e. slope) of their (red-)optical component at *griz* bands (*top panel*) and blue-optical-ultraviolet component (*bottom panel*). The highest- and lowest colour bins include spectral index values greater than 5.5 and smaller than -1.5, respectively. Candidates with low ultraviolet excesses are represented by open triangles in the bottom panel. Sources without available slope value are in grey colour. Numbered candidates with  $\alpha_v < 1.5$  are encased in a larger symbol of same shape (except X2). Galactic- and ecliptic coordinate grids are shown in pink and yellow. The sky locations of the centre, north pole, and south pole of the Galaxy, and the Large- and Small Magellanic Clouds are labelled as GC, NP, SP, LMC, and SMC, respectively. For each emphasized location on the ecliptic, the month (approximate mid-month date) of optimal night visibility from Earth is indicated.

#### 4.2 Neutron stars as resolved emitters or unresolved companions

The 2464 *Gaia* sources of the colour-selected subsample have practically no gamma- nor X-ray counterparts. Even the PIX1 and X2 candidates have each at least one optical neighbour source that could be a potential counterpart to the X-ray match. Assuming no significant interstellar extinction nor self-absorption at X rays, these two

candidates are too faint at X-rays for their *G*-band absolute magnitudes to be typical young thermally-emitting neutron stars. However, these could be, for example, weakly interacting binaries consisting of a white dwarf and a compact- or degenerate companion. A low occurrence of X-ray- and gamma-ray pulsars is also apparent in the ATNF database (although it excludes accretion-powered- and X-ray-millisecond pulsars): out of the 3320 pulsars, 122 (4 per cent) are non-radio pulsars, emitting pulses at infrared- or higher frequencies.

#### 4.2.1 Power-law emission

We find power-law components at the ultraviolet–optical in at least UV3 and UV4 (Figs. 10 and G3), UV8 and UV9 (Fig. 18), and up to the mid-infrared W2 band in UV7 (Fig. 18). We also find approximately-straight profiles at the optical–infrared (up to W2 band) in P3, P4, and P6 (Fig. 15), which have small proper motions of 0–6 mas yr<sup>-1</sup>. Finally, we find at least one possible transient power-law profile at the optical in P2 (Figs. 13 and G5).

The power-law extent to the infrared of the candidates can be contrasted with that of known pulsars. For instance, the Vela Pulsar has a flat power law emission ( $\alpha_\nu = 0$ ) from the ultraviolet (10<sup>15.4</sup> Hz) to the near-infrared  $K_s$  band (10<sup>14.1</sup> Hz) (fig. 2 in Zyuzin et al. 2013). PSR B0656+14 has  $JHK_s$ -band fluxes that tend to be along the main power law fit (Zharikov et al. 2021). The Geminga Pulsar has a power law profile constrained up to the  $H$  band, and at optical, flux deviations of about 0.15 dex relative to the combined fit (fig. 7 in Shibanov et al. 2006). In the case of the Crab Pulsar, the power law is maintained up to the  $L'$  band at the mid-infrared, and plausibly up to 8  $\mu\text{m}$  depending on the flux contribution of the knot (Sandberg & Sollerman 2009). Still, not all of the pulsars detected in the optical and that we mention in this study are constrained in the infrared nor even entirely in the optical (see Section 2.1 and Fig. 2), mostly because of their larger distances and faintness.

Elucidating the true emission mechanisms and temporal variability of the sources is beyond the scope of the present study. However, we briefly mention some possible causes of the observed features.

In the most fortunate case(s), the power-law profile might indeed stem from synchrotron or gyro-synchrotron emission (from accelerated charged particles), as observed in pulsars (Buschauer & Benford 1976; Melrose et al. 2021). The departure from a power-law profile at other wavelength ranges or epochs may indicate that:

- (i) the emission mechanism differs,
- (ii) the observability of the emission mechanism differs, because of for example surrounding diffuse material, a binary companion, or self-absorption (cf. the synchrotron self-absorption roll-over; O’Connor et al. 2005),
- (iii) the power-law emission is transient and either unique or of low occurrence (we note the pulse period of 18.18 min of the GLEAM-X J162759.5–523504.3 radio transient, proposed to be a compact star; Hurley-Walker et al. 2022), or
- (iv) the power-law profile is not caused by synchrotron emission but by a combination of observed flux fluctuations from thermally emitting sources, unresolved or partially resolved blends of blue and red components in binaries, and reddening.

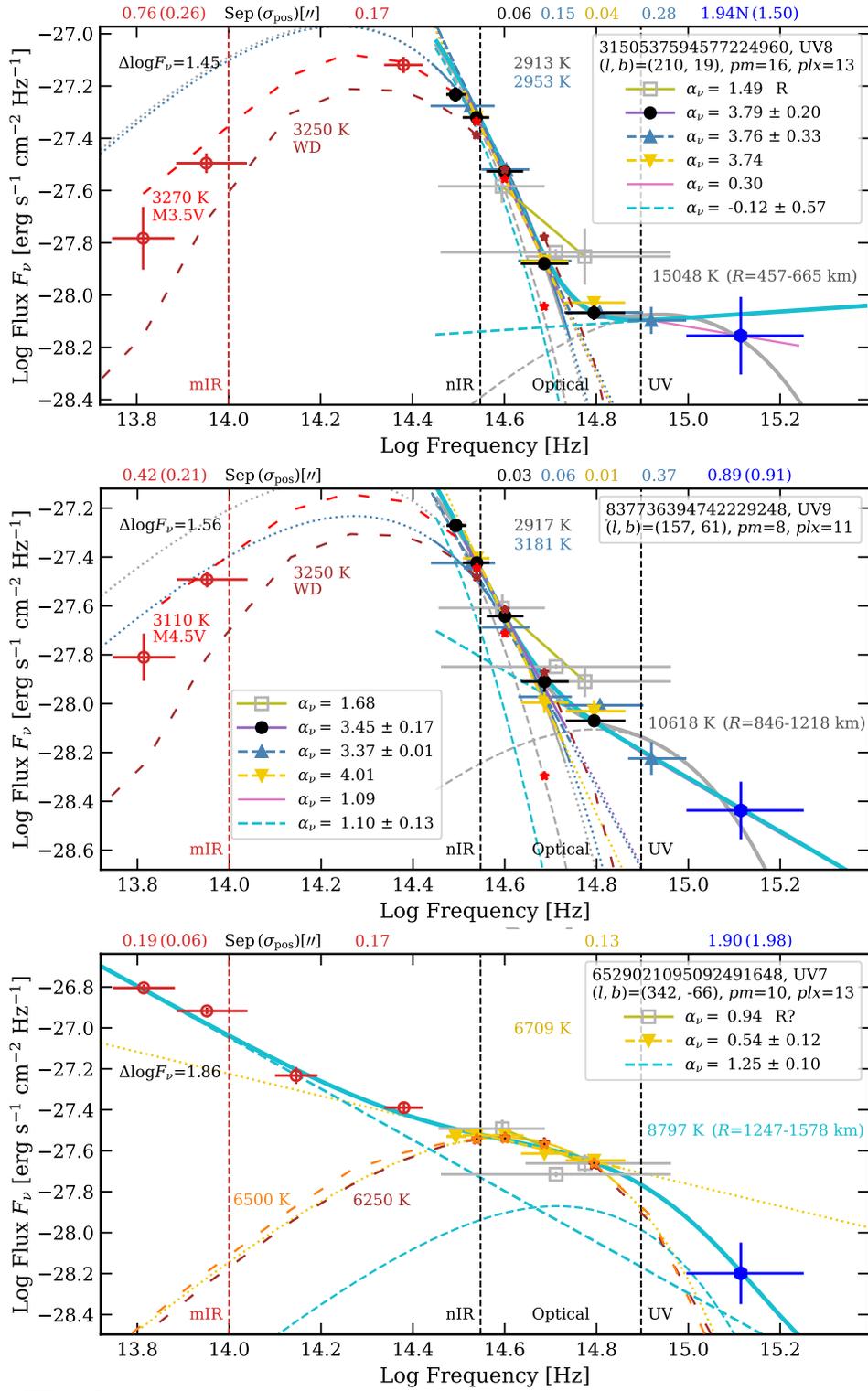
The search for ultraviolet excesses and power-law profiles among the sources led us to identify intricate blackbody- and power-law profiles, where the power-law component is substantiated by ultraviolet- or infrared measurements. This suggests that more power-law emission candidates could be found among colour-selected optical sources and using ultraviolet- and infrared data. In continuation, we discuss UV7, UV8, and UV9, pushing the envelope of interpretation a bit, because these represent classes of sources that may hold neutron stars.

In the cases of UV8 and UV9 (Fig. 18), we assume that (i) the two components in the SED have different origins, that is the SED divide does not result from opacity, (ii) interstellar extinction can be neglected, and (iii) the underlying  $griz$ -band part of the red component can be approximated by a blackbody curve. We then fit the  $NUVgriz$ -band fluxes ( $griz$  from SDSS and PS1 for UV8 and UV9, respectively) by two components consisting of (a) a cool blackbody

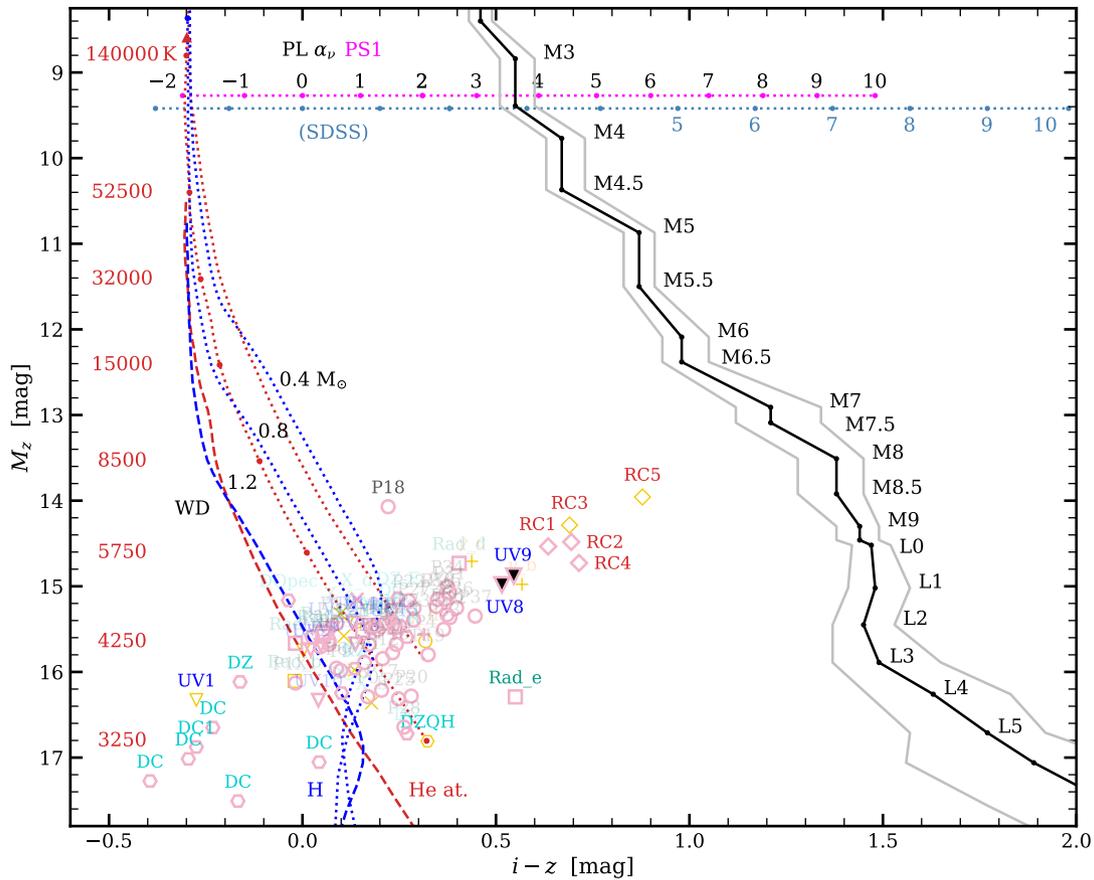
and a power law (cyan lines), and (b) a cool blackbody and a hot blackbody (dark-grey lines). We find power-law spectral indices of  $\alpha_\nu = -0.12 \pm 0.57$  and  $1.10 \pm 0.13$ . Assuming unbroken power laws, UV8 and UV9 are expected to be detected well- and marginally at X rays in RASS, as indicated in the corresponding panels in Figs. 6 and 7. However these are not detected; the 2RXS exposure map at their coordinates indicate exposure times of about 357 and 439 s. An underlying, power-law component at ultraviolet–optical–infrared appears more plausible in UV8 than in UV9, because the power-law extension to the mid infrared in UV8 is compatible with the W1W2 fluxes. In principle, independent of the stellar type- and distance of the red component (for example white dwarf at  $\sim 100$  pc or M-type dwarf at  $\sim 1000$  pc), the power law component could stem from a neutron star pulsar. Alternatively, the blue component could be thermal emission, and originate from a neutron star or its surroundings if its distance to us is small enough. The hot-blackbody parts of UV8 and UV9 imply effective temperatures of  $T_{\text{eff}} = 15\,048$  and  $10\,618$  K, and, assuming the  $d50$  distances, thermal radiuses of  $R = 552$  and  $1060$  km. These are 3.9 and 2.0 times smaller than the smallest known white dwarf radius, of 2140 km (see Section 4.2.2), which we use as a representative observational lower-limit. According to theoretical predictions of white dwarfs including the effects of general relativity, at  $T_{\text{eff}} = 10\,000$  K, a theoretical radius as small as 1000 km is only possible for 1.37  $M_\odot$ , the highest mass for a white-dwarf and above which it becomes gravitationally unstable (Althaus et al. 2022). Thus, taking the numbers and interpretation at face value, the blue components of UV8 and UV9 challenge the neutron star–white dwarf limit. To be less small than the smallest known white dwarf, the hot components would have to be at least 3.9 and 2.0 times farther than the  $d50$  distances ( $R = d \times \theta$ , where  $\theta$  is the constant angular radius), at  $\geq 340$  and 177 pc.

The red components of UV8 and UV9 have steep  $riz$ -band slopes ( $\alpha_\nu = 3.4 - 3.8$ ), red  $i - z$  colours (0.5–0.6 mag), and curved profiles. Example fits in Fig. 18 indicate that these are either (i) very red- and ultra-cool ( $< 3250$  K) white dwarfs at the *Gaia* distances or (ii) early M-type dwarfs, which as shown in the  $M_z$  versus  $i - z$  colour–absolute magnitude diagram of Fig. 19, would be about 5 mag brighter intrinsically. The ML-type dwarf sequence in this Figure results from complementing the Modern Mean Dwarf Stellar Colour and Effective Temperature Sequence (hereafter MSC) compilation of Eric Mamajek<sup>8</sup> with the MLT-type-dwarf mean PS1 colours from Best et al. (2018). For the SED fitting, we previously converted the MSC absolute magnitudes and colours to fluxes. After subtracting the blue components (power law or blackbody) from the SEDs, the red-optical slopes of UV8 and UV9 are slightly steeper than those of *Gaia* DR3 6584418167391671808 and *Gaia* DR3 5616323124310350976 (Apps et al. 2021), two very red-, nearby (28–30 pc), and faint ( $M_G \approx 16.5 - 17.7$  mag) white-dwarf sources. The former is the coolest spectroscopically-confirmed DZ white dwarf, of  $3048 \pm 35$  K and DZQH type (Elms et al. 2022). Their SEDs are shown in Fig. G6 of the online supplementary material. These two white-dwarf sources have  $G - G_{\text{RP}} = 0.94 - 1.08$  mag and are thus slightly redder than our colour selection boundary. If UV8 and UV9 were M-type dwarfs, then these would be at much larger distances (cf. equation (3)), close to 1 kpc, without accounting for extinction. The low parallax signal-to-noise ratios,  $snr_\pi$  of 5.7 (UV8) and 2.7 (UV9), and low visibility\_periods\_used of about 10 (Table 9) indicate that the

<sup>8</sup> [https://www.pas.rochester.edu/~emamajek/EEM\\_dwarf\\_UBVIJHK\\_colors\\_Teff.txt](https://www.pas.rochester.edu/~emamajek/EEM_dwarf_UBVIJHK_colors_Teff.txt)



**Figure 18.** SEDs with ultraviolet-, optical-, and infrared fluxes of UV8, UV9, and UV7, from the top to bottom. Examples of two-component fits to the *NUVugriz*-band fluxes of UV8 and UV9 are shown: cool blackbody + hot blackbody (dark-grey lines) and cool blackbody + power law (cyan lines). Example fits with early M-type dwarfs (at  $d \sim 1000$  pc) to the red components of UV8 and UV9 are shown by the red dashed line. The fit with the coolest He-atmosphere white-dwarf model available (brown dashed line) suggests that a cooler- or redder model is required to fit the optical–infrared fluxes. For UV7, an example of power law + hot black body fit to all of the fluxes is shown (cyan lines). Same as in Fig. 10.



**Figure 19.**  $M_z$  versus  $i - z$  colour-absolute magnitude diagram, in PS1 photometry unless stated otherwise, and using the distances of Table 9. Only photometry from PS1 (pink), else from NSC (yellow) are represented, for simplicity. A data point is plotted if each of the magnitude errors involved is smaller than 0.4 mag.  $\gamma$ -, X-, ultraviolet-, radio-, power-law profile-, and red-colour flagged sources are represented by pluses, crosses, triangles, squares, circles, and lozenges, and are labelled in orange, cyan, blue, green, grey, and red, respectively. Sources are labelled as in Tables 7 and 8 and can be localised using the text search function in a PDF-document reader. UV8, UV9, RC1–RC5, and other outliers sources are highlighted; the symbols of UV8 and UV9 are filled in black. Spectroscopically confirmed- and other literature white dwarfs mentioned in this study are represented by hexagons and labelled in turquoise. Isomasses of white-dwarf pure He- and H atmospheres are represented by red- and blue lines; those for  $1.2 M_{\odot}$  are dashed and those for  $0.8$  and  $0.4 M_{\odot}$  dotted. Effective temperatures are indicated for the  $0.8 M_{\odot}$  He isomass. The stellar main sequence and its 68 per cent confidence limits are represented by the black- and grey solid lines. Synthetic power-law colours are indicated for PS1- and SDSS photometry.

distances could be larger than the  $d_{50}$  ones. More accurate parallaxes or spectroscopy could solve the classification.

In the case of UV7, its power-law component (Fig. 18) could be pulsar synchrotron emission. The source is well isolated, at  $(l, b) = (342, -66)^{\circ}$ , has a relatively high  $snr_{\pi}$  of 9.4, and a proper motion  $pm = 10.5 \pm 2.6$  mas yr $^{-1}$ , which given the short time-baseline of the available ground-based survey images precludes an accurate verification of whether the source is moving transversally. The NSC  $griz$ -band slope of  $\alpha_{\nu} = 0.54 \pm 0.12$  is prolonged in the infrared by  $JK_S$ -band fluxes and surpassed by about 0.3 dex by  $W1W2$ -band fluxes. In NSC-DES optical images, the PSF is stellar and almost circular. In near-infrared images, the PSF is slightly broader than the average PSF of sources classified as stars, by a factor of about 1.5, this extension leading it to be classified as galaxy ( $p_{\text{Star}} = 0.00$ ,  $p_{\text{Galaxy}} = 0.99$ ) in VHS DR6. However, several pulsars are known to be in diffuse nebulae or knots. In the VISTA-DES-AllWISE (VEXAS-DESW) DR2 catalogue (Khramtsov et al. 2021), its  $grizyJK_SW1W2$  magnitudes, colours, and VHS  $p_{\text{Star}}$  parameter led it to be classified as a quasar ( $p_{\text{QSO}} = 0.99$ ), among the three options, star, quasar, and galaxy. The proper motion amplitude of UV7 is 6.4 and 1.3 times the standard deviations of the proper

motions of the *Gaia* EDR3 crossmatches to the sources classified as quasars and galaxies in VEXAS-DESW (see table 7 in Khramtsov et al. 2021), respectively, and suggest that UV7 could be classified as an extended AGN. However its parallax is 17.8 and 10.0 times the standard deviations of the parallaxes of the two subsets. Unlike the SEDs of the P3 and P4 quasar candidates (Fig. 15), the SED of UV7 appears to have a more obvious, outlined bulk at the optical. We note also that the bulk of UV7 has an  $r$ -band flux dip, as for Rad1 and Rad\_b, which in the case of Rad1, we suggested it to be caused by significant Na I D absorption (Section 3.5). If we fit all of the fluxes by a power law + hot blackbody, assuming that the nominal value of the  $NUV$ -band flux is the true value, we obtain a power-law component of  $\alpha_{\nu} = 1.25 \pm 0.10$  and a black body of  $T_{\text{eff}} = 8797$  K, and, assuming the  $d_{50}$  distance, a thermal radius of  $R = 1387$  km. With  $\alpha_{\nu} > 1.0$ , UV7 is expected to be undetectable at X rays in RASS (see Fig. 7 and Sections 2.3 and 3.8).

For illustrative purpose and for comparison with the ultraviolet-optical(–infrared) fluxes of known neutron stars, we represent the power-law component fits of  $\alpha_{\nu} = -0.12$  and  $1.25$  of UV8 and UV7 by the grey dashed lines in the apparent- (top) and absolute (bottom) SED representations of Fig. 2. These have relatively bright

apparent fluxes, close to those of PSR B0540–69, justifying the broad-optical search for synchrotron emission of pulsars in the solar neighbourhood.

Finally, we remark that the optical colours and faint magnitudes at which we searched for synchrotron emitters overlap with those expected for isolated stellar-mass black holes accreting interstellar matter (Chisholm et al. 2003; Kimura et al. 2021).

#### 4.2.2 Multiplicity

Knowing whether sources are isolated or binaries is important for searches of continuous gravitational wave emission, because binarity implies more modulations in the signal. The Gaia DR3 measurements for  $G \geq 19 - 20$  mag sources are single-source solutions and do not provide the masses of the components and the orbital elements. However, some of these measurements can give indications of binarity. In our search, we consider three types of binarity indicators: (i) *Gaia* photo-astrometric parameters, (ii), visual close neighbours or companions, and (iii) excesses or two components in SEDs.

(i) Useful *Gaia* photo-astrometric parameters for binarity are the parameters: *ruwe*, *ipd\_gof\_harmonic\_amplitude*, *ipd\_frac\_multi\_peak*, and *ipd\_frac\_odd\_win* (Gaia Collaboration et al. 2021a). We paraphrase here briefly their definitions. *ruwe* is the renormalised unit weight error, for the astrometry; a value of *ruwe*  $\gtrsim 1.4$  is indicative of an ill-behaved astrometric solution and may indicate binarity or multiplicity. The *ipd\_gof\_harmonic\_amplitude* parameter measures the amplitude of the variation in the Image Parameters Determination (IPD) goodness of fit (GoF; reduced chi-square) as function of the position angle of the scan direction; the amplitude indicates the level of asymmetry of an image and a large amplitude indicates that the source is double (the associated *ipd\_gof\_harmonic\_phase* parameter indicates the orientation of the asymmetric image). The *ipd\_gof\_harmonic\_amplitude* parameter allows for the identification of spurious solutions, where values greater than 0.1 and a *ruwe* greater than 1.4 indicate resolved doubles, which are not correctly handled yet in the processing. *ipd\_frac\_multi\_peak* provides the percentage of windows (having a successful IPD result) for which the IPD algorithm has identified a double peak, meaning that the detection may be a visually resolved double star (either an optical pair or a physical binary). *ipd\_frac\_odd\_win* provides the percentage of transits having either truncation or multiple gates flagged in one or more windows and in general a non-zero value indicates that this source may be contaminated by another nearby source. In addition, there is the *duplicate\_source* parameter, for *Gaia* pairs of sources closer together than 0.18 arcsec, for which only one source is retained in *Gaia* (E)DR3. Except *Gaia* DR3 5777941133042341632 (see below), none of the sources we list in Tables 7 and 8 is flagged as duplicate.

In the bottom rows of Tables 7 and 8, we indicate for comparison the median values for sources with six-parameter solutions (accounting for the position, parallax, proper motion, and astrometrically-estimated effective wavenumber) at  $G = 20$  and 21 mag<sup>9</sup>. Five-parameter solutions account for the position, parallax, and proper motion, and two-parameter solutions account only for the position.

We assumed sources with:

*ipd\_gof\_harmonic\_amplitude* < 0.1 and *ruwe*  $\geq 1.4$  as unresolved,  
*ipd\_gof\_harmonic\_amplitude*  $\geq 0.1$  and *ruwe*  $\geq 1.4$  as resolved,

<sup>9</sup> In section 4.5.2, Properties of the astrometric data, from Lennart Lindegren, in the *Gaia* (E)DR3 documentation at <https://gea.esac.esa.int>.

and *ipd\_gof\_harmonic\_amplitude*  $\geq 0.1$  and *ruwe* < 1.4 as possibly resolved binaries. These are referred to by the abbreviations U, R, and R?, respectively, in the binary indicator column ‘Ast.’ in Table 9.

The *Gaia* photo-astrometric binarity criteria may be useful for identifying pairs that are too close ( $\leq 0.3$  arcsec) to be resolved visually in the ground-based survey images. Most of our sources have *pm/plx* ratios lesser than one (see Table 9, where for simplicity the ratio error is computed from the linear sum of the relative errors in *pm* and *plx*), implying that the astrometric motion is dominated by parallactic motion (uncertainty) or binarity. Exceptions with relatively large proper motions (*pm/plx* > 3) are X2, UV13, UV14, UV15, Rad1, Rad\_a, P15, P18, and P30.

Among the sources of Table 9, all those that are photo-astrometrically resolved (‘R’) have typically the greatest values of the *astrometric\_excess\_noise* parameter (a measure of the residuals in the astrometric solution), in the range of 5.4–11.3 mas. P29 is not photo-resolved (‘U’), suggesting that, if the source has a companion that causes the high *ruwe* value, then the companion is not visible. Considering the *astrometric\_sigma5d\_max* parameter (the five-dimensional equivalent to the semi-major axis of the *Gaia* position error ellipse, including position, parallax, and proper motion), the sources have values in the range 0.81–4.54 mas, and P29 has the greatest value.

(ii) We checked all the sources of Table 9 for visual companions in single-band images from PS1, SDSS, NSC-NoirLab, and *GALEX*. This allowed us to constrain them beyond an angular separation of approximately 0.3 arcsec, above which binary components, especially of different colours, are easy to identify. The visual companions are either blends with the sources or fully resolved. Most have about the same colour and are as faint or fainter. None of the visual companions has proper motion nor parallax in *Gaia* DR3, except the widely separated and bright M-type companion of P18 (Appendix C). Those that have *Gaia* parameters are listed in Table 8, with indication of associated candidate. *Gaia* can resolve varying percentages of binaries of equal magnitudes down to separations of 0.05 arcsec (Gaia Collaboration et al. 2021b); the completeness may start to decrease at separations < 1.5 arcsec, drop below 80 per cent at < 0.7 arcsec, and reduce to about 10 per cent or less at < 0.4 arcsec (Fabricius et al. 2021). The visual companions are referred to by their angular separation (in arcsec) and approximate relative orientation in the column ‘Vis.’ of binary indicators in Table 9. One particular case is UV12 (*pm* = 15 mas yr<sup>-1</sup>), where the PS1 flux counts decrease symmetrically by about 0.3 arcsec east-west from the source position, without clearly indicating two peaks. We assumed that the source is a 0.6 arcsec wide pair centred on the *Gaia* source position, although it could also be an extended source.

Finally, we checked the sources at wider separations within 10 arcsec, whether these have relatively bright neighbour stars that are comoving or do not have *Gaia* proper motion nor parallax. At 9.4 arcsec north-west from UV3, there is a bright star, *Gaia* DR3 5777941133042341632 ( $G = 16.1$  mag), without proper motion nor parallax, with *ipd\_frac\_multi\_peak* = 52 per cent and *duplicate\_source* = 1, indicating that this bright star is itself probably a binary of separation < 0.18 arcsec. It has a small proper motion, of  $(-9.7 \pm 6.5, 2.6 \pm 7.0)$  mas yr<sup>-1</sup> in CATWISE2020.

(iii) From the crossmatches with other catalogues and from the SEDs, we could identify sources with gamma-ray-, X-ray-, ultraviolet-, and radio excesses, which we consider as probable- or possible indications of binarity. These are referred to in the binary indicator column ‘SED’ in Table 9. The abbreviations  $\gamma$ , X, N, and F stand for *Fermi*, RASS 0.1–2.4 keV, *GALEX NUV*- and *FUV* bands, respectively. Significant- and low ultraviolet-excesses in the SEDs

**Table 9.** Multiplicity of the sources.

Gaia DR3	<i>l</i> (deg)	<i>b</i>	<i>snr</i> <sub>π</sub>	vp	<i>pm</i> / <i>π</i>	<i>d</i> (pc)	gha	fmp (%)	fow (%)	ruwe	Flag	Binarity indicators <sup>a</sup>			<i>d</i> <sub>p</sub> <sup>-</sup> 0.05"	<i>d</i> <sub>p</sub> <sup>+</sup> (au) <sup>b</sup>		System <sup>c</sup>			
												SED (")	Ast.	Vis.(")		0.3"	Vis.	SED	V1	V2	S/A
4043369078205765888	358	-4	8.8	9	0.3±0.1	54.4 ( 6.0, 7.7)	0.072	6	5	1.515	γ_a	γ448.9	U	1.0 SW	2.4	19	62	27896	WD	WD	?
4040994030072768896	354	-3	8.1	9	0.4±0.3	84.9 (10.1,12.9)	0.144	0	0	1.095	γ_b	γ556.7	R?	0.9 SW	3.7	29	88	54404	WD	WD	?
5990998826943947520	335	5	4.1	9	1.0±0.5	100.5 (18.1,30.0)	0.157	0	0	1.049	γ_c	γ1109.4	R?	-	4.1	39	-	144777	WD	-	?
4144738037302227072	11	5	8.9	9	1.1±0.2	58.5 ( 6.7, 8.3)	0.153	0	0	1.135	γ_d	γ187.8	R?	-	2.6	20	-	12551	WD	-	?
2957941232274652032	227	-29	6.6	9	0.6±0.2	70.6 (11.0,15.7)	0.221	3	0	1.435	γ_e	γ1024.2	R	-	3.0	26	-	88381	WD	-	?
6456175155513145344	338	-40	24.9	24	11.9±0.5	62.4 ( 2.3, 2.9)	0.023	0	0	0.996	X2	X47.7	-	-	3.0	20	-	3120	WD	-	?
5922780280824141056	335	-9	6.0	10	0.4±0.3	89.5 (13.9,18.3)	0.161	2	0	1.466	X_a	X35.0	R	-	3.8	32	-	3769	WD	-	?
6027974578382721280	352	8	10.5	14	0.8±0.2	47.6 ( 4.5, 5.7)	0.343	2	0	2.223	X_b	X37.5	R	-	2.2	16	-	1999	WD	-	?
6029621818614152576	353	8	9.0	13	0.4±0.2	63.6 ( 6.7, 8.6)	0.207	12	6	1.568	X_c	X42.7	R	-	2.8	22	-	3086	WD	-	?
384577010978265344	115	-20	6.0	16	0.5±0.2	92.9 (14.1,17.8)	0.141	0	0	1.422	X_d	X57.3	R	-	3.9	33	-	6341	WD	-	?
5914009991961757952	331	-13	8.5	10	0.7±0.3	78.5 ( 9.5,11.6)	0.335	3	0	1.031	X_e	X54.3	R?	-	3.5	27	-	4893	WD	-	?
5386173659617460736*	287	24	6.3	14	1.5±0.5	100.8 (12.7,19.6)	0.362	3	0	1.236	UV1	NF0.32	R?	-	4.4	36	-	39	WD	-	?
6829498931265990656*	28	-41	11.6	12	0.4±0.2	60.2 ( 5.1, 6.1)	0.428	30	0	1.995	UV2	(N)1.55	R	0.57 SW	2.8	20	38	103	WD	WD	?
5777941133043108992*	315	-19	6.0	13	0.2±0.3	91.8 (14.2,16.5)	0.328	0	0	1.208	UV3	NF2.19	R?	-	3.9	32	-	237	WD	-	?
6901051613248041216	33	-27	12.1	15	0.6±0.2	71.3 ( 5.7, 7.8)	0.844	9	0	1.769	UV4	gNF0.72	R	0.6 SW	3.3	24	47	57	WD	-	?
6585452983927662080	3	-49	3.8	10	0.3±0.4	97.9 (20.5,18.2)	0.070	0	0	0.998	UV5	(N)3.04	-	-	3.9	35	-	353	WD	-	?
6858721824326705536	28	-33	11.0	17	0.8±0.2	59.8 ( 5.0, 7.2)	0.299	33	3	2.048	UV6	(N)1.70	R	-	2.7	20	-	114	WD	-	?
6529021095092491648	342	-66	9.4	10	0.8±0.3	78.0 ( 7.9,10.7)	0.302	0	0	1.138	UV7	(N)1.90	R?	-	3.5	27	-	168	WD	-	?
3150537594577224960	210	19	5.7	10	1.2±0.5	87.8 (15.0,18.0)	0.295	1	0	1.440	UV8	guN0.28	R	-	3.6	32	-	30	WD	-	?
837736394742229248	157	61	2.7	11	0.8±0.5	103.6 (21.0,15.4)	0.036	0	0	1.091	UV9	guN0.37	-	-	4.1	36	-	44	WD	-	?
4240872805678917376*	43	-14	4.6	9	0.9±0.5	92.6 (17.7,18.3)	0.098	0	0	1.028	UV10	(N)F0.62	-	-	3.7	33	-	69	WD	-	?
4438623270475014656	21	34	3.5	9	1.4±0.6	96.2 (20.5,19.3)	0.010	0	0	1.036	UV11	N1.54	-	-	3.8	35	-	178	WD	-	?
4465431356821050496	32	38	4.8	13	1.1±0.5	86.2 (16.6,20.4)	0.300	3	6	1.418	UV12	(N)1.45	R	0.6 EW	3.5	32	64	155	WD	WD	?
2480784311444314880*	150	-65	21.7	16	16.9±0.8	66.1 ( 2.9, 2.9)	0.065	0	0	1.148	UV13	u0.08	-	-	3.2	21	-	6	WD	-	?
1900830823016998144	90	-22	15.0	18	15.7±1.1	80.4 ( 5.2, 5.9)	0.029	0	0	0.986	UV14	(u)0.04	-	-	3.8	26	-	3	WD	-	?
280766365638075264	118	-37	8.9	14	16.1±2.0	90.3 ( 9.4,11.7)	0.046	0	0	1.279	UV15	u0.58	-	-	4.0	31	-	59	WD	-	?
557277267992311808	131	24	10.3	15	9.9±1.2	91.5 ( 8.4,10.2)	0.065	0	0	0.977	Rad1	rad5.63	-	-	4.2	31	-	573	WD	-	?
2185585922087166720	89	11	6.4	12	3.9±0.8	97.6 (12.5,14.1)	0.119	0	0	0.909	Rad_a	rad13.16	R?	-	4.3	33	-	1470	WD	-	?
4688982132605446784	303	-45	7.4	14	0.9±0.3	63.9 ( 8.6,10.5)	0.185	9	0	2.100	Rad_b	rad1.58	R	-	2.8	22	-	118	WD	-	?
6029611888623577088*	353	9	8.0	13	0.9±0.2	60.9 ( 8.0,10.6)	0.294	14	6	2.313	Rad_c	rad11.56	R	0.89 E	2.6	21	64	826	WD	WD	?
4176647926320238720	22	12	3.9	9	0.7±0.4	100.7 (21.8,20.2)	0.108	0	0	1.005	Rad_d	rad11.75	R?	-	3.9	36	-	1420	WD	-	?
5711114877897853696	240	2	9.5	9	0.2±0.2	53.4 ( 5.4, 6.6)	0.203	0	0	1.359	Rad_e	rad11.15	R?	-	2.4	18	-	668	WD	-	?
2024652913390061952	60	4	6.3	11	0.3±0.2	86.6 (13.7,17.5)	0.055	0	0	1.154	Rad_f	rad5.96	-	0.7 W	3.6	31	73	621	WD	WD	?
4149153813464969856	12	8	3.9	9	0.3±0.3	102.7 (18.4,15.5)	0.087	0	0	1.086	Rad_g	rad12.14	-	-	4.2	35	-	1435	WD	-	?
892683904225248000	186	22	3.3	10	0.6±0.4	90.7 (23.4,22.1)	0.118	0	0	1.095	P0	-	R?	-	3.4	34	-	-	WD	-	?
387812285286341504	120	-19	6.7	9	1.0±0.2	81.4 (11.4,12.2)	0.371	7	0	7.570	PIX1	X44.1	R	-	3.5	29	-	4262	WD	-	?
4443619962406121088*	31	26	5.4	14	1.0±0.5	98.5 (16.1,21.3)	0.173	0	0	1.309	P2	-	R?	-	4.1	36	-	-	WD	-	?
389792739739888128	272	65	2.8	10	0.5±0.4	102.1 (20.9,52.4)	0.181	0	0	0.991	P3	-	R?	-	4.1	46	-	-	WD	-	?
6600314326685634816	10	-58	3.2	10	0.3±0.3	99.1 (20.0,16.5)	0.064	0	0	1.038	P4	-	-	4.0	35	-	-	WD	-	?	
3910666820788919936	254	62	3.9	10	0.2±0.3	95.8 (19.6,18.9)	0.343	0	0	0.926	P5	-	R?	-	3.8	34	-	-	WD	-	?
3622634116211982976	310	51	4.1	9	0.0±0.2	88.0 (19.5,22.0)	0.071	1	0	1.196	P6	-	-	3.4	33	-	-	WD	-	?	
4234582018625351936*	36	-13	9.5	11	1.2±0.3	74.4 ( 7.9,10.1)	0.300	0	0	1.387	P7	-	R?	-	3.3	25	-	-	WD	-	?
5606206865714606208	242	-9	5.0	9	0.4±0.3	96.7 (16.3,17.9)	0.051	0	0	1.008	P8	-	-	4.0	34	-	-	WD	-	?	
4085595994046913792*	17	-11	18.1	11	0.4±0.1	48.0 ( 2.4, 3.7)	0.206	0	0	2.692	P9	-	R	0.8 NE	2.3	15	41	-	WD	WD	?
6041917107322758016*	347	17	3.8	9	1.2±0.6	101.5 (18.6,15.6)	0.097	0	0	1.083	P10	-	-	4.1	35	-	-	WD	-	?	
1959239908639738240	91	-12	4.7	9	1.0±0.4	99.0 (17.6,21.6)	0.113	0	0	1.054	P11	-	R?	-	4.1	36	-	-	WD	-	?
4486941991858372352	30	21	6.8	10	0.5±0.3	70.7 (10.2,13.4)	0.137	0	0	1.135	P12	-	R?	0.8 E	3.0	25	67	-	WD	WD	?
4494124177899820800	36	22	2.8	9	0.5±0.5	100.9 (21.0,17.3)	0.064	0	0	0.875	P13	-	-	4.0	35	-	-	WD	-	?	
4112307735705947264	358	10	6.7	10	0.7±0.3	86.6 (12.7,17.2)	0.112	0	0	1.093	P14	-	R?	0.8 NE	3.7	31	83	-	WD	WD	?
3257308626125076480	189	-40	4.1	11	5.9±1.6	95.5 (17.8,19.9)	0.168	0	0	1.022	P15	-	R?	-	3.9	35	-	-	WD	-	?
5648417357621486208	253	13	7.3	13	0.3±0.3	68.2 ( 9.5,12.6)	0.127	2	0	1.486	P16	-	R	-	2.9	24	-	-	WD	-	?
5642345785702095616	252	8	14.0	24	0.2±0.1	45.4 ( 2.8, 4.8)	0.387	3	0	2.274	P17	-	R	-	2.1	15	-	-	WD	-	?
3948582104883237632	271	80	7.9	12	6.7±1.0	168.0 ( 1.9, 1.0)	0.061	0	0	1.040	P18	-	-	5.282 S	8.3	51	893	-	WD	MS	?
309921197948007936	128	-33	5.8	9	0.5±0.2	66.6 (11.6,20.3)	0.172	0	0	1.201	P19	-	R?	0.9 NW	2.8	16	78	-	WD	WD	?
4149950169090938240	14	8	10.0	11	0.8±0.2	48.4 ( 4.7, 5.9)	0.390	5	18	1.639	P20	-	R	0.37 NE	2.2	16	20	-	WD	WD	?
6033410078502966784	356	9	8.1	11	0.3±0.2	54.7 ( 6.2, 8.4)	0.445	29	16	2.237	P21	-	R	0.72 SW	2.4	19	45	-	WD	WD	?
2928185797635630720	235	-6	7.8	15	0.1±0.2	85.0 (11.0,12.7)	0.186	1	0	1.153	P22	-	R?	-	3.7	29	-	-	WD	-	?
4137297229808521728	11	9	4.8	10	1.5±0.6	92.7 (16.3,19.7)	0.050	0	0	1.029	P23	-	-	3.8	34	-	-	WD	-	?	
4124968474672413440	10	8	3.9	13	0.7±0.4	84.9 (21.0,24.8)	0.149	0	0	0.980	P24	-	R?	-	3.2	33	-	-	WD	-	?
4115860154696775168	3	10	10.0	10	0.4±0.2	54.0 ( 5.4, 6.2)	0.067	0	4	1.197	P25	-	-	1.15 SW	2.4	18	69	-	WD	WD	?
4124806709024391424	9	8	5.3	11	0.6±0.3	92.4 (15.6,20.3)	0.177	0	0	1.313	P26	-	R?	-	3.8	34	-	-	WD	-	?
4125016578273139456	10	9	10.6	14	0.1±0.1	77.4 ( 6.9, 8.3)	0.216	0	0	1.092	P27	-	R?	-	3.5	26	-	-	WD	-	?
5596729522158314752	248	2	7.9	10	0.5±0.2	50.7 ( 5.6, 8.2)	0.346														

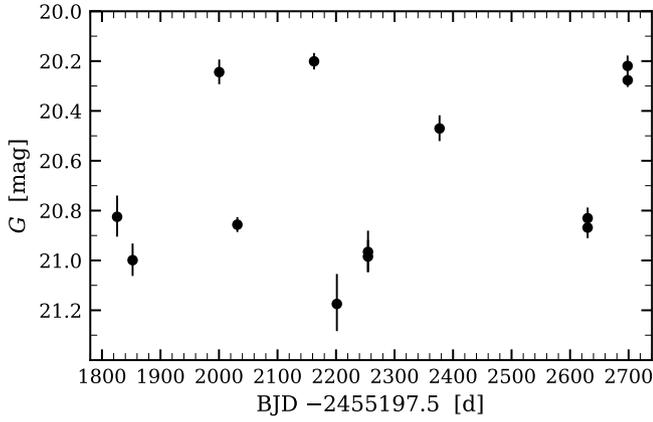


Figure 20.  $G$ -band magnitude versus time diagram of P1X1.

are indicated without- and within parenthesis. We provide the angular separation between the *Gaia* coordinates and the counterpart centroid. For UV8, UV9, UV13, UV14, and UV15, we adopt the angular separation with SDSS  $u$  band instead of *GALEX*. We note that the  $\gamma$ , X-ray, and a few of the radio counterparts have large coordinates uncertainties; also, UV4, UV10, and UV11 have *NUV*- or *FUV* counts that spread up to more than 2.5, 1, and 2 arcsec, respectively.

Out of the 72 sources of Table 9, 49, 17, and 35 have (possible) indications of binarity from photo-astrometry, a visual companion, and flux excess, respectively, and nine have no apparent indication of binarity. The later could still have for example tight companions of similar magnitudes and colours or substellar companions of LTY spectral types.

In the whole *Gaia* DR3 and compared to EDR3, many sources have additional measurements or parameters, for example related to binarity (Gaia Collaboration et al. 2022). None of the sources of Table 7 and 8 is flagged as non-single source, probably because these are fainter than the limits of  $G = 19 - 20$  mag for binarity analysis in DR3. One source has available epoch photometry and is significantly variable. P1X1 is in the *Gaia* Andromeda Photometric Survey (pencil beam of 5.5 deg radius) and is located far away (more than 2 deg) from the spiral disk of the Andromeda Galaxy, as seen in the optical. The source has  $G$ -band variations of up to 1 mag within less than 40 days, in the 2014.9–2017.4 epoch range and considering measurements with `flux_over_error` > 7. Figure. 20 shows the time series, in units of Barycentric Julian Days (BJD),  $G_{BP}$ - and  $G_{RP}$  bands measurements of `flux_over_error` > 7 are too few and not shown.

If we combine these indications of binarity with the distances, we can infer physical projected binary separations. In Table 9, we list the  $d_{50}$  distances with lower- and upper errors. The one-sigma lower error was obtained by subtracting  $d_{50}$  by the lower distance  $d_l = d_{16}$ . The upper error  $d_u - d_{50}$  depends on the photo-astrometric binarity indicator (column Ast.). For unflagged sources, we adopted  $d_u = d_{84}$ . For flagged sources, we adopted  $d_u = \max(d_{84}, 1/(plx - err_{plx}f))$ , where  $f$  is a correction factor for the parallax uncertainty underestimation.  $f = 1.5$  for sources with `ruwe` > 1.4 (flags ‘R’ or ‘U’) or  $f = (1.5 - 1.2)/(1.4 - 1.04) * (\text{ruwe} - 1.04) + 1.2$  for sources with `ruwe` < 1.4 but `IPD_gha` ≥ 0.1 (flag ‘R?’;  $f > 1$  for `ruwe` > 0.8), allowing for a continuous transition to the `ruwe` > 1.4 case. The factors of 1.5 and 1.2 were adapted from the cases of binaries of  $G = 19 - 20$  mag and separations 0–2 arcsec shown in figs. 16 and 17 in El-Badry et al. (2021). For P18, we adopted the distance of its

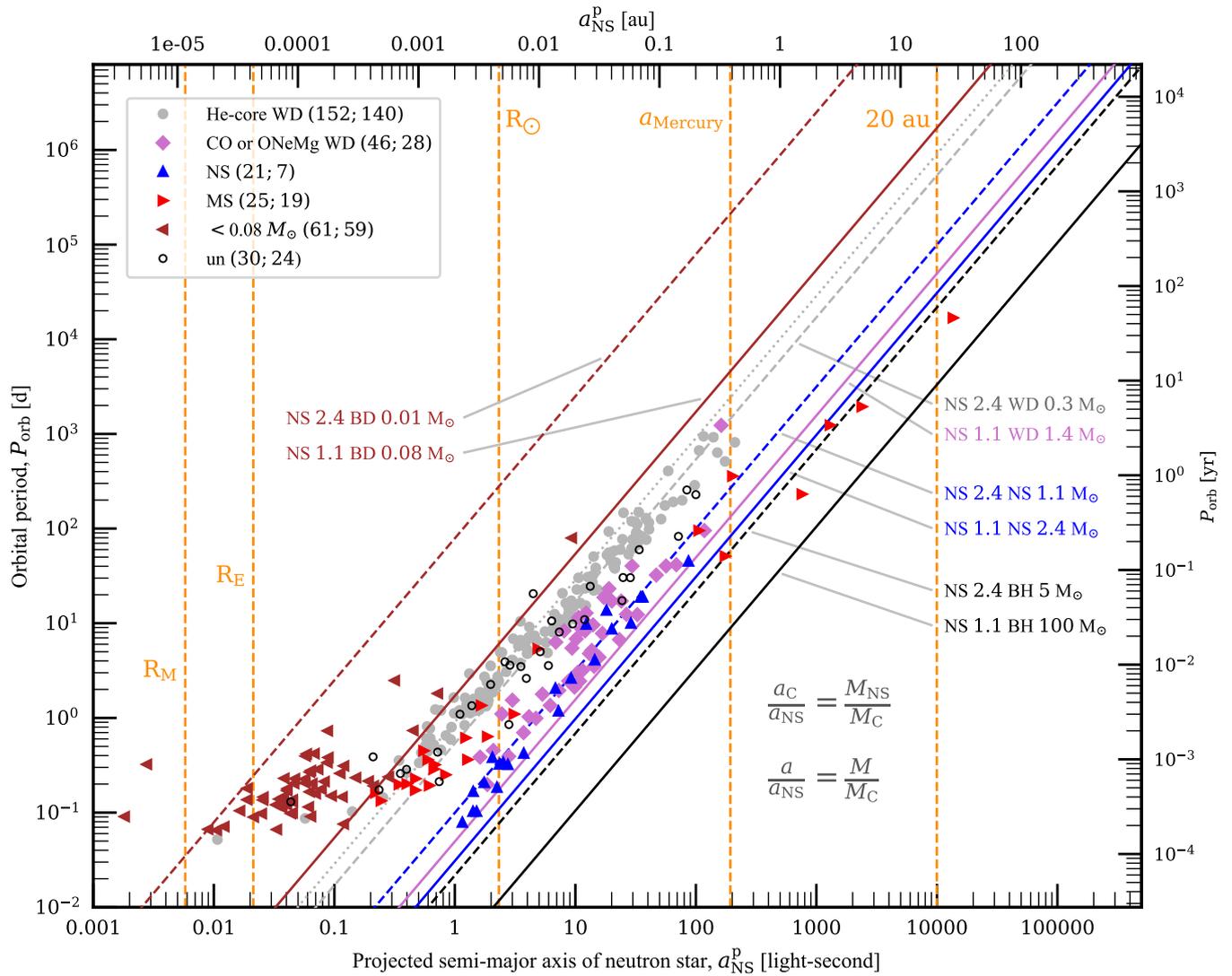
brighter and comoving stellar companion. For orientation, we list in Table 9 the physical projected binary separations (i)  $a_p^{d-}$  at the lower distance  $d_l$  and an angular separation of 0.05 arcsec, and (ii)  $a_p^{d+}$  at the upper distance  $d_u$  and an angular separation of (a) 0.3 arcsec, (b) the visual companion, and (c) the SED-excess counterpart.

Finally, we indicate possible types of the system components, components that are: the visible source exactly at the *Gaia* DR3 source position (V1), the visual companion (V2), and the SED excess- or photo-astrometric companion (S/A). For UV12, we assume a V1+V2 pair centred on the *Gaia* source position. In first approximation, we assume that all the V1 and V2 components are white dwarfs (WD; 0.1–1.3  $M_\odot$ ), except for (i) UV4 (V1; ultraviolet hot component), which at its current distance would have a too small radius to be a white dwarf (we thus indicate a question mark, ‘?’), (ii) UV7, P0, P3, P4, and P6 (V1; ‘?’), which have overall straight SED profiles, and (iii) the wide companion (V2) of P18, which probably is a main sequence star (MS) of 0.4  $M_\odot$ . Besides this, the *Gaia* sources of X2, Rad1, Rad\_a, UV13, UV14, UV15, P15, P27, and P36 are probable white dwarf candidates in GCNS or Gentile Fusillo et al. (2021). Also, in first approximation, we assume that all of the gamma-ray, X-ray, ultraviolet, or radio SED excesses are of unknown (companion) type (question mark ‘?’). Similarly, we assume that all of the photo-astrometric companions, independently of the visible companions, are of unknown type.

For guidance in the source classification, we derived radiuses from theoretical He- and H atmosphere white-dwarf fitting of the optical fluxes (Section 3.7) and blackbody fitting of the optical–ultraviolet fluxes. From the white-dwarf fitting, we have the theoretical white-dwarf mass and surface gravity ( $\log g$  where  $g$  is by default in  $\text{cm}^3/\text{g/s}$  units), which with the surface gravity equation  $g = GM/R^2$  provides us the white-dwarf radius. From the blackbody fitting (equations (10) and (11)), we have (i) the bolometric blackbody flux, which with the parallactic distance (Table 9) and equation (5) allows us to obtain the bolometric luminosity (in  $\text{erg s}^{-1}$ ), and we have (ii) the effective temperature, which with the bolometric luminosity and equation (2) provides us the thermal-emission radius. The derived radiuses are approximate because these depend on narrow spectral fitting regions (in most cases), opacity-related spectral redistributions of fluxes, distance, binarity, and reddening. The last one affects mostly sources towards the Galactic plane or centre. For simplicity, we account only for the uncertainty in the distance.

The extrapolations at the infrared (see the SEDs in Appendix G of the online supplementary material) of the blackbody- and theoretical white-dwarf fits typically match- or are lower than the observed fluxes, indicating unaccounted opacities and infrared fluxes in the fitting procedure. Despite the mismatches, most *Gaia* (V1) components appear to have radiuses in the white dwarf range of 0.005–0.025  $R_\odot$  at the adopted distances. White dwarf radiuses from model-independent mass- and radius measurements are in the range of 0.01–0.03  $R_\odot$  (fig. 9 in Parsons et al. 2017). Therefore, we preliminarily classified these components as white dwarfs.

The smallest known white dwarf is ZTF J190132.9+145808.7 (Gaia DR3 4506869128279648512), with an estimated radius of  $2140_{-230}^{+160}$  km (0.0031  $R_\odot$ ), an effective temperature of  $\sim 50\,000$  K, and a mass of 1.3  $M_\odot$  (Caiazzo et al. 2021). It is only slightly larger than the Moon, of 1737.5 km radius. In this context, the above 0.005–0.025  $R_\odot$  range corresponds to two to ten times the radius of the Moon. From the blackbody fitting at optical, we identified five V1 sources with very small radiuses at their  $d_{50}$  distances. These are P0, P1X1, UV10, P2, and Rad\_b, with  $R = 0.0012, 0.0016, 0.0020, 0.0025,$  and  $0.0031 R_\odot$ . The confirmation of these radius estimates would require the verification of the source type, distance, extinction,

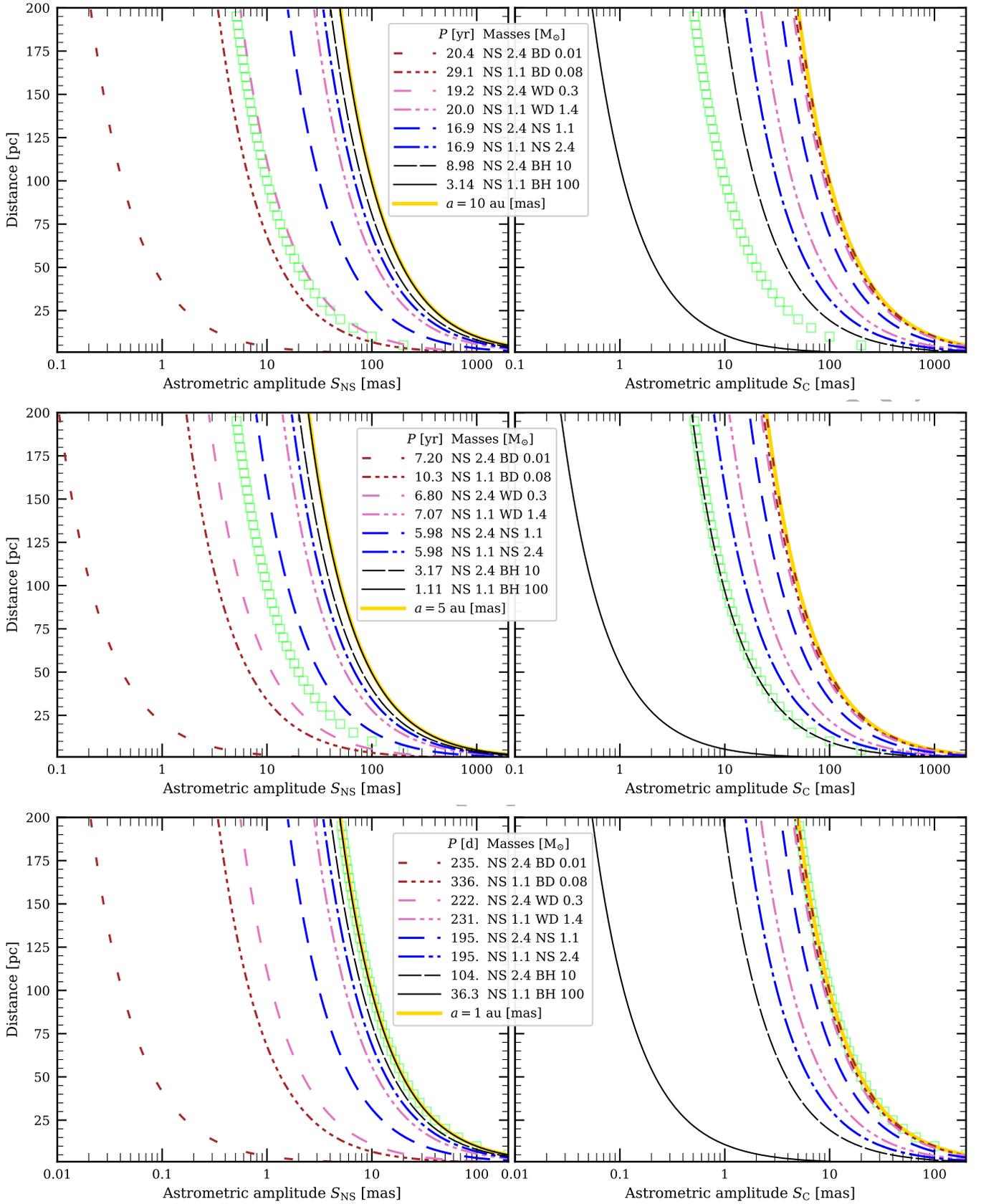


**Figure 21.** Orbital period versus projected semi-major axis of neutron stars with companions of different types. Parameter regions for low- and high mass-ratio NS–BD (brown), NS–WD (grey or pink), NS–NS (blue), and NS–BH (black) binaries are delimited by the dashed and solid lines, where BD, WD, NS, and BH stand for brown dwarf-, white dwarf-, neutron star-, and black-hole mass objects, respectively (see also fig. 5 in Singh et al. 2019). These lines are for an inclination of 90 deg and thus indicate the full semi-major axis. The grey dotted line, as compared to the grey dashed line, is for an inclination of 45 deg and indicates a projected semi-major axis smaller by a factor 0.71. ATNF pulsars in binaries are shown with a colour according to the type or candidate-type of their companion: low-mass He-core white dwarf (grey dots), CO- or ONeMg-core white dwarf (violet diamonds), neutron star (blue upward triangles), main sequence star (red rightward triangles), substellar-mass object (brown leftward triangles), or unspecified (black open circles). The respective numbers and millisecond-pulsar (spin  $\leq 30$  ms) subsets are indicated in parenthesis. The PSR J0737–3039AB binary pulsar is counted once but both components are represented in the plot. For comparison, the semi-major axis of Mercury and the radii of the Sun, Earth, and Moon are represented by the vertical dashed lines. Semi-major axis – mass relations are indicated, where  $a = a_{\text{NS}} + a_{\text{C}}$  and  $M = M_{\text{NS}} + M_{\text{C}}$  are the binary separation and total mass.

reddening, and binarity. Nevertheless, we can anticipate the effects, for example, of extinction and reddening. Assuming a low extinction of  $< 0.2$  mag over the *griz*-band range, then the unabsorbed flux is greater by a factor  $< 10^{0.4(0.2)} = 1.2$ , and the corrected radius is greater by a factor of only  $< 1.2^{0.5} = 1.1$  ( $R \propto F^{0.5}$ , from equations (2) and (5)). Assuming a reddening that causes underestimating the effective temperature by 750 K, then the corrected radius is smaller by a factor  $(T_{\text{eff}}/(T_{\text{eff}} + 750))^2$ , for example of 0.8–0.9 for  $T_{\text{eff}} = 7000 - 13000$  K ( $R \propto T_{\text{eff}}^{-2}$ , from equation (2)).

From the blackbody fitting at optical–ultraviolet, we derived emitting radii for UV1, UV3, UV4, and UV10 (Fig. 10), which have *NUV*- and *FUV*-band fluxes, and for UV7, UV8, and UV9 (Fig. 18), which have *NUV*-band fluxes and are already discussed in Sec-

tion 4.2.1. We indicate radius ranges accounting for distance uncertainties in the plots of the SEDs. For UV1, assuming that its optical and ultraviolet emission stems from a single blackbody source (which may not necessarily be true and the fit is approximate), the radius is of 891–1218 km. For the ultraviolet components of UV3 and UV4, the radii are of about 410–620 km (though in the case of UV4, the computation is purely formal, because the ultraviolet source is extended). For UV10, assuming that the ultraviolet emission stems only from a second component, the corresponding radius is of 95–140 km. In the cases of UV7, UV8, and UV9, the radii are of 1247–1578, 457–665, and 846–1218 km. The remaining eight ultraviolet candidates have too few near-ultraviolet measurements and do not allow us to determine whether these could have an ultraviolet



**Figure 22.** Astrometric orbital amplitude of a neutron star (*left*) and its companion (*right*), as a function of distance. Amplitudes for low- and high mass-ratio NS–BD (brown), NS–WD (pink), NS–NS (blue), and NS–BH (black) binaries are represented by the dashed lines, and, the dash-triple-dot-, dash-double-dot-, dash-single-dot-, and solid lines, respectively. From top to bottom, the physical binary separations are of 10, 5, and 1 au, and are represented as angular separations (yellow solid lines). The orbital period  $P$  for each case of binary component masses is indicated. Parallaxes ( $\pi = 1/d$ ) are shown by green squares.

blackbody component. From the perspective of our search, we tentatively interpret or propose that some of these ultraviolet excesses, of thermal or non-thermal origin, could relate to neutron stars, either from regions extending from these or from interaction processes with the system components. We recall that for instance for radio pulsars, because of the multi-path propagation of their radio emission, these have emitting regions that can be much larger than the neutron star radius and from a few tens of km to several  $10^4$  km, comparable to the light-cylinder radius, which is proportional to the pulsar period (Main et al. 2021).

As shown in the orbital-period versus projected-semi-major-axis diagram of Fig. 21, ATNF pulsars have detected companions typically of short orbital periods ( $\lesssim 10^3$  d), low- or lower masses, and mostly white-dwarf type. The two first aspects correlate with these pulsars having small projected semi-major axes. Besides the low-mass He-core- and higher-mass CO/ONeMg-core white dwarfs, there are ultra light- ( $< 0.08 M_{\odot}$ ), main-sequence-, and neutron-star companions. The numbers of each types of companions and their millisecond-pulsar subsets are indicated in parenthesis next to the abbreviated labels in the legend box. We note the significant amount of millisecond pulsars. These have spin periods shorter than 30 ms and could emit continuous gravitational waves at frequencies detectable by ground-based detectors. Small (initial) binary separations are required for mass transfer, accretion, and thereby the spinning-up of neutron stars to rotation periods of milliseconds (Alpar et al. 1982; Radhakrishnan & Srinivasan 1982; Bhattacharya & van den Heuvel 1991; Lorimer 2008). None of the ATNF millisecond pulsars has a measured projected semi-major axis larger than 200 lt-s (about the semi-major axis of Mercury), implying that in the case of white dwarf companions the projected binary separation would not be larger than about ten times this value ( $\lesssim 4$  au). However, subsequent mass loss of companions could increase the binary separation, and besides this, companions at relatively wide separations of the ATNF pulsars may not be easily detectable- nor systematically searched for with the pulsar-timing method.

Assuming that there are white dwarf – neutron star systems among our sources, any real, curvilinear orbital motion captured by *Gaia* DR3 data would concern those systems with significantly small angular separations. *Gaia* is most sensitive to orbital periods close to its observing period, as shown in the study about hidden (substellar) companions by Andrews et al. (2019). For white dwarf – neutron star systems ( $0.9+1.5 M_{\odot}$ ) of orbital periods of once and twice the *Gaia* DR3 observing period (2.83 yr), the binary separations are of  $a = 2.68$  and  $4.26$  au. For the sources of Table 9, the lower- and upper projected binary-separations are of  $a_p^{d-} = 2.1 - 8.3$  and  $a_p^{d+} = 2.5 - 8.5$  au at  $0.05$  arcsec angular separation ( $a_p^{d+} = 15 - 51$  au at  $0.3$  arcsec), implying that  $0.05$  arcsec is the level of angular separation at which these can be probed. From its own or complemented with other astrometric data, *Gaia* can also enable for detecting accelerations at larger separations, where the direction of acceleration may coincide with the relative location of a companion (Bowler et al. 2019; Brandt et al. 2021; Bonavita et al. 2022).

Because the visual companions of our sources are at very large projected separations ( $> 0.3$  arcsec) of a few  $10^1$  au, too large to cause any significant binary interaction with the main visual component and excess emission, these do not hinder the existence of neutron stars in the systems. On the other hand, photo-astrometric companions (R, R?, or U flags) with small projected separations of  $\lesssim 5$  au ( $\lesssim 0.05$  arcsec) could cause noticeable binary interaction on short time scales and excess emission.

In Fig. 22, we show the astrometric orbital amplitudes of a neutron star (left panel) and its companion (right panel) as a function of the

distance, for physical binary separations of 10, 5, and 1 au. For a circular orbit, the astrometric orbital amplitude is the angular semi-major axis

$$S_{\text{vis}}[\text{mas}] = \frac{1000}{d} a_{\text{vis}} = \frac{M_c}{M_{\text{vis}} + M_c} \frac{1000}{d} a, \quad (12)$$

where  $M_{\text{vis}}$  and  $M_c$  are the masses of the visible- and companion objects,  $d[\text{pc}]$  is the distance, and  $a[\text{au}] = a_{\text{vis}} + a_c$  the binary separation and sum of the component semi-major axes. The amplitude is obtained by subtracting the proper- and parallactic motion components from the time-varying astrometry of the photocentre. The figures show the astrometric signature of each component separately; in reality both components may be visible and cause a blend photocentre or only one component may be visible.

The amplitudes for low- and high mass-ratio NS–BD (brown), NS–WD (pink), NS–NS (blue), and NS–BH (black) binaries are represented by the dashed lines, and, the dash-triple-dot-, dash-double-dot-, dash-single-dot-, and solid lines, respectively, where NS, WD, BD, and BH stand for neutron star-, white dwarf-, brown dwarf-, and black-hole mass objects, respectively (the same binaries are also represented in Fig. 21). The physical binary separation is represented as angular separation by the yellow solid line. The orbital period  $P$  is indicated for each case of binary component masses. In arithmetic average, the astrometric amplitude is covered in  $P/4$ . For comparison, we show parallaxes ( $d = 1/\pi$ ) by the green squares. Per definition, the parallax is covered in  $1/4$  yr  $\approx 90$  d. In this context, we note that most sources of Table 9 have  $pm/plx$  ratios close to or lesser than one, that is their parallactic motion (uncertainty) appears to be a significant cause of the astrometric motion; exceptions with relatively large proper motions ( $pm/plx > 3$ ) are X2, UV13, UV14, UV15, Rad1, Rad\_a, P15, P18, and P30. From the right panels of Fig. 22, we see that for physical binary separations of 1–5 au, neutron stars orbiting white dwarfs can induce in white dwarfs significant astrometric jitter or modulation when compared to the parallactic motion. Quantitatively, from 1 to 5 au, it is of 44–89 to 220–444 per cent, on time-scales of 0.15–0.16 to 1.70–1.77 yr. This would thus concern potential binaries with angular separations  $\lesssim 0.05$  arcsec in Table 9. Finally and trivially, for a 0.1 au binary separation (not shown), orbital astrometric jitters induced in every of the above binary components are always smaller than 10 per cent of the parallax. Considering the inclination ( $i$ ), the angle between the line of sight and the normal vector to the orbital plane, for inclinations of 90 and 0 deg, the astrometric displacements are a segment and a circle on the sky, respectively ( $\cos(i) = b_{\text{vis}}/S_{\text{vis}}$ , where  $b_{\text{vis}}$  is the semi-minor axis of the visible object). For an inclination of 0 deg, it produces the largest binary wobble area in the sky, but no Doppler shifts in radial velocity. However, independent of inclination, an astrometric wobble for these binaries will always be measured, and in general, binaries have inclinations distributed uniformly.

Regarding the minimal separations of the binary candidates, we can assume that these could be of 0.1 au or less. In the catalogue of low-mass X-ray binaries (LMXB) in the Galaxy and the Large- and Small Magellanic Clouds (Liu et al. 2007), the least intense LMXB sources are the transient ultra-soft X-ray sources. These have orbital periods of a few hours to about 150 h, which are shorter than for a white dwarf – neutron star binary of  $1.0+1.5 M_{\odot}$  and 0.1 au separation, of  $P = 175.3$  h = 7.30 d. Too close separations would imply intense accretion and intense X-ray emission, which is apparently not the case for our sources. At less close separations and up to possibly 5 au, weak interactions between the stellar components (including orbital material) through irradiation, particle winds, magnetic fields, and gravitation could occur, and possibly cause X-ray, radio-, or ul-

traviolet excesses. Discoveries of tight white dwarf – neutron star binaries or double white dwarfs at separations  $<1\text{--}4$  au are important for gravitational wave searches (see e.g. Korol et al. 2022). In particular, the tightest binaries can be detected at 0.1–10 mHz with the Laser Interferometer Space Antenna (LISA; Amaro-Seoane et al. 2017).

We keep for a future work a more detailed characterization of the sources. This will benefit from updated parameters provided by the next *Gaia* Data Releases, in particular distance- and binary parameters. For some of the sources, it would be interesting to confirm whether these have power-law emission (at  $10^0\text{--}10^1$   $\mu\text{Jy}$  flux level), and whether it is pulsed and relates to pulsars and neutron stars. In the affirmative case, it would be interesting to determine how their ultraviolet–optical emission relates to radio emission, the magnetic field, and spindown emission flux (see e.g. Strader et al. 2016). Some of the sources with near- and mid-infrared excesses could be investigated in relation to the possible existence of an extended pulsar wind nebula or a resolved supernova fallback disc (as considered for the RX J0806.44123 neutron star, Posselt et al. 2018) or discs of other types, which could be detected and resolved more easily because the sources have nearer distances. Because neutron stars have very high gravitational fields and are almost point-like with just 20–30 km in size, these can enable high fly-by velocities and potentially ‘heat up’ orbital material shared with their stellar companions. Other indirect observational signatures of neutron stars, in particular through beam sweeping on orbital material (Mottez et al. 2020), could occur.

## 5 CONCLUSIONS

These results are from a search for neutron stars among *Gaia* broad-optical sources, based on magnitudes and colours derived from observations of known neutron stars and scaled to distances of the solar neighbourhood. Because nearby neutron stars are expected to be very old and practically invisible electromagnetically, these would only reveal themselves again, either as recycled pulsars or through interactions with companion stars and circumstellar material. In both cases, it is their – past or present – interactions with companions that would render these visible electromagnetically again.

Neutron stars with stellar companions can be divided into three categories: non interacting, weakly interacting, and intensively interacting. The intensively interacting neutron stars have already been identified among the accreting low-mass X-ray binaries, and are few ( $\sim 200$ ) and relatively distant ( $\sim \text{kpc}$ s; Liu et al. 2007). Thus, the nearest neutron stars, which amount to 1000–2000 within 100 pc, should be weakly interacting or non interacting, isolated. The ones that can be found electromagnetically are probably those that were recycled in the past by a companion and are now (millisecond) pulsars and those that are presently weakly interacting with stellar companions and orbital material, through irradiation, particle winds, magnetic fields, and gravitation.

Because the sources are searched in a photometric region of faint and blue sources that is in common with white dwarfs, visible companions are likely to be white dwarfs. This is also in confluence with most known pulsars in binaries having white dwarf companions. The present, *Gaia* DR3 measurements of the faint sources are single-star solutions and do not permit us to infer the masses of the components and the orbital elements yet. However, these measurements can give indications of binarity. With the complement of ultraviolet, optical, infrared fluxes, we do identify sources with two-component profiles (such as UV3, UV4, UV7, UV8, and UV10), involving power-law or thermal emissions, with small thermal radiuses.

Further work is required to determine whether these sources relate indeed to neutron stars. In particular, the confirmation of the source types, multiplicity, and component masses, searches of changes in electromagnetic fluxes and properties over time, and the elucidation of the astrophysical processes involved are required. Pulses or modulations of periods shorter than a few seconds could hint at neutron stars.

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## APPENDIX A: FURTHER DETAILS ON THE $M_G > 16$ SAMPLE, THE COLOUR-SELECTED SUBSAMPLE, AND PROBABLE WHITE-DWARF PHOTOMETRIC CANDIDATES

For the 75 073 sources in the  $M_G > 16$  sample, the relative flux uncertainties ( $1/\text{snr}_{\text{flux}}$ ) at  $G$  band are lesser than 10 per cent, and for most of the 58 135 and 58 656 sources with  $G_{BP}$  and  $G_{RP}$  photometry, the uncertainties are lesser than 30 and 20 per cent, that is 0.3 and 0.2 mag (magnitude uncertainty  $\approx 2.5 \log(1 \pm 1/\text{snr}_{\text{flux}})$ ). These uncertainties reflect the minimum numbers of observations for the bandpasses required for the *Gaia* (E)DR3 catalogue:  $\text{phot\_g\_n\_obs} \geq 10$ ,  $\text{phot\_bp\_n\_obs} \geq 2$ , and  $\text{phot\_rp\_n\_obs} \geq 2$ , for  $G$ ,  $G_{BP}$ , and  $G_{RP}$ , respectively. The maximum apparent magnitudes at  $G_{BP}$ ,  $G$ , and  $G_{RP}$  in the sample are 24.5, 21.4, and 22.3 mag (sources without parallax in the whole *Gaia* catalogue can have values as high as 25.3, 23.0, and 24.7 mag), whereas the mean apparent magnitudes are of 21, 20.5, and 19 mag, respectively. The maximum absolute magnitudes are of 23.3, 21.7, and 20.0 mag using either the inverse parallax or the  $d50$  distance. The implied intrinsic limits are shown by the lower grey dotted lines in Fig. 3. The absolute magnitude difference between the former and latter distance methods is always smaller than +0.8 mag (distance factor lesser than 1.5), with zero difference at  $\text{snr}_\pi > 10$ , and an increasing difference towards  $M_G = 16$  mag for  $\text{snr}_\pi < 5 - 10$ . For our search, these differences are not significant.

In the colour-selected subsample, two sources have very blue  $G_{BP} - G$  colours of  $-2.7$  mag and are not shown in Fig. 3. These also have the highest value of 8 in the subsample, of the corrected colour-excess factor ( $\text{phot\_bp\_rp\_excess\_factor\_corrected}$ ). The factor is defined as the sum of the  $G_{BP}$ - and  $G_{RP}$ -band fluxes divided by the  $G$ -band flux, corrected by a colour function. For an isolated stellar point source it is expected to be close to zero, with positive values when the source has more flux at  $G_{BP}$  and  $G_{RP}$  bands than at  $G$  band and vice versa for negative values (Riello et al. 2021). The  $G$ -band flux is obtained from profile fitting in a relatively small field, of  $0.35 \times 2.1$  arcsec<sup>2</sup> for faint sources, and the  $G_{BP}$ - and  $G_{RP}$  band fluxes are sums in an aperture of  $3.5 \times 2.1$  arcsec<sup>2</sup>, thus any high excess factor would indicate contamination from a nearby source. Gaia DR3 4661504581157717120 ( $G = 20.7$ ,  $G - G_{RP} = 0.5$  mag) is in a dense field of the Large Magellanic Cloud, clearly visible as a relatively blue source in *ugriz*-band stack images queried at the NOIRLab Astro Data Lab<sup>10</sup>. It blends with a star 2.2 arcsec south and of  $G = 18.6$  mag. It corresponds to NSC DR2 189095\_13039 with  $u - g = 21.235 - 21.219 = 0.02$  mag (only *ug*-band photometry are available) and the blending, redder star is NSC DR2 189095\_10634, with  $u - g = 20.643 - 18.854 = 1.79$ ,  $g - r = 0.49$ ,  $r - i = 0.26$ , and  $i - z = 0.10$  mag. Gaia DR3 5853004242120032256 ( $G = 21.0$ ,  $G - G_{RP} = 0.8$  mag) is in the Galactic plane, at  $(l, b) = (313.17, -3.70)^\circ$ . It is clearly visible in images of the DECam Plane Survey (DECaPS) DR1 (Schlafly et al. 2018), where it appears redder than its nearest and red *Gaia* neighbour at 2.4 arcsec. In fact, it consists of a 0.65 arcsec separation blend of the *iz*-band DECaPS 1028228089938032219 ( $i = 21.2$  mag) and *grizY*-band DECaPS 1028228089934061633 ( $i = 20.3$  mag), which have red colours. Thus the unusually blue  $G_{BP} - G$  colours of the

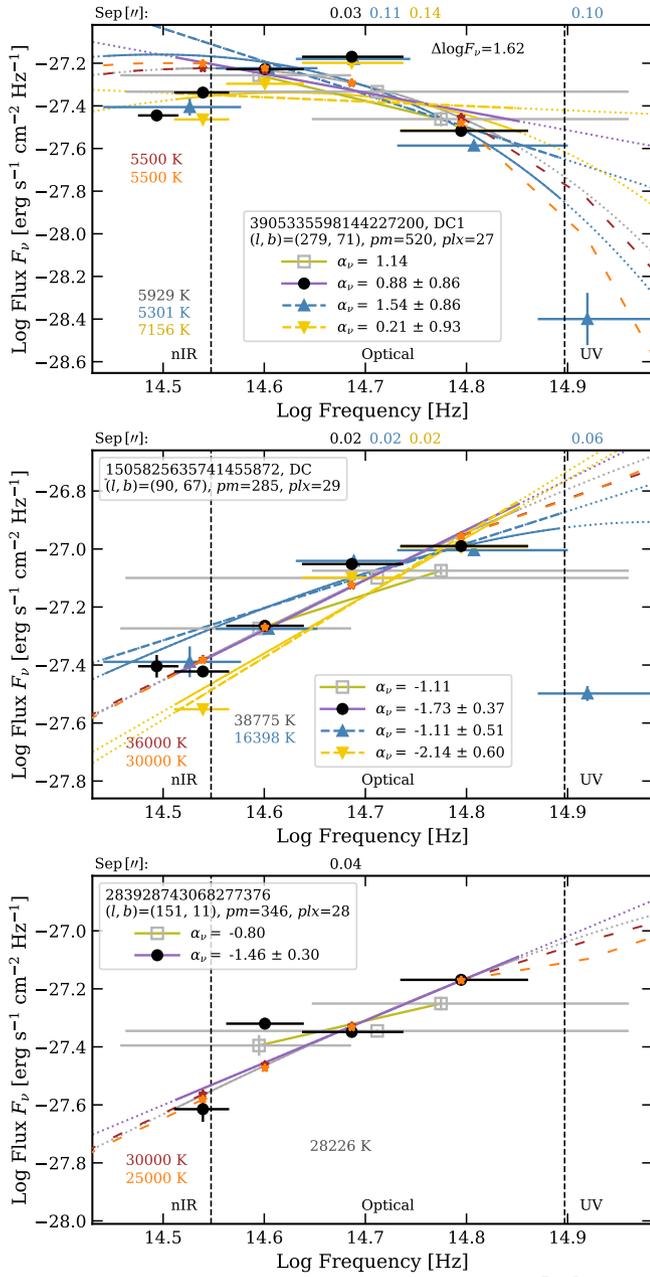
two *Gaia* sources and their very high colour-excess factors are probably caused by the blends within arcseconds. The remaining of the 2464 sources have corrected colour-excess factors in the range  $-0.6$  to 1.6 and peaking at 0.1. There is also a flux bias towards greater values (overestimating the flux) at low fluxes close to the minimum thresholding in *Gaia* DR3 and it affects mostly the  $G_{BP}$  band for red sources (Riello et al. 2021; Fabricius et al. 2021). The flux bias is negligible for input  $G_{BP}$ - and  $G_{RP}$ -band magnitudes that are less faint than about 20.5 and 20.0 mag (Fabricius et al. 2021). This bias implies that in our colour selection of faint sources we may have taken in sources that are in fact redder than their colour values in the catalogue, as for example RC1–RC5 (Appendix D).

Regarding known probable white-dwarf photometric candidates among the sources of the colour-selected subsample, there are (i) 113 with  $P_{WD} > 0.5$  in GCNS, and (ii) 72 with  $P_{WD} \leq 0.5$  in GCNS but  $P_{WD} > 0.5$  in Gentile Fusillo et al. (2021, 71 sources) or Gentile Fusillo et al. (2019, Gaia DR3 1781440902671450880). Also, there are 35 in the 100 pc white-dwarf candidate sample of Torres et al. (2019), of which two are not in the previous three references and 33 are with  $P_{WD} > 0.5$  in GCNS. GCNS- and not-GCNS probable white-dwarf photometric candidates are represented by yellow- and orange small squares in Fig. 3, and have  $M_G < 17.7$  mag. Three of the former are identified as resolved multiple systems in GCNS. These are bound wide binaries and indicated by red circles. Gaia DR3 1570574230528214400 ( $M_G = 16.0$ ,  $G_{BP} - G = 0.7$  mag) is part of a double white dwarf binary of separation of 128 au, with Gaia DR3 1570574260593313152 ( $M_G = 15.5$ ) as the brighter component; it was previously identified as an unresolved large proper-motion star in the catalogue of Lépine & Shara (2005). Gaia DR3 4476576831314323456 ( $M_G = 16.0$ ,  $G_{BP} - G = 0.5$  mag) is part of a double white dwarf binary of separation of 824 au, with Gaia DR3 4476576831311990144 ( $M_G = 15.5$ ) as the brighter component; both components were previously identified individually as white dwarf photometric candidates in the catalogue of Gentile Fusillo et al. (2019). Gaia DR3 6178573689547383168 ( $M_G = 16.5$ ,  $G_{BP} - G = -0.1$  mag) is part of a white-dwarf–main-sequence binary of separation of 2754 au, with Gaia DR3 6178573792627114496 ( $M_G = 7.7$ , photometric spectral type  $\sim$  K6V) as the brighter component; the components were previously identified as a wide binary in the catalogue of Hartman & Lépine (2020). In total there are 143 sources with  $P_{WD} > 0.5$  in Gentile Fusillo et al. (2021): these have  $A_V$  mean extinctions of 0.01–0.09 mag,  $d50$  distances of 32–104 pc,  $P_{WD}$  of 0.91–1.00,  $\text{snr}_\pi$  of 3.4–166,  $M_G$  of 16.0–17.6 mag, numbers of *Gaia* DR3 sources in their respective constant-area surrounding fields of 30–11355 (DENSITY parameter), H-atmosphere  $T_{\text{eff}}$  of 3734–6958 K (78 sources), He-atmosphere  $T_{\text{eff}}$  of 3956–7785 K (84 sources), and proper motions of 1.8–2354 mas yr<sup>-1</sup>.

## APPENDIX B: SEDS OF THREE NEARBY WHITE-DWARF SOURCES

The SEDs of three large proper-motion (285–520 mas yr<sup>-1</sup>), nearby ( $d50 \approx 36$  pc) white-dwarf sources are shown in Fig. B1. Gaia DR3 3905335598144227200 (SDSS J122048.65+091412.1; ‘DC1’) is an example of DC white dwarf. Its SED diverges from that of a blackbody and from those of theoretical white dwarf pure H and He atmospheres. The flux suppression at *iz* bands, producing bluer colours relative to the *r* band (e.g.  $r - i$  and  $r - z$ ), is caused by H<sub>2</sub> pressure-induced absorption; this absorption is greater in white dwarf H atmospheres that are cooler or richer in helium. The DC

<sup>10</sup> <https://datalab.noirlab.edu>



**Figure B1.** SEDs of three white-dwarf sources with *griz*-band flux profiles that are: (*top panel*) very curved (‘DC1’), (*middle panel*) curved-up (large  $\alpha_v$  errors), peaking at *gr* bands, and with significantly suppressed *u*-band flux (Gaia DR3 1505825635741455872), (*bottom panel*) straight-up with an apparent *i*-band flux excess (Gaia DR3 283928743068277376). Same as in Fig. 10.

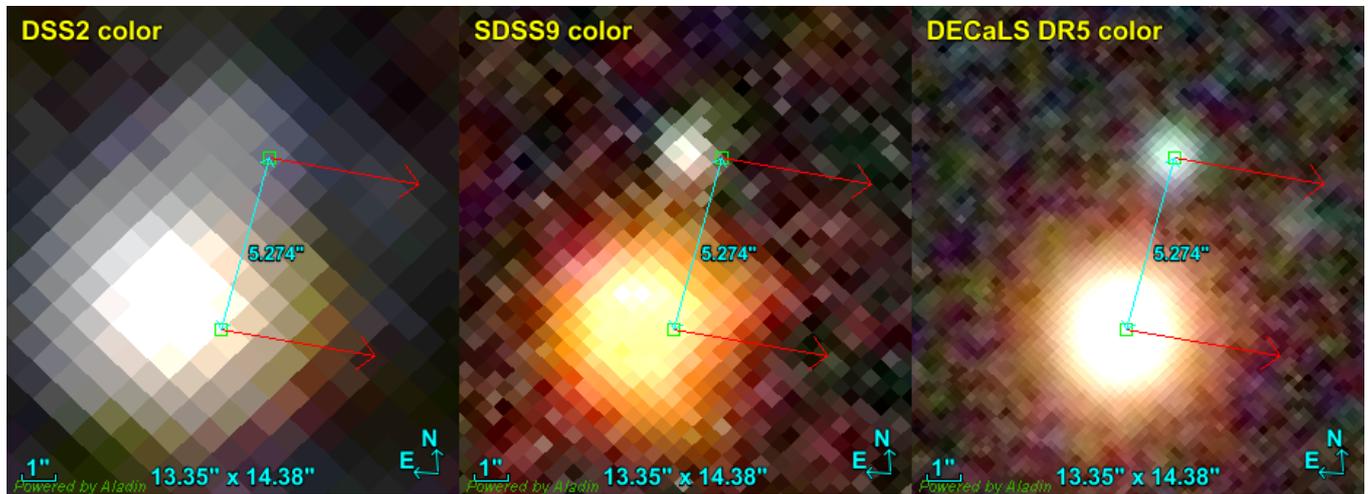
white dwarf has a mixed atmosphere of  $N(\text{H})/N(\text{He}) = 10^{-1.22}$  and  $T_{\text{eff}} = 3531 \pm 37$  K (Gates et al. 2004; Leggett et al. 2018). Gaia DR3 1505825635741455872 (SDSS J140324.67+453332.7) is a DC white dwarf with a *griz*-band flux profile that is blue, curved (large  $\alpha_v$  errors), peaking at *gr* bands, and with significantly suppressed *u*-band flux.

Gaia DR3 283928743068277376 is a probable white dwarf candidate based on *Gaia* photometry and astrometry (Gentile Fusillo et al. 2019, 2021; GCNS). It is spectroscopically unconfirmed and noted as having blue and peculiar *Gaia* and PS1 colours (McCleery et al. 2020). The SED in Figure B1 indicates that it is very hot ( $\sim 30\,000$  K)

**Table C1.** Astrometry of the proper motion stellar binary of P18.

Parameter	Component A	Component B
<i>Gaia</i> DR3	3948582104883237632	3948582104883968384
<i>pmRA</i> (mas yr <sup>-1</sup> )	-88.586±2.108	-90.558±0.044
<i>pmDEC</i> (mas yr <sup>-1</sup> )	-15.676±1.150	-15.720±0.035
Plx (mas)	(13.53±1.72)	5.882±0.041
RA ICRS (°)	187.59980167314257	187.60021864187
DEC ICRS (°)	18.886339386336545	18.88492845292
Epoch (yr)	2016.0	2016.0
<i>G</i> (mag)	20.781±0.014	15.694±0.003
<i>G<sub>BP</sub></i> (mag)	21.021±0.193	16.995±0.005
<i>G<sub>RP</sub></i> (mag)	19.873±0.153	14.565±0.004
$\rho$ (arcsec), PA (deg)	5.274, 164.4	
<i>a<sub>proj</sub></i> (au) at 168 pc	886	
NSC DR2		
RA J2000 (°)	187.599795417444	187.60020211637547
DEC J2000 (°)	18.8863284791447	18.884931674173455
Epoch (yr)	2016.5714	2016.7941
$\rho$ (arcsec), PA (deg)	5.216, 164.6	
PS1 DR1		
RA J2000 (°)	187.599828930	187.600258740
DEC J2000 (°)	18.886344310	18.884933650
Epoch (yr)	2011.5613	2011.8995
$\rho$ (arcsec), PA (deg)	5.285, 163.9	
SDSS DR 13		
RA ICRS (°)	187.600089120098	187.600512478144
DEC ICRS (°)	18.8863672307873	18.8849507640562
Epoch (yr)	2005.3562	2005.3562
$\rho$ (arcsec), PA (deg)	5.299, 164.2	
<i>Gaia</i> - SDSS		
<i>pmRA</i> (mas yr <sup>-1</sup> )	-92.0±1.6	-94.0±0.1
<i>pmDEC</i> (mas yr <sup>-1</sup> )	-9.4±1.9	-7.5±0.1
NSC - SDSS		
<i>pmRA</i> (mas yr <sup>-1</sup> )	-89.2±1.7	-92.4±0.3
<i>pmDEC</i> (mas yr <sup>-1</sup> )	-12.4±2.0	-6.0±0.6

and has a peculiar *i*-band flux excess. The later probably stems from contamination by the glare of the bright- and very small proper motion Gaia DR3 283928678644413824 star ( $G = 16.48$  mag,  $2.6$  mas yr<sup>-1</sup>). The glare contamination is strongest redwards and at the PS1 epoch, when the separation of the sources is of 3.37 arcsec. (At the later *Gaia* 2016.0 epoch, it is even closer, of 2.8 arcsec.) At an earlier epoch, in *ugriz*-band images at the border of the SDSS DR9 survey (where no catalogue photometry is available), the white dwarf source is farther at 5.4 arcsec and well isolated. Its SDSS *ri*-band counts compared to other sources with PS1 magnitudes indicate fluxes consistent with a relatively straight *griz*-band profile.



**Figure C1.** Sequence of DSS2- (1995–1996), SDSS- (2005), and DECaLS (2015–2017-epoch) colour images showing that P18 is comoving with the brighter and redder star, Gaia DR3 3948582104883968384. The small green squares indicate the *Gaia* DR3 positions at epoch 2016.0 and the red arrows indicate the proper motions, magnified to show their equality.

### APPENDIX C: A LARGE PROPER-MOTION-, ~900 AU-WIDE, WHITE-DWARF–M-TYPE-DWARF BINARY

Gaia DR3 3948582104883237632 (P18;  $\alpha_V = 1.6$ ) is located 5.3 arcsec north of a five magnitudes brighter star, Gaia DR3 3948582104883968384 ( $G = 15.69$  mag). The two objects share the same *Gaia* proper motion of  $(-89.6, -15.7)$  within  $2 \text{ mas yr}^{-1}$ . We corroborated this independently by measuring their *Gaia*–SDSS and NSC–SDSS proper motions, assuming the source nominal coordinates in the catalogues (Table C1). The agreement between the declination components of the proper motions is corroborated less well, possibly because the PSFs of these sources blend along the declination. The displacement over time of the stellar binary can be seen in the survey colour images of Fig. C1, from DSS2 (blue epoch 1995.2 and red epoch 1996.4) to SDSS DR9 (epoch 2005.4) to DECaLS DR5 (epoch 2015–2017), and relative to the *Gaia* DR3 2016.0 positions. Possibly because of the glare of the bright star, the candidate has slightly-larger-than-usual PS1 *griz*-band uncertainties (0.10, 0.08, 0.06, and 0.08 mag, respectively), its SDSS PSF magnitudes have unrealistic errors (we considered its SDSS model magnitudes instead), and its parallax (and  $d_{50} = 79$  pc) disagrees significantly with that of the bright star. The parallax of the later is more accurate and implies a distance of  $168 \pm 1$  pc (from the *Gaia* (E)DR3 distance catalogue of Bailer-Jones et al. 2021) and thereby a tangential velocity of  $v_t = 73$  km/s. At the larger distance, the  $G$ -band absolute magnitude of P18 becomes  $M_G = 20.78 + 5 \times \log(5.8817) - 10 = 14.63$  mag, which remains well below the stellar main sequence. The  $G_{BP} - G = 1.30$ ,  $G - G_{RP} = 1.13$ , and  $M_G = 9.54$  mag of the bright star indicate consistently an M2.5V spectral type, corresponding to an effective temperature of 3500 K and a mass of  $0.40 M_\odot$ , based on the MSC compilation. At 168 pc, the binary would have a projected physical separation of 886 au. The probability of chance alignment at this projected physical separation is likely to be less than 0.1 per cent, especially in this sparse stellar field well above the direction of the Galactic plane, and it is near the peak ( $\sim 1000$  au) of the distribution of separations of low-mass stellar wide binaries (El-Badry & Rix 2018; Gaia Collaboration et al. 2021b; El-Badry et al. 2021). Assuming a mass of  $0.40 M_\odot$  for each component, and multiplying

the physical separation by 1.26 to account statistically for inclination angle and eccentricity of binary orbits (Fischer & Marcy 1992), the binary would have an orbital period of  $4.2 \times 10^4$  yr.

### APPENDIX D: RED-COLOUR DWARFS

The five sources with the reddest PS1-, SDSS- and NSC *griz*-band slopes, independent of slope uncertainty, are Gaia DR3 900742499823605632 (RC1), Gaia DR3 4389594118549228416 (RC2), Gaia DR3 4780916942594976768 (RC3), and Gaia DR3 4906188219358053248 (RC5). Their parameters and photometry are listed in Tables 8, E3, and E4, and their SEDs are shown in Fig. G6 (available as online supplementary material).

In the  $M_G$  versus  $G - G_{RP}$  colour–absolute magnitude diagram of Fig. F2 (available as online supplementary material), these have colours close to 0.9 mag, as red as the DQpec white dwarf LHS 2229 (Gaia DR3 740483560857296768, flagged ‘DQpec’). DQ white dwarfs have atmospheres enriched in carbon, and the peculiar DQ LHS 2229 has very strong shifted  $C_2$  Swan bands in the blue optical (see Giammichele et al. 2012), affecting mostly the  $g$  band. Because of this, in the SED of LHS 2229 we fitted only the *riz* bands (Figs. 11, G3 and G6). However at the optical–infrared, the five sources are much redder than LHS 2229, as seen at the  $G - J$ ,  $i - z$  and  $i - J$  (Figs. F4, F5, and F6),  $r - i$  (Fig. F7),  $r - J$  (Figs. F16 and F17),  $z - J$  (Fig. F12), and  $i - W1$  colours (Fig. F15). In fact, their colours are those of early-M-type dwarfs. Considering the increasing number of sources towards the  $G - G_{RP}$  selection boundary (Fig. 3), similar red-colour sources could probably be found beyond the boundary, some of these merging with the ML-type dwarf sequence.

From least-square fitting with main-sequence dwarf photometry of the MSC compilation, we obtain the following spectral types: RC1 (M4V), RC2 (M4.5V), RC3 (M4.5V), RC4 (M5V), and RC5 (M5.5V). Because the sources are under the main sequence (3–4 mag under in the  $M_G$  versus  $i - z$  diagram of Fig. 19), these could be of low-metallicity and subdwarfs. However, the  $J - K$  versus  $i - J$  colours of RC3, RC4, and RC5 overlap with the main sequence, and do not suggest extreme- or ultra-subdwarf M types, which have less red  $J - K$  colours (fig. 1 in Zhang et al. 2017). Their  $J - K$  versus

**Table D1.** Red-colour dwarfs.

Flag	$Plx$ (mas)	$\mu_{\alpha^*}$ (mas yr <sup>-1</sup> )	$\mu_{\delta}$ (mag)	$G$ (mag)	$BP-G$ (mag)	$G-RP$ (mag)	$g-r$ (mag)	$r-i$ (mag)	$i-z$ (mag)	P	$z-J$ (mag)	$J-H$ (mag)	$J-K_s$ (mag)	$J-W1$ (mag)	$W1-W2$ (mag)
RC1	11.1±2.9	-4.5	-15.6	20.82	0.44±0.42	0.80±0.22	1.73	1.28	0.74	3	1.25	-	-	(1.18)	(0.18)
RC2	10.8±2.8	-9.0	-9.9	20.94	0.36±0.29	0.78±0.13	1.76	1.43	0.77	3	1.67	-	-	0.98	-0.13
RC3	11.1±2.6	29.2	-28.4	20.90	0.57±0.39	0.89±0.14	1.46	1.60	0.69	2	1.53	0.48	0.75	1.10	-0.44
RC4	14.6±3.0	-8.8	10.4	20.86	0.56±0.42	0.86±0.17	1.49	1.66	0.71	2	1.64	0.38	0.82	1.02	0.03
RC5	10.7±2.0	53.8	-19.0	20.88	0.48±0.42	0.88±0.14	1.65	2.15	0.88	2	1.64	-	0.71	0.92	0.01

Notes. Proper motion component errors are of 1.3–2.7 mas yr<sup>-1</sup>. The griz-band photometric (P) colours are from 2–NSC and 3–SDSS.

$J-W2$  and  $J-H$  versus  $z-J$  colours also overlap with the main sequence (fig. 18 in Zhang et al. 2018). Interestingly, the red-colour sources are located towards sparse stellar regions out of the direction of the Galactic plane (Section 4.1) and their *Gaia* photo-astrometric parameters do not appear to indicate binarity. However their  $snr_{\pi}$  are low, of 4–5, and their `visibility_periods_used` are of about 10, suggesting that their distances could be larger. We note that RC1 has a less coincidental mid-infrared counterpart, located 1.73 arcsec west, and has no  $HK_s$ -band measurements. Supposing that RC1 is in fact relatively faint in the mid- and near-infrared, then it could either be (i) an M-type subdwarf or (ii) a white dwarf cooler than 3250 K, such as the few ultra-cool white dwarfs known (McCleery et al. 2020). Finally, we note that RC3 and RC5 have large proper motions of 41–57 mas yr<sup>-1</sup>.

#### APPENDIX E: ADDITIONAL PHOTOMETRY

#### APPENDIX F: ADDITIONAL PHOTOMETRIC DIAGRAMS OF THE SOURCES (ONLINE SUPPLEMENTARY MATERIAL)

#### APPENDIX G: SPECTRAL FLUX DENSITY DISTRIBUTIONS INCLUDING INFRARED FLUXES OF THE SOURCES (ONLINE SUPPLEMENTARY MATERIAL)

ORIGINAL UNEDITED MANUSCRIPT

**Table E1.** PS1- and infrared photometry of the sources.

Flag	Sep ( $\prime\prime$ )	g PS1 (mag)	r PS1 (mag)	i PS1 (mag)	z PS1 (mag)	y PS1 (mag)	Sep ( $\prime\prime$ )	J (mag)	H (mag)	K <sub>s</sub> (mag)	P ( $\prime\prime$ )	W 1 (mag)	W 2 (mag)
$\gamma_a$	-	-	-	-	-	-	-	-	-	-	6	-	-
$\gamma_b^a$	-	-	-	-	-	-	0.12	17.971±0.219	17.319±0.230	17.112±0.260	6	-	-
$\gamma_c$	-	-	-	-	-	-	0.24	18.647±0.160	-	-	1	-	-
$\gamma_d$	0.14	21.445±0.065	20.323±0.064	19.710±0.021	19.396±0.005	19.501±0.061	0.37	17.818±0.064	-	17.031±0.112	1	-	-
$\gamma_e$	0.20	-	19.642±0.043	20.052±0.017	-	-	-	-	-	-	-	-	-
X2	-	-	-	-	-	-	0.17	19.338±0.184	19.259±0.289	-	1	-	-
X_a	-	-	-	-	-	-	0.30	18.735±0.070	-	18.165±0.208	1	-	-
X_b	0.05	21.044±0.073	20.318±0.023	19.995±0.114	-	19.727±0.147	0.22	18.293±0.072	-	17.646±0.162	1	-	-
X_c	0.05	20.855±0.032	20.192±0.032	19.935±0.450	19.568±0.136	19.780±0.087	0.29	18.777±0.181	-	-	1	-	-
X_d	0.02	21.209±0.021	20.509±0.024	20.132±0.026	19.991±0.022	19.927±0.081	0.03	18.782±0.111	-	-	2	0.37	18.306±0.151
X_e	-	-	-	-	-	-	0.24	19.035±0.095	-	18.375±0.304	1	-	-
UV1	-	-	-	-	-	-	-	-	-	-	-	-	-
UV2 <sup>b</sup>	0.05	20.031±0.021	19.767±0.012	19.660±0.009	19.639±0.023	19.534±0.024	0.17	18.688±0.089	-	-	1	-	-
UV3	-	-	-	-	-	-	0.26	18.533±0.072	-	17.634±0.159	1	0.84	17.440±0.068
UV4	0.05	20.127±0.018	20.262±0.017	19.926±0.020	19.702±0.019	19.293±0.032	0.51	18.137±0.078	-	17.466±0.156	1	-	-
UV5	-	-	-	-	-	-	-	-	-	-	-	-	-
UV6	0.07	20.060±0.020	19.727±0.016	19.620±0.008	19.572±0.031	19.497±0.057	-	-	-	-	-	-	-
UV7	-	-	-	-	-	-	0.17	18.951±0.050	-	17.646±0.087	1	0.19	16.020±0.026
UV8	0.06	21.570±0.056	21.099±0.033	20.216±0.033	19.701±0.026	19.481±0.056	0.17	18.275±0.065	-	-	2	0.76	17.465±0.082
UV9	0.03	21.575±0.040	21.174±0.091	20.505±0.020	19.959±0.029	19.576±0.052	-	-	-	-	0.42	-	17.544±0.288
UV10	0.06	20.895±0.035	20.974±0.025	21.204±0.068	21.163±0.056	-	-	-	-	-	-	-	17.613±0.229
UV11	0.07	21.242±0.020	20.736±0.025	20.539±0.016	20.369±0.038	20.283±0.089	0.27	19.276±0.161	-	-	2	-	-
UV12	0.07	20.751±0.076	20.419±0.011	20.247±0.026	20.169±0.042	19.811±0.142	-	-	-	-	-	-	-
UV13	0.59	21.141±0.028	20.155±0.016	19.912±0.013	19.775±0.018	19.477±0.040	0.19	18.345±0.045	17.983±0.059	17.948±0.117	1	0.75	17.818±0.097
UV14	0.52	21.364±0.051	20.471±0.026	20.083±0.014	19.952±0.033	19.858±0.066	0.05	18.954±0.116	-	-	2	-	17.811
UV15	0.49	21.338±0.033	20.610±0.017	20.520±0.017	20.282±0.038	19.822±0.136	0.19	19.251±0.170	-	-	2	1.00	17.915±0.113
Rad1	0.12	21.242±0.060	20.870±0.020	20.404±0.021	20.351±0.051	-	-	-	-	-	-	-	-
Rad_a	0.05	21.347±0.091	20.865±0.043	20.583±0.027	20.529±0.182	20.250±0.186	-	-	-	-	-	-	-
Rad_b <sup>c</sup>	-	-	-	-	-	-	0.17	19.565±0.073	-	19.461±0.122	-	-	-
Rad_c	0.03	20.591±0.043	19.949±0.046	19.569±0.038	19.588±0.076	19.550±0.028	0.39	18.469±0.161	-	-	1	-	-
Rad_d	0.02	21.950±0.135	20.797±0.050	20.150±0.016	19.746±0.016	19.452±0.046	0.10	18.261±0.058	-	17.500±0.130	1	-	-
Rad_e	0.03	21.967±0.172	20.858±0.069	20.479±0.085	19.928±0.052	19.510±0.065	-	-	-	-	-	-	-
Rad_f	0.23	21.798±0.153	20.922±0.056	20.401±0.077	20.161±0.092	19.706±0.044	0.36	18.320±0.046	17.782±0.056	17.451±0.074	3	-	-
Rad_g	0.03	21.934±0.161	21.057±0.064	20.727±0.065	20.571±0.178	19.953±0.172	0.09	19.075±0.164	-	-	1	-	-
P0	0.05	20.678±0.032	21.011±0.061	21.246±0.040	21.077±0.168	-	-	-	-	-	2.08	(17.156±0.059)	(17.057±0.172)
P1X1	0.22	20.223±0.018	20.458±0.019	20.663±0.028	20.682±0.071	20.676±0.012	-	-	-	-	-	-	-
P2	0.03	20.717±0.025	20.677±0.023	20.715±0.026	20.646±0.058	-	-	-	-	-	-	-	-
P3 <sup>d</sup>	0.01	20.908±0.067	20.621±0.098	20.659±0.019	20.633±0.035	-	0.08	19.387±0.095	18.922±0.152	18.201±0.199	4	0.41	17.394±0.070
P4 <sup>e</sup>	0.21	-	-	20.783±0.045	-	-	0.19	19.598±0.059	18.839±0.115	18.241±0.089	7	0.05	17.711±0.099
P5 <sup>f</sup>	0.02	21.020±0.029	20.838±0.047	20.660±0.029	20.613±0.058	19.631±0.160	0.21	20.081±0.262	-	-	4	-	-
P6 <sup>g</sup>	0.00	21.178±0.040	20.992±0.079	20.767±0.043	20.679±0.052	-	0.32	-	-	-	1	0.12	17.761±0.113
P7	0.05	20.569±0.017	20.267±0.033	20.062±0.035	19.994±0.043	20.002±0.093	0.12	19.089±0.181	-	-	1	-	17.215±0.224
P8	0.06	21.302±0.055	20.985±0.104	20.776±0.112	20.605±0.041	20.535±0.165	-	-	-	-	-	-	-
P9	0.38	20.057±0.021	19.701±0.073	19.488±0.018	19.389±0.026	19.492±0.057	0.42	18.422±0.090	-	17.785±0.174	1	-	-
P10 <sup>h</sup>	0.03	21.260±0.026	20.910±0.055	20.675±0.033	20.462±0.100	20.091±0.067	0.10	19.882±0.226	-	-	1	-	-
P11	0.04	21.267±0.036	20.909±0.012	20.640±0.022	20.464±0.006	20.296±0.117	-	-	-	-	-	-	-
P12	0.17	20.892±0.083	20.566±0.016	20.298±0.022	20.091±0.063	20.004±0.072	0.28	19.117±0.126	-	-	2	-	-
P13	0.01	21.400±0.032	21.017±0.076	20.737±0.030	20.486±0.072	20.744±0.175	0.06	19.884±0.228	-	-	2	-	-
P14	0.14	20.933±0.010	20.531±0.027	20.203±0.040	20.114±0.054	-	0.39	18.962±0.130	-	-	1	-	-
P15 <sup>i</sup>	0.03	21.336±0.003	20.866±0.024	20.604±0.020	20.409±0.035	20.035±0.185	0.11	19.588±0.135	19.324±0.215	-	4	-	-
P16	0.10	20.912±0.028	20.461±0.026	20.177±0.013	19.944±0.022	19.700±0.075	0.15	18.956±0.132	-	17.887±0.209	1	-	-
P17	0.01	20.497±0.022	19.979±0.030	19.701±0.019	19.496±0.010	19.666±0.043	0.07	18.457±0.079	-	17.985±0.213	1	1.75	(17.032±0.056)
P18	0.30	21.203±0.098	20.778±0.077	20.418±0.060	20.197±0.081	-	0.44	19.511±0.191	-	-	2	-	(16.835±0.128)
P19	0.51	21.011±0.030	20.534±0.027	20.241±0.037	19.916±0.037	19.703±0.027	1.05	18.436±0.051	-	-	2	1.14	17.599±0.084
P20	0.04	20.845±0.033	20.356±0.026	19.986±0.015	19.705±0.110	19.738±0.136	-	-	-	-	-	-	17.605±0.264
P21	0.47	20.637±0.036	20.107±0.075	19.741±0.027	19.581±0.157	19.419±0.176	0.30	18.502±0.089	-	18.143±0.281	1	-	-
P22	0.08	21.130±0.044	20.498±0.110	20.090±0.017	19.816±0.114	19.426±0.182	0.23	18.471±0.075	-	17.957±0.228	1	2.26	(16.792±0.057)
P23	0.18	21.583±0.027	20.962±0.052	20.517±0.049	20.230±0.035	-	0.17	18.987±0.126	-	-	1	-	(16.602±0.118)
P24	0.09	21.686±0.026	21.137±0.094	20.565±0.082	20.322±0.057	19.810±0.177	0.16	19.187±0.148	-	-	1	-	-
P25	0.25	21.334±0.025	20.715±0.036	20.223±0.059	19.975±0.044	19.674±0.146	0.13	18.452±0.084	-	17.620±0.145	1	-	-
P26	0.17	21.596±0.126	20.950±0.040	20.534±0.085	20.160±0.045	19.976±0.197	0.46	18.383±0.074	-	17.555±0.148	1	-	-
P27	0.02	21.096±0.035	20.453±0.073	19.990±0.024	19.701±0.015	19.757±0.096	0.14	18.427±0.076	-	17.771±0.178	1	-	-
P28	0.06	21.561±0.023	20.893±0.059	20.433±0.028	20.171±0.093	-	-	-	-	-	0.94	17.634±0.091	18.467±0.506
P29	0.03	21.703±0.079	21.001±0.056	20.513±0.026	20.168±0.084	-	0.05	19.013±0.136	-	-	1	-	-
P30	0.08	21.689±0.135	21.003±0.068	20.465±0.043	20.116±0.019	19.732±0.080	0.12	18.904±0.148	-	-	2	-	-
P31	0.04	21.613±0.075	20.916±0.060	20.429±0.019	20.049±0.046	19.580±0.141	0.14	18.795±0.095	-	17.805±0.177	1	-	-
P32	0.10	20.979±0.055	20.293±0.030	19.792±0.022	19.411±0.019	19.260±0.058	0.14	17.802±0.033	17.107±0.031	17.005±0.055	3	-	-
P33	0.18	21.712±0.006	20.875±0.085	20.529±0.019	20.164±0.087	-	-	-	-	-	-	-	-
P34	0.03	21.790±0.046	20.993±0.048	20.393±0.041	20.018±0.021	19.674±0.101	0.02	18.545±0.084	-	-	2	0.14	18.118±0.186
P35	0.23	21.575±0.037	20.686±0.122	20.188±0.005	19.820±0.118	19.800±0.142	0.34	18.261±0.067	-	17.851±0.193	1	-	18.066
P36	0.01	22.022±0.139	21.188±0.026	20.503±0.082	20.105±0.010	19.806±0.139	0.10	18.681±0.061	18.453±0.103	18.181±0.126	3	-	-
P37	0.09	21.368±0.075	20.568±0.033	19.927±0.110	19.480±0.058	19.343±0.026	0.19	18.062±0.069	-	17.484±0.164	1	-	-

Notes. *JHK<sub>s</sub>*-band photometry (P) from 1) VHS, 2) UHS, 3) UKIDSS GPS, 4) UKIDSS LAS, 5) VMC, 6) VVV, and 7) VIKING (3–4: *K* - instead of *K<sub>s</sub>* band). *W 1* *W 2* magnitudes in parenthesis; less coincidental counterparts. <sup>a</sup> *Z*=19.065±0.231, *Y*=18.538±0.233 (6). <sup>b</sup> *Y*=18.870±0.047 (1). <sup>c</sup> *Y*=19.676±0.071 (5). <sup>d</sup> *Y*=19.714±0.102 (4). <sup>e</sup> *Z*=20.088±0.033, *Y*=19.796±0.053 (7). <sup>f</sup> *Y*=19.959±0.138 (4). <sup>g</sup> *Y*=20.259±0.277 (1). <sup>h</sup> *Z*=20.286±0.208 (UKIDSS GCS). <sup>i</sup> *Y*=20.137±0.146 mag (4).

Table E2. SDSS and NSC photometry of the sources.

Flag	Sep ( $r'$ )	$u$ SDSS (mag)	$g$ SDSS (mag)	$r$ SDSS (mag)	$i$ SDSS (mag)	$z$ SDSS (mag)	Sep ( $r'$ )	$g$ NSC (mag)	$r$ NSC (mag)	$i$ NSC (mag)	$z$ NSC (mag)	$Y$ NSC (mag)
$\gamma_a$	-	-	-	-	-	-	0.29	-	19.958±0.085	19.009±0.056	-	-
$\gamma_b$	-	-	-	-	-	-	0.20	22.690±0.101	21.111±0.038	20.188±0.035	19.621±0.035	19.209±0.048
$\gamma_c$	-	-	-	-	-	-	0.09	21.655±0.030	20.501±0.013	20.157±0.025	19.720±0.032	19.449±0.052
$\gamma_d$	-	-	-	-	-	-	-	-	-	-	-	-
$\gamma_e$	-	-	-	-	-	-	-	-	-	-	-	-
X2	-	-	-	-	-	-	0.04	20.852±0.009	20.220±0.007	20.089±0.009	19.955±0.015	19.821±0.067
X_a	-	-	-	-	-	-	0.20	21.273±0.018	20.589±0.020	20.177±0.022	20.079±0.028	19.898±0.054
X_b	-	-	-	-	-	-	0.20	20.909±0.019	20.275±0.013	19.930±0.026	19.751±0.032	19.656±0.063
X_c	-	-	-	-	-	-	0.18	20.431±0.013	19.924±0.009	19.707±0.012	19.600±0.016	19.576±0.041
X_d	-	-	-	-	-	-	-	-	-	-	-	-
X_e	-	-	-	-	-	-	0.18	-	20.488±0.020	-	-	-
UV1	-	-	-	-	-	-	0.09	20.449±0.007	20.818±0.005	21.070±0.033	21.344±0.091	-
UV2	-	-	-	-	-	-	0.23	19.922±0.013	-	19.641±0.015	-	-
UV3	-	-	-	-	-	-	0.02	20.747±0.017	20.939±0.020	-	-	-
UV4	-	-	-	-	-	-	0.02	20.016±0.015	-	-	-	-
UV5	-	-	-	-	-	-	0.10	21.109±0.080	20.812±0.040	-	20.688±0.106	-
UV6	-	-	-	-	-	-	0.15	20.007±0.012	-	19.406±0.016	-	-
UV7	-	-	-	-	-	-	0.13	20.518±0.006	20.435±0.007	20.213±0.008	20.211±0.018	20.224±0.040
UV8	0.15	21.638±0.116	21.564±0.045	21.072±0.039	20.198±0.038	19.587±0.061	0.04	21.472±0.017	21.075±0.014	-	19.698±0.010	-
UV9	0.06	21.954±0.154	21.416±0.044	21.328±0.048	20.619±0.043	19.956±0.087	0.01	21.476±0.099	21.390±0.091	-	19.912±0.014	-
UV10	-	-	-	-	-	-	0.05	-	-	-	-	-
UV11	0.04	22.563±0.030 <sup>a</sup>	21.647±0.100	20.960±0.071	20.722±0.073	20.447±0.153	0.12	21.106±0.006	20.660±0.008	20.490±0.005	20.351±0.008	20.098±0.035
UV12	0.23	21.774±0.169	20.726±0.028	20.436±0.028	20.308±0.035	19.805±0.101	0.20	20.638±0.009	20.374±0.007	-	20.250±0.025	-
UV13	0.15	20.792±0.091	21.440±0.054	20.137±0.038	19.891±0.024	19.591±0.056	0.11	21.101±0.011	20.159±0.005	19.966±0.007	19.731±0.009	19.475±0.027
UV14	0.04	22.497±0.293	21.565±0.048	20.510±0.028	20.052±0.026	19.623±0.065	0.03	21.500±0.031	20.495±0.015	-	19.952±0.019	-
UV15	0.09	21.699±0.190	21.699±0.057	20.661±0.038	20.459±0.052	19.999±0.109	0.03	21.408±0.027	20.772±0.021	-	20.199±0.029	-
Rad1	0.18	-	21.424±0.049	20.867±0.055	20.624±0.067	20.553±0.180	-	-	-	-	-	-
Rad_a	-	-	-	-	-	-	-	-	-	-	-	-
Rad_b	-	21.337±0.129 <sup>a</sup>	-	-	-	-	0.15	20.198±0.012	20.208±0.012	20.113±0.011	20.133±0.021	-
Rad_c	-	-	-	-	-	-	0.36	20.406±0.010	19.752±0.010	19.482±0.017	19.337±0.020	19.252±0.042
Rad_d	-	-	-	-	-	-	0.02	22.000±0.039	-	20.312±0.028	-	-
Rad_e	-	-	-	-	-	-	0.04	21.891±0.092	20.609±0.055	20.234±0.052	19.781±0.066	18.828±0.138
Rad_f	-	-	-	-	-	-	-	-	-	-	-	-
Rad_g	-	-	-	-	-	-	0.07	-	21.212±0.023	-	-	-
P0	0.07	20.804±0.080	20.705±0.030	20.968±0.048	21.165±0.086	21.213±0.278	0.09	20.651±0.053	20.998±0.075	-	-	-
P1X1	-	-	-	-	-	-	-	-	-	-	-	-
P2	0.05	21.350±0.121	20.754±0.031	20.751±0.048	21.007±0.096	21.077±0.321	0.06	20.688±0.011	20.721±0.020	20.833±0.054	20.984±0.054	-
P3	0.01	-	21.208±0.042	20.555±0.031	20.467±0.035	20.324±0.095	0.03	21.010±0.016	20.626±0.016	-	20.801±0.024	-
P4	-	-	-	-	-	-	0.03	21.062±0.024	21.016±0.029	20.938±0.043	20.620±0.045	-
P5	0.14	22.571±0.349	21.195±0.043	20.800±0.043	20.719±0.055	20.865±0.218	0.02	21.068±0.015	20.911±0.021	-	20.636±0.032	-
P6	-	21.198±0.022 <sup>a</sup>	-	-	-	-	0.01	20.742±0.009	20.926±0.007	20.472±0.012	20.434±0.022	-
P7	-	-	-	-	-	-	0.18	20.571±0.013	-	19.515±0.025	-	-
P8	-	-	-	-	-	-	0.01	21.485±0.017	21.031±0.022	20.842±0.024	20.726±0.064	20.781±0.198
P9	-	-	-	-	-	-	0.42	19.788±0.012	-	-	-	-
P10	-	-	-	-	-	-	0.01	21.350±0.019	20.932±0.008	20.753±0.017	-	20.721±0.073
P11	-	-	-	-	-	-	-	-	-	-	-	-
P12	0.17	22.497±0.302	21.162±0.036	20.518±0.029	20.334±0.034	20.350±0.113	0.24	-	-	20.136±0.019	-	-
P13	-	-	-	-	-	-	0.01	21.484±0.037	21.049±0.022	-	20.682±0.037	-
P14	-	-	-	-	-	-	0.33	21.065±0.037	20.430±0.015	20.081±0.032	-	-
P15	0.11	23.056±0.403	21.552±0.048	20.975±0.039	20.583±0.039	20.486±0.117	0.02	-	-	-	20.562±0.050	-
P16	-	-	-	-	-	-	0.13	20.906±0.027	20.359±0.018	20.141±0.022	-	-
P17	-	-	-	-	-	-	0.05	20.531±0.008	19.922±0.008	19.662±0.013	19.601±0.016	19.446±0.033
P18	0.08	-	21.418±0.050	20.961±0.047	20.893±0.065	20.564±0.172	0.04	21.264±0.019	20.745±0.018	-	20.214±0.034	-
P19	0.20	22.194±0.364	21.111±0.050	20.512±0.044	20.110±0.040	19.635±0.104	0.48	20.940±0.017	20.397±0.015	-	19.594±0.015	-
P20	-	-	-	-	-	-	0.31	-	20.265±0.009	-	-	-
P21	-	-	-	-	-	-	0.53	20.090±0.018	19.970±0.008	19.294±0.019	19.239±0.035	19.458±0.078
P22	-	-	-	-	-	-	0.21	-	-	19.900±0.015	-	-
P23	-	-	-	-	-	-	0.18	-	20.727±0.014	-	-	-
P24	-	-	-	-	-	-	0.16	-	20.774±0.019	-	-	-
P25	-	-	-	-	-	-	0.48	20.939±0.018	20.243±0.009	20.009±0.026	19.830±0.032	20.016±0.213
P26	-	-	-	-	-	-	0.06	-	20.837±0.020	-	-	-
P27	-	-	-	-	-	-	0.09	-	20.389±0.012	-	-	-
P28	-	-	-	-	-	-	0.03	21.857±0.031	20.846±0.023	20.234±0.023	19.982±0.027	19.789±0.049
P29	-	-	-	-	-	-	0.02	21.807±0.045	20.982±0.013	20.484±0.031	-	-
P30	-	-	-	-	-	-	0.10	-	-	-	-	-
P31	-	-	-	-	-	-	0.04	21.673±0.030	20.979±0.019	20.448±0.022	20.188±0.033	20.045±0.058
P32	-	-	-	-	-	-	0.51	-	19.997±0.019	-	-	-
P33	-	-	-	-	-	-	0.12	21.619±0.041	20.688±0.019	20.247±0.021	20.007±0.025	20.089±0.069
P34	-	-	-	-	-	-	-	-	-	-	-	-
P35	-	-	-	-	-	-	0.40	-	20.060±0.018	-	-	-
P36	-	-	-	-	-	-	-	-	-	-	-	-
P37	-	-	-	-	-	-	0.04	21.809±0.025	20.601±0.013	19.978±0.026	19.604±0.028	19.352±0.049

Notes. SDSS DR13  $u$ - and  $z$ -band zeropoint corrections of -0.04 and 0.02 mag are applied according to <https://www.sdss.org/dr13/algorithms/fluxcal/#counts2mag>. <sup>a</sup>  $u$ -band magnitude from NSC.

**Table E3.** PS1- and infrared photometry of other sources.

Flag	Sep ( $\prime\prime$ )	$g$ PS1 (mag)	$r$ PS1 (mag)	$i$ PS1 (mag)	$z$ PS1 (mag)	$y$ PS1 (mag)	Sep ( $\prime\prime$ )	$J$ (mag)	$H$ (mag)	$K_s$ (mag)	P	Sep ( $\prime\prime$ )	W 1 (mag)	W 2 (mag)
DZ-E	0.22	21.590±0.107	20.767±0.029	19.898±0.017	19.651±0.013	19.709±0.070	0.15	19.135±0.131	–	–	1	–	–	–
DC1	0.03	20.192±0.012	19.324±0.007	19.469±0.011	19.744±0.026	20.012±0.046	–	–	–	–	–	–	–	–
DQpec	0.01	18.262±0.028	16.404±0.001	15.968±0.003	16.005±0.002	16.012±0.006	0.09	15.125±0.046	14.720±0.063	14.535±0.078	8	0.25	14.251±0.016	14.202±0.025
RC1	0.04	22.069±0.179	21.511±0.023	20.179±0.023	19.544±0.016	19.153±0.042	0.14	18.192±0.054	–	–	2	1.73	(17.017±0.057)	(16.832±0.132)
RC2	0.03	–	21.727±0.042	20.225±0.026	19.530±0.021	19.137±0.035	0.08	17.850±0.053	–	–	2	0.30	16.875±0.046	17.006±0.145
RC3	–	–	–	–	–	–	0.08	17.782±0.045	17.304±0.049	17.035±0.077	1	0.08	16.678±0.026	17.121±0.110
RC4 <sup>a</sup>	0.03	–	21.442±0.153	20.034±0.028	19.319±0.013	18.952±0.023	0.14	17.582±0.068	17.205±0.088	16.759±0.080	1	0.26	16.557±0.041	16.524±0.108
RC5	–	–	–	–	–	–	0.05	17.365±0.017	–	16.654±0.043	1	0.27	16.446±0.029	16.437±0.072
DZQH	–	–	–	–	–	–	0.23	17.581±0.015	–	17.625±0.091	1	0.13	16.965±0.051	16.717±0.126
VR	0.60	20.795±0.044	19.023±0.005	18.231±0.005	17.961±0.006	17.823±0.018	0.06	17.000±0.021	–	16.931±0.098	1	–	–	–

Notes.  $JHK_s$  photometry (P) from 1) VHS, 2) UHS, 3) UKIDSS GPS, 4) UKIDSS LAS, 5) VMC, 6) VVV, 7) VIKING, and 8) 2MASS (3–4:  $K$  - instead of  $K_s$  band). <sup>a</sup>  $Y=18.295±0.073$  (1).

**Table E4.** SDSS and NSC photometry of other sources.

Flag	Sep ( $\prime\prime$ )	$u$ SDSS (mag)	$g$ SDSS (mag)	$r$ SDSS (mag)	$i$ SDSS (mag)	$z$ SDSS (mag)	Sep ( $\prime\prime$ )	$g$ NSC (mag)	$r$ NSC (mag)	$i$ NSC (mag)	$z$ NSC (mag)	$Y_{NSC}$ (mag)
DZ-E	–	–	–	–	–	–	0.15	21.654±0.030	–	19.939±0.015	–	–
DC1	0.11	22.382±0.292	20.366±0.028	19.349±0.028	19.458±0.023	19.909±0.084	0.14	20.189±0.007	19.395±0.006	19.641±0.022	20.059±0.014	–
DQpec	0.08	18.210±0.022	18.242±0.025	16.411±0.017	15.962±0.018	16.012±0.014	0.11	18.205±0.003	16.331±0.002	–	16.101±0.002	–
RC1	0.06	–	23.186±0.187	21.458±0.060	20.181±0.032	19.441±0.049	0.05	22.875±0.060	21.426±0.023	–	19.487±0.014	–
RC2	0.04	–	23.481±0.282	21.724±0.114	20.296±0.048	19.523±0.070	0.06	–	–	20.079±0.017	–	–
RC3	–	–	–	–	–	–	0.03	23.059±0.032	21.601±0.012	20.000±0.005	19.310±0.005	19.129±0.013
RC4	0.15	–	–	21.739±0.091	20.115±0.039	19.113±0.064	0.01	23.078±0.177	21.588±0.045	19.926±0.006	19.219±0.019	–
RC5	–	–	–	–	–	–	0.01	23.677±0.078	22.029±0.021	19.880±0.007	19.001±0.006	18.746±0.014
DZQH	–	–	–	–	–	–	0.02	21.433±0.014	19.925±0.006	19.366±0.006	19.043±0.007	18.956±0.021
VR	–	–	–	–	–	–	0.56	20.719±0.095	18.625±0.016	18.094±0.013	–	–

Note. SDSS DR13  $u$ - and  $z$ -band zeropoint corrections of -0.04 and 0.02 mag are applied according to <https://www.sdss.org/dr13/algorithms/fluxcal/#counts2mag>.